

Stoichiometry and Mole Concept (Part 1)

Learning Objectives:

- define relative atomic mass, A_r
- define relative molecular mass M_r , and calculate relative molecular mass (and relative formula mass) as the sum of relative atomic masses
- calculate the percentage mass of an element in a compound when given appropriate information
- calculate empirical and molecular formulae from relevant data
- calculate stoichiometric reacting masses and volumes of gases (one mole of gas occupies 24.0 dm^3 at room temperature and pressure); calculations involving the idea of limiting reactants may be set
- apply the concept of solution concentration (in mol/dm^3 or g/dm^3) to process the results of volumetric experiments and to solve simple problems
- calculate percentage yield and percentage purity

1.1 Relative Atomic Mass, A_r

- Definition: The **relative atomic mass (A_r) of an element is the average mass of one atom of the element when compared with $\frac{1}{12}$ the mass of one atom of carbon-12.**

$$\text{Relative atomic mass, } A_r = \frac{\text{average mass of one atom of the element}}{\frac{1}{12} \text{ mass of an atom of carbon-12}}$$

- Relative atomic mass is a ratio and has no unit.
- The relative atomic masses of some elements are given below:

Element	Relative atomic mass (A_r)
hydrogen	1.0
carbon	12.0
oxygen	16.0
chlorine	35.5
magnesium	24.3

Some A_r values are not whole numbers

- Why are some A_r values not whole numbers?

Example: Why is A_r of chlorine 35.5?

The A_r of an element has to take into account the masses of all the isotopes of the element and their relative abundances.

Chlorine exists as a mixture of two isotopes, 75.0% of chlorine-35 and 25.0% of chlorine-37.

$$\begin{aligned}\text{Hence, the relative atomic mass of chlorine} &= (0.75 \times 35) + (0.25 \times 37) \\ &= 26.25 + 9.25 \\ &= \underline{35.5}\end{aligned}$$

Sum of the A_r of all the atoms in a molecule

1.2 Relative Molecular Mass and Relative Formula Mass, M_r

- Definition: The **relative molecular mass (M_r) of a molecule is the average mass of one molecule of a substance when compared with $\frac{1}{12}$ the mass of one atom of carbon-12.**

<p>Relative molecular mass, $M_r = \frac{\text{average mass of one molecule of an element or a compound}}{\frac{1}{12} \text{ mass of an atom of carbon-12}}$</p>
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- Relative molecular mass is a ratio and has no unit.
- To find the M_r of a molecule, we just **add up the relative atomic masses of all atoms** in the molecule.
- Ionic** compounds such as sodium chloride and magnesium nitrate **consist of ions and not molecules**. Hence, for ionic compounds, the term **relative formula mass (M_r)** is used instead of relative molecular mass.

Example: Find the relative molecular mass/relative formula mass of

- (a) carbon dioxide (b) ammonia gas (c) sucrose, $C_{12}H_{22}O_{11}$ (d) $CuSO_4 \cdot 5H_2O$

(a) M_r of carbon dioxide = $(1 \times 12.0) + (2 \times 16.0)$

= 44.0

(b) M_r of ammonia gas = $(1 \times 14.0) + (3 \times 1.0)$

= 17.0

(c) M_r of $C_{12}H_{22}O_{11}$ = $(12 \times 12.0) + (22 \times 1.0) + (11 \times 16.0)$

= 342.0

(d) M_r of $CuSO_4 \cdot 5H_2O$ = $(1 \times 63.5) + (1 \times 32.1) + (4 \times 16.0) + (5 \times 18.0)$

= 249.6

Quick Check 1

Homework

Calculate the relative molecular mass/relative formula mass of the following substances:

(a) H_2SO_4 = $(2 \times 1.0) + (1 \times 32.1) + (4 \times 16.0)$ = 98.1	(b) $Ca(NO_3)_2$ = $(1 \times 40.1) + 2[(1 \times 14.0) + (3 \times 16.0)]$ = 164.1
(c) $(NH_4)_2Cr_2O_7$ = $2[(1 \times 14.0) + (4 \times 1.0)] + (2 \times 52.0) + (7 \times 16.0)$ = 252	(d) $Cu(NH_3)_4SO_4$ = $(1 \times 63.5) + 4[(1 \times 14.0) + (3 \times 1.0)] + (1 \times 32.1) + (4 \times 16.0)$ = 229.60
(e) CH_3COOH = $(1 \times 12.0) + (3 \times 1.0) + (1 \times 12.0) + (2 \times 16.0) + (1 \times 12.0)$ = 71	(f) $Na_2CO_3 \cdot 10H_2O$ = $(2 \times 23) + (1 \times 12.0) + (3 \times 16.0) + 10[(2 \times 1.0) + (1 \times 16.0)]$ = 286
(g) $K_2SO_4 \cdot Al_2(SO_4)_3 \cdot 24H_2O$ = $(2 \times 39.1) + (1 \times 32.1) + (4 \times 16.0) + (2 \times 27) + 3[(1 \times 32.1) + (4 \times 16.0)] + 24[(2 \times 1.0) + (1 \times 16.0)]$ = 2666.9	

$$M_r \text{ of water} = 18.0$$

2.1 Composition of Compounds by Mass

The percentage of an element in a compound by mass

$$= \frac{\text{No. of atoms of the element in the formula} \times A_r \text{ of the element}}{M_r \text{ of the compound}} \times 100\%$$

Example 1

What is the percentage by mass of hydrogen present in hydrogen peroxide, H_2O_2 ?

$$M_r \text{ of } H_2O_2 = (2 \times 1.0) + (2 \times 16.0) = 34.0$$

percentage by mass of hydrogen in H_2O_2

$$= \frac{1.0 \times 2}{34.0} \times 100\%$$

$$= 5.88\% \text{ (3 s.f.)}$$

Example 2

What is the percentage of water in copper(II) sulfate crystals, $CuSO_4 \cdot 5H_2O$?

Percentage by mass of water in $CuSO_4 \cdot 5H_2O$

$$= \frac{5 \times 18.0}{63.5 + 32.1 + (4 \times 16.0) + (5 \times 18.0)} \times 100\% \rightarrow M_r \text{ of } CuSO_4 \cdot 5H_2O$$

$$= \frac{5 \times 18.0}{249.6} \times 100\%$$

$$\text{Quick Check 2} = 36.1\% \text{ (3 s.f.)}$$

1 Calculate the following:

(a) percentage of carbon in ethanoic acid, CH_3COOH

(b) percentage of water in $Na_2CO_3 \cdot 10H_2O$

2(a) Percentage of carbon in ethanoic acid

$$= \frac{12.0 \times 2}{12.0 + (3 \times 1.0) + 12.0 + 16.0 + 16.0 + 1.0}$$

$$= \frac{24.0}{60.0} \times 100\%$$

$$= 40.0\% \text{ (3 s.f.)}$$

b) Percentage of water in $Na_2CO_3 \cdot 10H_2O$

$$= \frac{18.0 \times 10}{(2 \times 23.0) + (12.0) + (3 \times 16.0) + (10 \times 18.0)} \times 100\%$$

$$= 62.9\% \text{ (3 s.f.)}$$

penalised if not 3 s.f.

2 An iron ore extraction involves the extraction of haematite, which contains Fe_2O_3 , and magnetite, which contains Fe_3O_4 . Which has greater percentage of iron by mass, Fe_2O_3 or Fe_3O_4 ?

$$\% \text{ of Fe in } Fe_2O_3 = \frac{(2 \times 55.8)}{(2 \times 55.8) + (3 \times 16.0)} \times 100\%$$

$$= 69.9\% \text{ (3 s.f.)}$$

$$\% \text{ of Fe in } Fe_3O_4 = \frac{(3 \times 55.8)}{(3 \times 55.8) + (4 \times 16.0)} \times 100\%$$

Therefore, Fe_3O_4 contains greater % of Fe. = 72.3% (3 s.f.)

Note: What is the percentage of oxygen in Fe_3O_4 ? Answer: 27.7

Sum of percentages of individual elements in compound = 100 %

2.2 Calculating the Mass of an Element/Water of Crystallisation in a Compound

The mass of an element in a sample of a compound

$$= \frac{\text{No. of atoms of the element in the formula} \times A_r \text{ of the element}}{M_r \text{ of the compound}} \times \text{Mass of sample}$$

Example 1

Calculate the mass of oxygen in 32.0 g of copper(II) sulfate, CuSO_4 .

$$\begin{aligned} \text{Mass of oxygen(O) in CuSO}_4 &= \frac{4 \times \text{Relative atomic mass of O}}{\text{Relative formula mass of CuSO}_4} \times \text{mass of sample} \\ &= \frac{4 \times 16.0}{63.5 + 32.1 + 4(16.0)} \times 32.0 \\ &= 12.8 \text{ g (3 s.f.)} \end{aligned}$$

Example 2

Calculate the mass of water in 12.5 g of hydrated copper(II) sulfate, $\text{CuSO}_4 \cdot 5\text{H}_2\text{O}$.

$$\begin{aligned} \text{Mass of water(H}_2\text{O) in CuSO}_4 \cdot 5\text{H}_2\text{O} &= \frac{5 \times \text{Relative molecular mass of H}_2\text{O}}{\text{Relative formula mass of CuSO}_4 \cdot 5\text{H}_2\text{O}} \times \text{mass of sample} \\ &= \frac{5 \times 18.0}{249.6} \times 12.5 \text{ g} \\ &= 4.51 \text{ g (3 s.f.)} \end{aligned}$$

Quick Check 3

1 Calculate the mass of

- calcium in 25.0 g of calcium carbonate;
- chlorine in 27.0 g of copper(II) chloride;
- water in 54.1 g of $\text{FeCl}_3 \cdot 6\text{H}_2\text{O}$.

$$\begin{aligned} \text{a) Mass of calcium in CaCO}_3 &= \frac{40.1}{40.1 + (16.0 \times 3) + 12.0} \times 25.0 \\ &= 10.0 \text{ g (3 s.f.)} \end{aligned}$$

$$\begin{aligned} \text{b) Mass of chlorine in CuCl}_2 &= \frac{35.5 \times 2}{63.5 + (35.5 \times 2)} \times 27.0 \\ &= 14.3 \text{ g (3 s.f.)} \end{aligned}$$

$$\begin{aligned} \text{c) Mass of water in FeCl}_3 \cdot 6\text{H}_2\text{O} &= \frac{6(18.0)}{55.8 + (35.5 \times 3) + 6(18.0)} \times 54.1 \\ &= 21.6 \text{ g (3 s.f.)} \end{aligned}$$

2 A sample of iron chloride has the formula FeCl_n where n is a whole number. If the percentage of chlorine in the compound is 65.5%, what is the value of n ? $n=3$

Percentage

$$\text{Mass of chlorine in FeCl}_n = \underline{65.5\%}$$

$$\begin{aligned} \text{Percentage of iron in FeCl}_n &= 100\% - 65.5\% \\ &= 34.5\% \end{aligned}$$

$$34.5\% = 55.8$$

$$1\% = 1.6174$$

$$100\% = 161.74$$

$$\text{value of } n = \frac{161.74 - 55.8}{35.5}$$

$$= 2.98 \text{ (2 s.f.)}$$

3.1 The Mole and Avogadro's Number

- The mole is the **counting unit** used by chemists for very small particles such as atoms, molecules, ions and electrons.
- It is taken from the Latin word, "moles", meaning "heap" or "pile".
- One mole of a substance contains the same number of particles as the number of atoms in 12 g of carbon-12.**
- The number of atoms in 12 g of the carbon-12 isotopes is known as **Avogadro's constant/Avogadro's number**.

Its value is 6.02×10^{23} .

- The symbol of mole is mol. The SI unit for the amount of substance is mole.
- One mole of any substance contains 6.02×10^{23} particles.

Items	Unit used to count	Number of items in one unit
socks	pair	2
eggs	dozen	12
bottles	carton	24
papers	ream	500
atoms, molecules, ions, electrons	mole	6.02×10^{23}

Examples

(a) 1 mole of neon, Ne, contains 6.02×10^{23} neon atoms.

(b) 1 mole of hydrogen gas, H_2 , contains
1 mole of hydrogen molecules or 6.02×10^{23} hydrogen molecules,
2 moles of hydrogen atoms or $2 \times (6.02 \times 10^{23})$ hydrogen atoms.

(c) 1 mole of methane gas, CH_4 , contains
1 mole of methane molecules or 6.02×10^{23} methane molecules,
1 mole of carbon atoms or 6.02×10^{23} carbon atoms,
4 moles of hydrogen atoms or $4 \times 6.02 \times 10^{23}$ hydrogen atoms.

(d) 1 mole of sodium chloride, NaCl, contains
1 mole of formula units(NaCl) or 6.02×10^{23} formula units(NaCl),
1 mole of sodium ions or 6.02×10^{23} sodium ions,
1 mole of chloride ions or 6.02×10^{23} chloride ions.

(e) 1 mole of magnesium chloride, $MgCl_2$, contains
1 mole of formula units($MgCl_2$) or 6.02×10^{23} formula units($MgCl_2$),
1 mole of magnesium ions or 6.02×10^{23} magnesium ions,
2 moles of chloride ions or $2 \times 6.02 \times 10^{23}$ chloride ions.

- Since 1 mole of a substance contains 6.02×10^{23} particles, we can use a convenient formula to find the number of moles of particles in a substance.

Number of moles = $\frac{\text{number of particles}}{6.02 \times 10^{23}}$

Final answer: 3 s.f

Example 1

How many moles of water are there in 3.00×10^{24} molecules of water?

$$\begin{aligned} \text{Number of moles of water molecules} \\ = \frac{\text{number of water molecules}}{6.02 \times 10^{23}} \end{aligned}$$

$$= \frac{3.00 \times 10^{24}}{6.02 \times 10^{23}} = 4.98 \text{ mol}$$

Example 2

How many atoms are there in 0.300 mol of iron?

Number of iron atoms

$$= \text{number of moles of iron atoms} \times 6.02 \times 10^{23}$$

$$= 0.300 \times 6.02 \times 10^{23}$$

$$= 1.81 \times 10^{23} //$$

Example 3

What is the number of (a) ammonia molecules; (b) nitrogen atoms; (c) hydrogen atoms in 0.250 moles of ammonia gas?

a) Number of ammonia molecules

$$= 0.250 \times 6.02 \times 10^{23}$$

$$= 1.51 \times 10^{23}$$

c) Number of hydrogen atoms

$$= 0.250 \times 6.02 \times 10^{23} \times 3$$

$$= 4.52 \times 10^{23} //$$

b) Number of nitrogen atoms

$$= 0.250 \times 6.02 \times 10^{23}$$

$$= 1.51 \times 10^{23} //$$

Quick Check 4

1 Calculate the number of moles of atoms in 2.40×10^{25} molecules of hydrogen gas, H_2 .

Number of moles of atoms in 2.40×10^{25} molecules of H_2

$$= \frac{2 \times 2.40 \times 10^{25}}{6.02 \times 10^{23}}$$

$$= 79.7 \text{ mol}$$

$\rightarrow \text{Zn}(\text{NO}_3)_2$

2 Calculate the number of (a) zinc ions and (b) nitrate ions in 0.500 moles of zinc nitrate.

$$\begin{aligned} \text{a) Number of zinc ions: } & 0.500 \times 6.02 \times 10^{23} \\ & = 3.01 \times 10^{23} // \end{aligned}$$

$$\begin{aligned} \text{b) Number of nitrate ions: } & 0.500 \times 6.02 \times 10^{23} \times 2 \\ & = 6.02 \times 10^{23} // \end{aligned}$$

3 Given 0.250 moles of carbon dioxide, calculate

(a) the number of carbon dioxide molecules,

(b) the number of atoms that are present.

a) Number of CO_2 molecules

$$= 0.250 \times 6.02 \times 10^{23}$$

$$= 1.505 \times 10^{23}$$

$$= 1.51 \times 10^{23} // \quad (3 \text{ s.f})$$

b) Number of atoms that are present

$$= 3 \times 1.505 \times 10^{23}$$

$$= 4.515 \times 10^{23}$$

$$= 4.52 \times 10^{23} //$$

3.2 Molar Mass

- Molar mass is the mass of one mole of any substance.

(i) For substances consisting of atoms

The molar mass is the relative atomic mass of the element in grams per mole (g/mol).

E.g. Molar mass of carbon = 12.0 g/mol

Molar mass of sodium = 23.0 g/mol

(ii) For substances consisting of molecules

The molar mass is the relative molecular mass of the substance in grams per mole.

E.g. Molar mass of oxygen gas = $16 \times 2 = 32.0$ g/mol

Molar mass of water = 18.0 g/mol

(iii) For substances consisting of ions

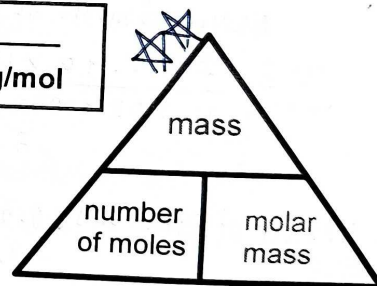
The molar mass is the relative formula mass of the substance in grams per mole.

E.g. Molar mass of sodium chloride = $23.0 + 35.5 = 58.5$ g/mol

Molar mass of ammonium sulfate = $2[14.0 + (4 \times 1.0)] + 32.1 + (4 \times 16.0) = 132.1$ g/mol (132.0 g/mol (3 s.f.))

- If we know the mass of a substance, we can calculate the number of moles using the formula:

$\text{Number of moles of substance} = \frac{\text{Mass of substance in g}}{\text{Molar mass of substance in g/mol}}$



Example 1

Calculate the number of moles of atoms in 8.00 g of helium. monatomic (Noble gas)

Number of moles of atoms in 8.00 g of helium

$$= \frac{8.00}{4.0 \text{ g/mol}} = 2.00 \text{ mol}$$

Example 2

Calculate the number of moles of molecules in 4.50 g of water. 1/20

Number of moles of ~~at~~ molecules in 4.50 g of water

$$= \frac{4.50}{2(1.0) + 16.0}$$

$$= 0.250 \text{ mol}$$

Example 3

Calculate the mass of 0.400 moles of iron atoms.

Mass of 0.400 moles of iron atoms

$$= 0.400 \times 55.8$$

$$= 22.32 = 22.3 \text{ g/mol}$$

Example 4

Calculate the number of chloride ions in 6.66 g of calcium chloride.

Number of moles of Cl^- in 6.66 g of calcium chloride

$$= \frac{6.66}{40.1 + 2(35.5)} \times 2$$

$$= 0.11989 \text{ mol} \quad (5\text{s.f.})$$

Number of Cl^- in 6.66 g of CaCl_2

$$= 0.11989 \times 6.02 \times 10^{23}$$

Example 5

0.250 mol of fructose has a mass of 45.0 g. What is the relative molecular mass of fructose?

Relative molecular mass of fructose

$$\text{Molar mass of fructose} = \frac{45.0}{0.250}$$

$$= 180.0 \text{ g/mol}$$

Relative molecular mass of fructose = 180.0 (NO UNITS)

Quick Check 5

1 Calculate the number of moles of atoms for each of the following:

(a) 32.0 g of oxygen

(b) 8.00 g of calcium

(c) 3.00×10^{23} iodine atoms(d) 1.50×10^{24} carbon atoms

a) Number of moles of atoms for 32.0 g of oxygen

$$= \frac{32.0}{2 \times 16.0 \text{ g/mol}} \times 2$$

$$= 2.00 \text{ mol} \quad (3\text{s.f.})$$

b) Number of moles of atoms for 8.00 g of calcium

$$= \frac{8.00}{40.1 \text{ g/mol}}$$

$$= 0.200 \text{ mol} \quad (3\text{s.f.})$$

c) Number of moles of atoms for 3.00×10^{23} iodine atoms

$$= \frac{3.00 \times 10^{23}}{6.02 \times 10^{23}}$$

$$= 0.498 \text{ mol} \quad (3\text{s.f.})$$

d) Number of moles of atoms for 1.50×10^{24} carbon atoms

$$= \frac{1.50 \times 10^{24}}{6.02 \times 10^{23}}$$

$$= 2.49 \text{ mol} \quad (3\text{s.f.})$$

2 Calculate the number of moles of molecules for each of the following:

(a) 32.0 g of sulfur dioxide

(b) 20.0 g of nitrogen gas

(c) 2.40×10^{23} molecules of hydrogen(d) 12.0×10^{24} molecules of ammoniaa) Number of moles of molecules for 32.0 g of SO_2

$$= \frac{32.0}{(32.1) + (2 \times 16.0) \text{ g/mol}}$$

$$= 0.499 \text{ mol} \quad (3\text{s.f.})$$

b) Number of moles of molecules for 20.0 g of N_2

$$= \frac{20.0}{2(14.0) \text{ g/mol}}$$

$$= 0.714 \text{ mol} \quad (3\text{s.f.})$$

c) Number of moles of molecules for 2.40×10^{23} molecules of hydrogen

$$= \frac{2.40 \times 10^{23}}{6.02 \times 10^{23}}$$

$$= 0.399 \text{ mol} \quad (3\text{s.f.})$$

d) Number of moles of molecules for 12.0×10^{24} molecules of ammonia

$$= \frac{12.0 \times 10^{24}}{6.02 \times 10^{23}}$$

$$= 19.9 \text{ mol} \quad (3\text{s.f.})$$

3 Calculate the mass of each of the following:

(a) 0.600 mole of magnesium chloride

(c) 6.00×10^{23} atoms of copper

(b) 2.00 moles of oxygen gas

(d) 1.20×10^{24} molecules of chlorine gas

a) Mass of 0.600 mole of magnesium chloride

$$= (0.600)(24.3 + 35.5)$$

$$= 35.88$$

$$= 35.9 \text{ g (3s.f.)}$$

b) Mass of 2.00 moles of oxygen gas

$$= (2.00)(16.0 \times 2)$$

$$= 64 \text{ g}$$

$$= 64.0 \text{ g (3s.f.)}$$

c) Mass of 6.00×10^{23} atoms of copper

$$= 6.00 \times 10^{23} \times (63.5)$$

$$= 3.81 \times 10^{25}$$

d) Mass of 1.20×10^{24} molecules of chlorine gas

$$= 1.20 \times 10^{24} \times (35.5 \times 2)$$

$$= 85.2 \times 10^{24} \text{ g}$$

4 How many hydrogen chloride, HCl molecules would have a mass of 292 g?

$$\text{Number of moles of HCl} = \frac{\text{mass of HCl}}{\text{molar mass of HCl}} = \frac{292}{1.0 + 35.5}$$

$$= 8.00 \text{ mol (3s.f.)}$$

$$\text{Number of molecules of HCl} =$$

5 What is the number of (a) molecules; (b) atoms in 4.50 g of water?

a) Number of moles of molecules in 4.50 g of water

$$= \frac{4.50}{18.0}$$

$$= 0.250 \text{ mol (3s.f.)}$$

Number of molecules in 4.50 g of water

$$= 0.250 \times 6.02 \times 10^{23}$$

$$= 1.505 \times 10^{23} \times 3$$

$$= 4.51 \times 10^{23}$$

b) Number of moles of atoms in 4.50 g of water

$$= 0.250 \times 6.02 \times 10^{23} \times 3$$

$$= 4.52 \times 10^{23} \text{ (3s.f.)}$$

6 How many ions are there in 60.0 g of magnesium chloride?

Number of moles of ions in 60.0 g of MgCl₂

$$= \frac{60.0}{24.3 + (35.5 \times 2)}$$

$$= 0.62959 \text{ mol}$$

$$\text{Number of ions} = 0.62959 \text{ mol}$$

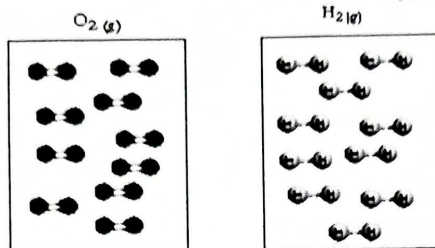
3.3 Molar Volume of Gases

- Avogadro's Law states that equal volumes of all gases, under the same temperature and pressure contain the same number of particles.

→ Will not give same mass
→ Different molar mass



Amedeo Avogadro



Equal Volumes and the Same Temperature and Pressure

- Molar volume** of a gas is the volume occupied by one mole of any gas.
- At **room conditions** (i.e. **20°C** and **1 atmospheric pressure**), one mole of any gas at r.t.p. has a volume of **24.0 dm³** or **24000 cm³**. This volume is called **molar volume** of a gas at r.t.p.
- Examples: Molar volume of oxygen gas at r.t.p. = 24.0 dm³
Molar volume of helium gas at r.t.p. = 24.0 dm³
Molar volume of carbon dioxide at r.t.p. = 24.0 dm³
- The conditions of temperature and pressure must be specified.
 - If temperature decreases, what happens to the molar volume of gas?
The molar volume decreases.
 - At standard temperature (0 °C) and pressure (1 bar) (s.t.p.), the molar volume of a gas is **22.7 dm³**.
- Since at r.t.p., one mole of a gas would occupy a volume of 24.0 dm³, we can use a convenient formula to find the number of moles of a gas.



Number of moles of a gas = $\frac{\text{Volume of gas}}{\text{Molar volume of gas}}$	← 24.0 dm ³ at r.t.p.
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Example 1

Calculate the number of moles of carbon dioxide in 3.00 dm³ of the gas at r.t.p.

Number of moles in carbon dioxide in 3.00 dm³ of CO₂ at r.t.p.

$$= \frac{3.00}{24.0}$$

$$= 0.125 \text{ mol}$$

Example 2

Calculate the volume of 0.550 moles of methane gas at r.t.p.

Volume of 0.550 moles of methane gas at r.t.p.

$$= 0.550 \times 24.0$$

$$= 13.2 \text{ dm}^3 \text{ (3 s.f.)}$$

Example 3

Calculate the volume of 4.50 g of oxygen gas at r.t.p.

Volume of 4.50 g of oxygen gas at r.t.p.

$$= \frac{4.50}{2(16.0)} \times 24.0 \text{ dm}^3$$

$$= 3.38 \text{ dm}^3 \text{ (3 s.f.)}$$

→ No. of moles of O₂ = $\frac{4.50}{2(16.0)}$

= 0.14063 mol

Volume of O₂ = 0.14063 × 24.0

$$= 3.38 \text{ dm}^3$$

Example 4

What is the mass of 12.0 dm^3 of carbon dioxide at r.t.p.?

$$\begin{aligned}\text{Number of moles of } \text{CO}_2 &= \frac{12.0}{24.0} \\ &= 0.500 \text{ mol}\end{aligned}$$

$$\begin{aligned}\text{Mass of } \text{CO}_2 &= \text{no. of moles} \times \text{molar mass} \\ &= 0.500 \times [12.0 + (2 \times 16.0)] \\ &= 0.500 \times 44.0 \\ &= 22.0 \text{ g}\end{aligned}$$

Quick Check 6

1 Calculate the volume of the following gases at r.t.p.

(a) 0.200 mol of oxygen,

(b) 3.00 mol of hydrogen

Q1a) Volume of 0.200 mol of oxygen at r.t.p

$$\begin{aligned}&= 0.200 \times 24.0 \\ &= 4.80 \text{ dm}^3\end{aligned}$$

b) Volume of 3.00 mol of hydrogen at r.t.p

$$\begin{aligned}&= 3.00 \times 24.0 \\ &= 72.0 \text{ dm}^3\end{aligned}$$

2 Calculate the number of moles of molecules of the following gases:

(a) 12.0 dm^3 of nitrogen at r.t.p.,

(b) 150 cm^3 of carbon monoxide at r.t.p.

Q2

$$\begin{aligned}\text{a) Number of moles of molecules of } 12.0 \text{ dm}^3 \text{ of nitrogen at r.t.p} \\ &= \frac{12.0}{24.0} \\ &= 0.5 \text{ mol}\end{aligned}$$

$$\text{b) } 150 \text{ cm}^3 = 0.15 \text{ dm}^3$$

$$\begin{aligned}\text{Number of moles of molecules of } 150 \text{ cm}^3 \text{ of carbon monoxide at r.t.p} \\ &= \frac{0.15}{24.0} \\ &= 0.00625 \text{ mol}\end{aligned}$$

3 Calculate the mass of the following gases at r.t.p.

(a) 12.0 dm^3 of hydrogen,

(b) 480 cm^3 of carbon dioxide

Q3a) Number of moles of hydrogen

$$\begin{aligned}&= \frac{12.0}{24.0} \\ &= 0.500 \text{ mol}\end{aligned}$$

$$\begin{aligned}\text{Mass of hydrogen} &= 0.500 \times [(1.0) \times 2] \\ &= 1.00 \text{ g (3 s.f.)}\end{aligned}$$

b) Number of moles of CO_2

$$\begin{aligned}&= \frac{480}{24.0} \\ &= 20.0 \text{ mol} \\ \text{Mass of carbon dioxide} &= 20.0 \times [12.0 + 2(16.0)] \\ &= 880 \text{ g}\end{aligned}$$



4 Calculate the volume of the following gases at r.t.p.

(a) 14.0 g of nitrogen,

(b) 3.20 g of sulfur dioxide, SO_2

(c) 1.80×10^{23} molecules of chlorine gas

a) Number of moles of nitrogen

$$= \frac{14.0}{2(14.0 \text{ g/mol})}$$

$$= 0.500 \text{ mol (3s.f.)}$$

Volume of 14.0 g of nitrogen at r.t.p.

$$= 0.500 \times 24.0$$

$$= 12 \text{ dm}^3 //$$

b) Number of moles of sulfur dioxide

$$= \frac{3.20}{32.1 + 2(16.0) \text{ g/mol}}$$

$$= 0.049922 \text{ (5s.f.)}$$

Volume of 3.20 g of sulfur dioxide at r.t.p.

$$= 0.049922 \times 24$$

$$= 1.20 \text{ dm}^3 \text{ (3s.f.)}$$

5 A sample of carbon monoxide gas has a volume of 6.00 dm^3 at r.t.p.

Calculate

(a) the number of moles of gas,

(b) the number of molecules, $\rightarrow \text{mol} \times (6.02 \times 10^{23})$

(c) the number of atoms,

(d) the mass of the carbon monoxide sample

a) Number of moles of gas in sample

$$= \frac{6.00}{24.0}$$

$$= 0.25 \text{ mol} //$$

b) Number of molecules in sample

$$= 0.25 \times 6.02 \times 10^{23}$$

$$= 1.505 \times 10^{23}$$

$$= 1.51 \times 10^{23} // \text{ (3s.f.)}$$

c) Number of atoms in sample

$$= 1.505 \times 10^{23} \times 2$$

$$= 3.01 \times 10^{23} // \text{ (3s.f.)}$$

d) Mass of the carbon monoxide sample

$$= 0.25 \times (12.0 + 16.0)$$

$$= 7.00 \text{ g} // \text{ (3s.f.)}$$

c) Number of moles of atoms for 1.80×10^{23} molecules of chlorine gas

$$= \frac{1.80 \times 10^{23}}{6.02 \times 10^{23}}$$

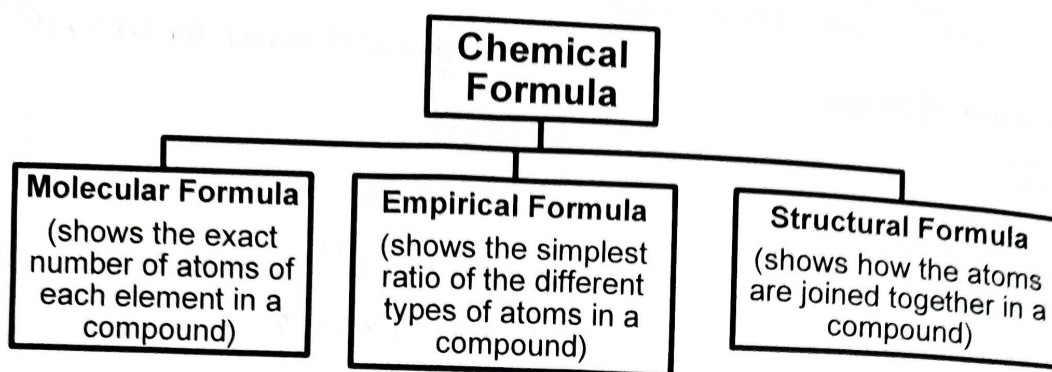
$$= 0.29900 \text{ mol (5s.f.)}$$

Volume of 1.80×10^{23} molecules of chlorine gas at r.t.p.

$$= 0.29900 \times 24.0$$

$$= 7.18 \text{ dm}^3 //$$

4. Empirical and Molecular Formulae



Example : **Ethane**

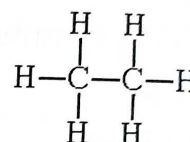
Molecular formula:



Empirical formula:



Structural formula:



Compound	Molecular Formula	Empirical Formula
Water	H ₂ O	H ₂ O
Methane	CH ₄	CH ₄
Hydrogen Peroxide	H ₂ O ₂	H ₂ O
Glucose	C ₆ H ₁₂ O ₆	CH ₂ O
Ethene	C ₂ H ₄	CH ₂
Propene	C ₃ H ₆	CH ₂

Molecular formula same as its empirical formula

Molecular formula is a multiple of its empirical formula

Different compounds, same empirical formula

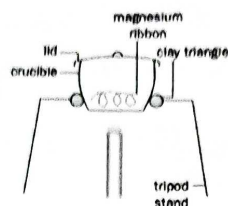
4. Calculating the Empirical Formula from Masses of Elements that are combined together

- The empirical formula of a compound can be found from the masses of elements that are combined together.
- The number of moles of atoms that are combined together are determined.
- The empirical formula is obtained using the simplest mole ratio of the atoms.

Exact : (3s.f)
Non-Exact : (5s.f)

Example 1

To determine the empirical formula of magnesium oxide, magnesium ribbon is heated in a crucible as shown below.



The following results are obtained:

Mass of crucible + lid	= 26.52 g
Mass of crucible + lid + magnesium	= 27.72 g
Mass of crucible + lid + magnesium oxide	= 28.52 g

Mass of magnesium burnt = $27.72 - 26.52 = 1.20$ g

Mass of oxygen that combined with magnesium = $28.52 - 27.72 = 0.80$ g

	Magnesium (Mg)	Oxygen (O)
Step 1 Write down the mass of each element (g)	1.20	0.80
Step 2 Write down the molar mass of each element (g/mol)	24.3	16.0
Step 3 Divide each mass by its molar mass to obtain the number of moles of each element (mol)	0.049383 (5s.f)	0.0500 (3s.f)
Step 4 Divide each no. of moles by the smallest number	$\frac{0.049383}{0.049383} = 1$	$\frac{0.0500}{0.049383} = 1$ (3s.f)

Empirical formula of magnesium oxide is MgO

Example 2

30.0 g of aluminium sulfide contains 19.2 g of sulfur. Find the empirical formula of the compound.

Element	Aluminium (Al)	Sulfide (S)
Mass (g)	$30.0\text{g} - 19.2\text{g}$ $= 10.8\text{g}$	19.2
Molar mass (g/mol)	27.0	32.1
No. of moles (mol)	$\frac{10.8}{27.0} = 0.400$	$\frac{19.2}{32.1} = 0.59813$
Simplest ratio	$\frac{0.400}{0.400} = 1$ $1 \times 2 = 2$	$\frac{0.59813}{0.400} \approx 1.5$ $1.5 \times 2 = 3$

Empirical formula of the compound is Al₂S₃

4. Calculating the Molecular Formula from Empirical Formula

The molecular formula can be calculated from the empirical formula and relative molecular mass.

Example 1

Propene has the empirical formula CH_2 . The relative molecular mass of propene is 42.0. Find the molecular formula of propene.

Let the molecular formula of propene be $(\text{CH}_2)_n$

$$M_r \text{ of } (\text{CH}_2)_n = 42.0$$

$$[12.0 + (1.0 \times 2)] \times n = 42.0$$

$$14.0n = 42.0$$

$$n = \frac{42.0}{14.0} = 3$$

Therefore, molecular formula of propene is C_3H_6

Example 2

Caffeine is a compound found in coffee and tea. The percentage composition of caffeine is 49.5% carbon, 5.10% hydrogen, 16.5% oxygen and 28.9% nitrogen.

The relative molecular mass of caffeine is 194. Determine the

- empirical formula
- molecular formula

- When percentage composition of the compound is given instead of masses of the elements, we assume 100 g of the compound is analysed.
- Each percentage then gives the mass of the element in grams in terms of 100 g of the compound

Let the mass of caffeine be 100g

Element	C	H	O	N
Mass in 100g (g)	49.5	5.10	16.5	28.9
Molar mass (g/mol)	12.0	1.0	16.0	14.0
NO. of moles (mol)	$\frac{49.5}{12.0} = 4.125$	$\frac{5.10}{1.0} = 5.10$	$\frac{16.5}{16.0} = 1.0313$	$\frac{28.9}{14.0} = 2.0643$
Simplest ratio	$\frac{4.125}{1.0313} \approx 4$	$\frac{5.10}{1.0313} \approx 5$	$\frac{1.0313}{1.0313} = 1$	$\frac{2.0643}{1.0313} \approx 2$

(a) Empirical formula of caffeine is $\text{C}_4\text{H}_5\text{ON}_2$

(b) Let the molecular formula of caffeine be $(\text{C}_4\text{H}_5\text{ON}_2)_n$

$$M_r \text{ of } (\text{C}_4\text{H}_5\text{ON}_2)_n = 194$$

$$[(12.0 \times 4) + (1.0 \times 5) + 16.0 + (14.0 \times 2)]_n = 194$$

Therefore, molecular formula of caffeine is $\text{C}_8\text{H}_{10}\text{O}_2\text{N}_4$

$$97.0n = 194$$

$$n = \frac{194}{97.0} = 2$$

Quick Check 7

1 Find the empirical formulae of the following:

- (a) a compound consisting of 3.50 g of nitrogen combined with 8.00 g of oxygen;
 (b) a compound consisting of 5.37 g of iron combined with 4.63 g sulfur.

a)

Element	Nitrogen	Oxygen
Mass (g)	3.50	8.00
Molar mass (g/mol)	14.0	16.0
No. of moles (mol)	0.25	0.5
Simplest Ratio	$\frac{0.25}{0.25} = 1$	$\frac{0.5}{0.25} = 2$

The empirical formula of the compound is NO_2 //

b)

Element	iron	sulfur
Mass (g)	5.37	4.63
Molar mass (g/mol)	55.8	32.1
No. of moles (mol)	0.096237	0.14424
Simplest Ratio	$\frac{0.096237}{0.096237} = 1$	$\frac{0.14424}{0.096237} = 1.5$

$$1:1.5 = 2:3$$

The empirical formula of compound is Fe_2S_3 //

2 Find the empirical formulae of the following:

- (a) a compound with composition 46.7% silicon and 53.3% oxygen by mass;
 (b) a compound with composition 10.0% carbon, 0.84% hydrogen and 89.1% chlorine by mass.

a)

element	silicon	oxygen
Percentage	46.7	53.3
Mass in 100g	46.7 46.7	53.3
molar (g/mol)	28.1	32.0
No. of moles (mol)	$\frac{46.7}{28.1} = 1.6619 \text{ (5sf)}$	$\frac{53.3}{32.0} = 1.6656 \text{ (5sf)}$
Simplest Ratio	$\frac{1.6619}{1.6619} = 1$	$\frac{1.6656}{1.6619} = 1.0022 \text{ (5sf)}$

$$\text{Ratio} = 1:1 \Rightarrow \text{SiO}_2$$

Empirical formulae = SiO_2 //

b)

Element	Carbon	Hydrogen	Chlorine
Mass in 100g	10.0	0.84	89.1
molar mass (g/mol)	12.0	2.0	71
No. of moles (mol)	$\frac{10.0}{12.0} = 0.8333$	0.420	1.2549
Simplest Ratio	$\frac{0.8333}{0.420} = 2$	$\frac{0.420}{0.420} = 1$	$\frac{1.2549}{0.420} = 3$

$$\frac{19.840}{20} = 1$$

$$\frac{29.879}{29.879} = 1$$

$$\frac{29.879}{29.879} = 1$$

	Carbon	Hydrogen	Chlorine
Mass in 100g	10.0	0.84	89.1
molar mass (g/mol)	12.0	1.0	71
No. of moles	0.8333	0.84	1.2549
Simplest Ratio	$\frac{0.8333}{0.8333} = 1$	$\frac{0.84}{0.8333} = 1$	$\frac{1.2549}{0.8333} = 1.5$

$$\text{or } 1:1:1.5 = 2:2:3$$

- formula = $\text{C}_2\text{H}_2\text{Cl}_3$ //

3

A carbohydrate contains 54.5% carbon, 9.1% hydrogen, the balance being oxygen.

(a) Find the empirical formula of the carbohydrate.

(b) If the relative molecular mass of the carbohydrate is 88, what is its molecular formula?

Percentage of oxygen in the carbohydrate

$$= 100 - 54.5 - 9.1$$

$$= 36.4\%$$

Let mass of carbohydrate be 100g

Element	carbon	hydrogen	oxygen
mass in 100g	54.5	9.1	36.4
molar mass (g/mol)	12.0	1.0	32.0
No. of moles (mol)	$\frac{54.5}{12.0} = 4.54167$	$\frac{9.1}{1.0} = 9.1$	$\frac{36.4}{32.0} = 1.1375$
Simplest Ratio	$\frac{4.54167}{1.1375} = 3.9923$	$\frac{9.1}{1.1375} = 8$	$\frac{1.1375}{1.1375} = 1$

a) Empirical formula of carbohydrate: C_4H_8O

b) Let the molecular formula be $(C_4H_8O)_n$

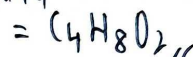
$$Mr \text{ of } (C_4H_8O)_n = 88$$

$$[2(12.0) + 4(1.0) + 32.0]n = 88$$

$$60n = 88$$

$$n = \frac{88}{60} = 1.4667$$

\therefore Molecular formula



4 The following results were obtained in an experiment to determine the formula of an oxide of silicon.

Mass of crucible = 15.20 g

Mass of crucible + silicon = 15.48 g

Mass of crucible + oxide of silicon = 15.80 g

(a) Find the empirical formula of the oxide of silicon.

(b) If the mass of 1 mole of the oxide of silicon is 60.0 g, what is its molecular formula?

$$a) \text{ Mass of silicon} = 15.48 \text{ g} - 15.20 \text{ g}$$

$$= 0.28 \text{ g}$$

$$\text{Mass of oxygen reacted with silicon} = 15.80 \text{ g} - 15.48 \text{ g}$$

$$= 0.32 \text{ g}$$

Element	Si	O
mass	0.28	0.32
molar mass	28.1	16.0
No. of moles	$\frac{0.28}{28.1} = 0.009664$ $= 0.01$	$\frac{0.32}{16.0} = 0.02$
Simplest Ratio	$\frac{0.01}{0.01} = 1$	$\frac{0.02}{0.01} = 2$

ANSWERS TO QUICK CHECK

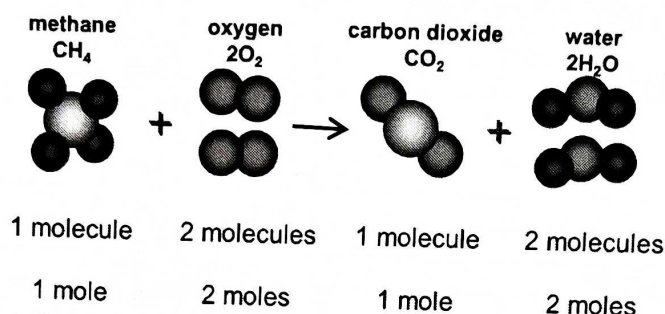
	Quick Check 1 (pg 2)		Quick Check 5 (pg 8 - 9)
(a)	98.1	3(a)	57.2 g
(b)	164.1	3(b)	64.0 g
(c)	252.0	3(c)	63.3 g
(d)	227.6	3(d)	142 g
(e)	60.0	4	4.82×10^{24}
(f)	286.0	5(a)	1.51×10^{23}
(g)	948.6	5(b)	4.52×10^{23}
		6	1.14×10^{24}
	Quick Check 2 (pg 3)		
1(a)	40.0 %		
1(b)	62.9 %		
2	69.9 % ; 72.3% ; Fe_3O_4 ; 27.7% ; 100%		Quick Check 6 (pg 11 - 12)
		1(a)	4.80 dm ³
		1(b)	72.0 dm ³
	Quick Check 3 (pg 4)		
1(a)	10.0 g	2(a)	0.500 mol
1(b)	14.3 g	2(b)	0.00625 mol
1(c)	21.6 g	3(a)	1.00 g
2	3	3(b)	0.880 g
		4(a)	12.0 dm ³
		4(b)	1.20 dm ³
	Quick Check 4 (pg 6)		
1	79.7 mol	4(c)	7.18 dm ³
2(a)	3.01×10^{23}	5(a)	0.250 mol
2(b)	6.02×10^{23}	5(b)	1.51×10^{23}
3(a)	1.51×10^{23}	5(c)	3.01×10^{23}
3(b)	4.52×10^{23}	5(d)	7.00 g
	Quick Check 5 (pg 8 - 9)		Quick Check 7 (pg 16 - 17)
1(a)	2.00 mol	1(a)	NO_2
1(b)	0.200 mol	1(b)	Fe_2S_3
1(c)	0.498 mol	2(a)	SiO_2
1(d)	2.49 mol	2(b)	CHCl_3
2(a)	0.499 mol	3(a)	$\text{C}_2\text{H}_4\text{O}$
2(b)	0.714 mol	3(b)	$\text{C}_4\text{H}_8\text{O}_2$
2(c)	0.399 mol	4(a)	SiO_2
2(d)	19.9 mol	4(b)	SiO_2

Stoichiometry and Mole Concept (Part 2)

5.1 Calculations from Equations

- A balanced chemical equation provides information on:
 - reactants used
 - products formed
 - ratio** of the **number of moles** of reactants and products i.e. **mole ratio**
- A balanced chemical equation enables us to calculate amount of reactants required and products formed. The amount can be expressed in terms of mass, volume or number of moles.

Example



The chemical equation tells us that:

- 1 molecule of CH₄ reacts with 2 molecules of O₂ to produce 1 molecule of CO₂ and 2 molecules of H₂O.
- 1 x 6.02 x 10²³ molecules of CH₄ react with 2 x 6.02 x 10²³ molecules of O₂ to produce 1 x 6.02 x 10²³ molecules of CO₂ and 2 x 6.02 x 10²³ molecules of H₂O.
- 1 mol of CH₄ reacts with 2 mol of O₂ to produce 1 mol of CO₂ and 2 mol of H₂O.

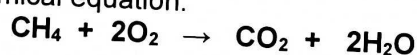
The relationship between the number of moles of reactants and the number of moles of products involved in a chemical reaction is known as its **stoichiometry**.

Example 1

Calculate the mass of water produced when 0.250 mole of methane is completely burnt in oxygen.

Solution

Step 1: Write the balanced chemical equation.



Step 2: Find the **ratio** of the **number of moles** of H₂O to the number of moles of CH₄.

$$\frac{\text{No. of moles of H}_2\text{O}}{\text{No. of moles of CH}_4} = \frac{2}{1}$$

Step 3: Use the ratio to find the number of moles of H₂O produced when 0.250 moles of CH₄ is burnt.

$$\begin{aligned} \text{No. of mole of H}_2\text{O} &= \frac{2}{1} \times \text{no. of moles of CH}_4 \\ &= 2 \times 0.250 \\ &= \underline{0.500 \text{ mol}} \end{aligned}$$

Step 4: Convert the number of moles of H₂O produced to mass of H₂O.

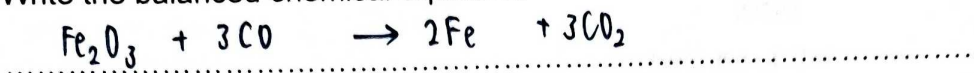
$$\begin{aligned} \text{Mass of H}_2\text{O} &= \text{no. of moles of H}_2\text{O} \times \text{molar mass of H}_2\text{O} \\ &= 0.500 \times 18.0 \\ &= \underline{9.00 \text{ g (3 s.f.)}} \end{aligned}$$

Example 2

Iron(III) oxide reacts with carbon monoxide to form iron and carbon dioxide.
What mass of iron is produced from 40.0 g of iron(III) oxide?

Solution

Step 1: Write the balanced chemical equation.



Step 2: Convert 40.0 g of Fe_2O_3 to number of moles of Fe_2O_3 .

$$\text{No. of moles of Fe}_2\text{O}_3 = \frac{40.0}{(2 \times 55.8) + (3 \times 16.0)} = 0.25063 \text{ mol}$$

Step 3: Find the ratio of the number of moles of Fe to the number of moles of Fe_2O_3 .

$$\frac{\text{No. of moles of Fe}}{\text{No. of moles of Fe}_2\text{O}_3} = \frac{2}{1}$$

Step 4: Use the ratio to find the number of moles of Fe produced.

$$\begin{aligned} \text{No. of moles of Fe produced} &= \frac{2}{1} \times \text{no. of moles of Fe}_2\text{O}_3 \text{ reacted} \\ &= \frac{2}{1} \times 0.25063 \\ &= 0.50126 \text{ mol} \end{aligned}$$

Step 5: Convert the number of moles of Fe produced to mass of Fe.

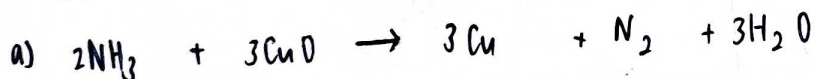
$$\begin{aligned} \text{Mass of Fe} &= 0.50126 \times 55.8 \\ &= 28.0 \text{ g (3 s.f.)} \end{aligned}$$

Example 3

Ammonia gas reacts with hot copper(II) oxide to form copper, nitrogen gas and water.

(a) Write a balanced equation for the reaction.

(b) If 2.00 g of copper(II) oxide is used, find the volume of ammonia gas required at r.t.p.



$$\begin{aligned} \text{b) Number of moles of CuO} &= \frac{2.00}{(63.5 + 16.0)} \\ &= 0.025157 \text{ mol} \end{aligned}$$

$$\frac{\text{No. of moles of NH}_3}{\text{No. of moles of CuO}} = \frac{2}{3}$$

$$\begin{aligned} \text{No. of moles of NH}_3 &= \frac{2}{3} \times 0.025157 \\ &= 0.016771 \text{ mol} \end{aligned}$$

$$\begin{aligned} \text{Volume of NH}_3 &= 0.016771 \times 24.0 \\ &= 0.403 \text{ dm}^3 \text{ (3 s.f.)} \end{aligned}$$

Example 4

Sodium reacts with water to form sodium hydroxide and hydrogen gas. Calculate the mass of sodium that reacts with water to produce 240 cm³ of hydrogen at r.t.p.



$$\text{No. of moles of H}_2 = \frac{240}{24000}$$

$$= 0.0100 \text{ mol}$$

$$\frac{\text{No. of moles of Na}}{\text{No. of moles of H}_2} = \frac{2}{1}$$

$$\text{No. of moles of Na} = \frac{2}{1} \times \text{No. of moles of H}_2$$

$$= \frac{2}{1} \times 0.0100$$

$$= 0.0200 \text{ mol}$$

$$\text{Mass of Na} = \text{No. of moles} \times \text{molar mass}$$

$$= 0.0200 \times 23.0$$

$$= 0.460 \text{ g}$$

Quick Check 1

- 1 In an experiment, 2.80 g of iron was reacted with excess hydrochloric acid. The equation for the reaction is



Calculate

- (a) the mass of iron(II) chloride produced in the reaction, 6.36
(b) the volume of hydrogen gas produced, measured at r.t.p. 1.20 dm³

$$\begin{aligned} \text{a) No. of moles of Fe} &= 2.80 \div 55.8 \\ &= 0.050179 \text{ mol} \end{aligned}$$

$$\frac{\text{No. of moles of FeCl}_2}{\text{No. of moles of Fe}} = \frac{1}{1}$$

$$\text{No. of moles of FeCl}_2 = 0.050179 \text{ mol}$$

$$\begin{aligned} \text{Mass of FeCl}_2 &= 0.050179 \times (55.8 + 35.5 \times 2) \\ &= 6.36 \text{ g (3 s.f.)} \end{aligned}$$

$$\begin{aligned} \text{b) } \frac{\text{No. of moles of H}_2}{\text{No. of moles of Fe}} &= \frac{1}{1} \end{aligned}$$

$$\begin{aligned} \text{Volume of H}_2 &= 0.050179 \times 24.0 \\ &= 1.20 \text{ dm}^3 \text{ (3 s.f.)} \end{aligned}$$

- 2 Magnesium burns brilliantly in a gas jar of carbon dioxide to form magnesium oxide and carbon.
- (a) Write a balanced equation for the reaction.
- (b) If 1.20 g of magnesium is completely burnt, calculate
- the volume of carbon dioxide used up, at r.t.p.
 - the mass of magnesium oxide formed.

- ③ Potassium chlorate(V) decomposes when strongly heated. The equation is



Calculate the mass of potassium chlorate(V) required to produce 12.0 dm^3 of oxygen gas at r.t.p.

$$\frac{\text{No. of moles of KClO}_3}{\text{No. of moles of O}_2} = \frac{2}{3}$$

$$\text{No. of moles of O}_2 = 3 \times \frac{12.0}{24.0} = 1.50 \text{ mol}$$

$$\text{No. of moles of KClO}_3 = 1.50 \times \frac{2}{3} = 1$$

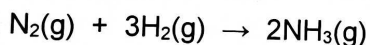
$$\begin{aligned} \text{Mass of potassium chlorate required} &= 2[39.1 + 35.5 + 3(16.0)] \\ &= 245.2 \text{ g} \end{aligned}$$

6.1 Calculations for Volumes of Reacting Gases

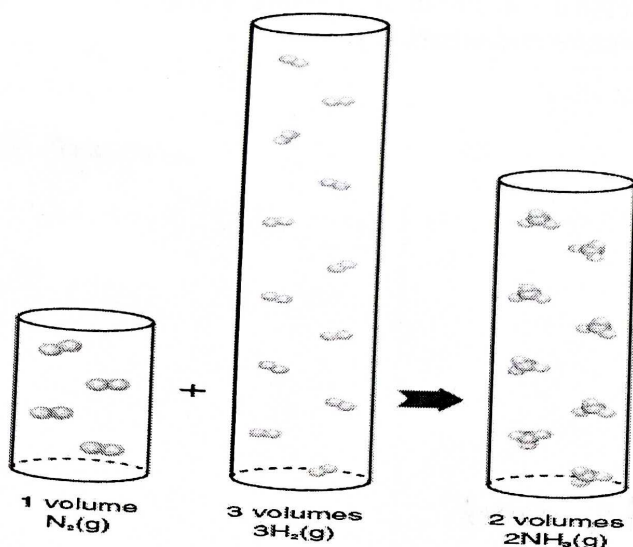
- According to Avogadro's Law, the volume of a gas in a reaction is **proportional** to the number of moles of the gas.
- For reactions involving gaseous reactants and products, the **mole ratio** is **the same** as the **volume ratio** of the gases (provided all volumes are measured at the **same temperature and pressure**).

Example

Nitrogen gas and hydrogen gas reacts to form ammonia.



Mole ratio	1	3	2
Volume ratio	1	3	2
Volume / cm^3	10.0	30.0	20.0



According to the equation,

$$\frac{\text{No. of moles of H}_2}{\text{No. of moles of N}_2} = \frac{3}{1}$$

According to Avogadro's Law,

$$\frac{\text{Volume of H}_2}{\text{Volume of N}_2} = \frac{3}{1}$$

$$\text{Volume of H}_2 = 3 \times \text{volume of N}_2$$

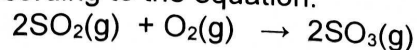
We can extend this to the volume of NH_3 produced.

E.g.

If 10.0 cm^3 of N_2 reacts, the volume of H_2 that reacts is 30.0 cm^3 and the volume of NH_3 produced is 20.0 cm^3 .

Example 1

Sulfur dioxide reacts with oxygen according to the equation:



40.0 cm³ of sulfur dioxide reacted with oxygen to form sulfur trioxide.

Calculate

- (a) the volume of oxygen reacted.
- (b) the volume of sulfur trioxide formed.

(All volumes are measured at the same temperature and pressure.)

Solution

(a) From equation,

$$\frac{\text{No. of moles of O}_2}{\text{No. of moles of SO}_2} = \frac{1}{2}$$

According to Avogadro's Law, $\frac{\text{volume of O}_2}{\text{volume of SO}_2} = \frac{1}{2}$

Hence, volume of O₂ reacted = $\frac{1}{2} \times$ volume of SO₂ reacted

$$\begin{aligned} &= \frac{1}{2} \times 40.0 \text{ cm}^3 \\ &= 20.0 \text{ cm}^3 \end{aligned}$$

(b) From equation,

$$\frac{\text{No. of moles of SO}_3}{\text{No. of moles of SO}_2} = \frac{1}{1}$$

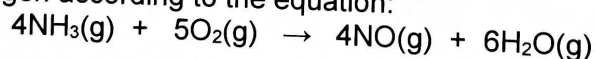
According to Avogadro's Law, $\frac{\text{volume of SO}_3}{\text{volume of SO}_2} = \frac{1}{1}$

Hence, volume of SO₃ formed = $\frac{1}{1} \times$ volume of SO₂ reacted

$$= 40.0 \text{ cm}^3$$

Example 2

Ammonia reacts with oxygen according to the equation:



Calculate the volume of ammonia gas that reacted if 100 cm³ of oxygen gas is used.
(All volumes are measured at the same temperature and pressure.)

From equation,

$$\frac{\text{No. of moles of NH}_3}{\text{No. of moles of O}_2} = \frac{4}{5}$$

According to Avogadro's Law,

$$\frac{\text{Volume of NH}_3}{\text{Volume of O}_2} = \frac{4}{5}$$

Volume of NH₃ reacted = $\frac{4}{5} \times$ volume of O₂ reacted

$$= 80 \text{ cm}^3$$

Quick Check 2

1 40.0 cm³ of ammonia gas was decomposed according to the equation:
$$2\text{NH}_3(\text{g}) \rightarrow \text{N}_2(\text{g}) + 3\text{H}_2(\text{g})$$

Calculate

- (a) the volume of nitrogen gas produced,
(b) the volume of hydrogen gas produced.

(All volumes are measured at the same temperature and pressure.)

a) From equation,

$$\frac{\text{No. of moles of N}_2}{\text{No. of moles of NH}_3} = \frac{1}{2}$$

According to Avogadro's Law, $\frac{\text{Volume of N}_2}{\text{Volume of NH}_3} = \frac{1}{2}$

$$\begin{aligned}\text{Volume of nitrogen gas produced} &= 40.0 \times \frac{1}{2} \\ &= 20.0 \text{ cm}^3\end{aligned}$$

From equation,

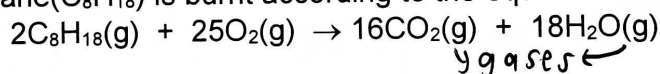
$$\frac{\text{No. of moles of H}_2}{\text{No. of moles of NH}_3} = \frac{3}{2}$$

According to Avogadro's Law,

$$\frac{\text{Volume of H}_2}{\text{Volume of NH}_3} = \frac{3}{2}$$

$$\begin{aligned}\text{Volume of hydrogen gas produced} &= 40.0 \times \frac{3}{2} \\ &= 60.0 \text{ cm}^3\end{aligned}$$

2 In the motor engine, octane (C₈H₁₈) is burnt according to the equation:



In the hot engine, all the substances in the equation are gases. In the combustion of 40.0 cm³ of gaseous octane, calculate

- (a) the volume of oxygen gas used,
(b) the total volume of gaseous products produced. → Volume of all

(All volumes are measured at the same temperature and pressure.)

a) From equation,

$$\frac{\text{No. of moles of O}_2}{\text{No. of moles of C}_8\text{H}_{18}} = \frac{25}{2}$$

According to Avogadro's law,

$$\frac{\text{Volume of O}_2}{\text{Volume of C}_8\text{H}_{18}} = \frac{25}{2}$$

$$\begin{aligned}\text{Volume of O}_2 \text{ used} &= 40.0 \times \frac{25}{2} \\ &= 500 \text{ cm}^3\end{aligned}$$

b)

$$\frac{\text{No. of moles of gaseous products produced}}{\text{No. of moles of C}_8\text{H}_{18}} = \frac{16+18}{2} = \frac{34}{2}$$

According to Avogadro's law

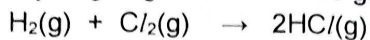
$$= \frac{\text{Volume of gaseous products produced}}{\text{No. of moles of C}_8\text{H}_{18}}$$












$$\begin{aligned}&= \frac{34}{2} \\ \text{Volume of gaseous products produced} &= \frac{34}{2} \times 40.0 \\ &= 680 \text{ cm}^3\end{aligned}$$

7.1 Limiting Reactant

- The limiting reactant is the reactant that is completely **used up** in a reaction and it **limits** the amount of products formed.

Example: Reaction between hydrogen gas and chlorine gas to give hydrogen chloride gas



Experiment	Amount of reactants used		Amount of products formed		
	Hydrogen (H ₂)	Chlorine (Cl ₂)	Hydrogen chloride (HCl)	Unreacted hydrogen	Unreacted chlorine
A	1	1	2	0	0
					All the reactants are used up.
B	2	1	2	1	0
					Excess hydrogen is used. Hence, some hydrogen is unreacted. In this case, chlorine is the limiting reactant.
C	1	2	2	0	1
					 Excess chlorine is used. Hence, some chlorine is unreacted. In this case, hydrogen is the limiting reactant.

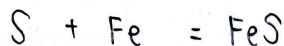
The amount of a product formed in a reaction is always determined by the amount of the **limiting reactant** (the reactant that is used up).

Example 1

A mixture containing 8.00 g of sulfur and 8.00 g of iron filings is heated to form iron(II) sulfide. Identify the limiting and excess reactant and calculate the mass of iron(II) sulfide formed.

Solution

Step 1: Write the balanced chemical equation.



Step 2: Convert the mass of iron and sulfur given into number of moles.

$$\begin{aligned} \text{No. of moles of Fe given} &= \frac{8.00}{55.8} \\ &= 0.14337 \end{aligned}$$

$$\begin{aligned} \text{No. of moles of S given} &= \frac{8.00}{32.1} \\ &= 0.24922 \end{aligned}$$

also includes unreacted sulfur

Take into consideration ratio

Step 3: Find out which reactant is in excess and which reactant is the limiting reactant

$$\frac{\text{No. of moles of S}}{\text{No. of moles of Fe}} = \frac{0.24922}{0.14337} = 1.7432$$

No. of moles of S **needed** if all the Fe is used up = 1.7432 mol

Since no. of moles of S given > no. of moles of S needed, S is in **excess** and Fe is the **limiting reactant**.

OR

No. of moles of Fe

No. of moles of S

$$= \frac{0.14337}{0.24992} \times \frac{1}{1} = 0.57366$$

No. of moles of Fe **needed** if all the S is used up = 0.24992

Since no. of moles of Fe given < no. of moles of Fe needed,

Fe is the **limiting reactant** and **S** is in **excess**.

Step 4: The **number of moles of limiting reactant** determines the number of moles of product.

$$\frac{\text{No. of moles of FeS}}{\text{No. of moles of Fe}} = \frac{1}{1}$$

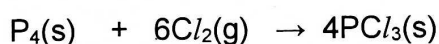
$$\text{No. of moles of FeS formed} = 0.14337$$

Step 5: Convert the number of moles of FeS formed into mass.

$$\begin{aligned} \text{Mass of FeS produced} &= 0.14337 \times (55.8 + 32.1) \\ &= 12.6 \text{ g} \end{aligned}$$

Example 2

A mixture of 125 g of phosphorus and 323 g of chlorine gas are allowed to react to form phosphorus(III) chloride.



Calculate the mass of phosphorus(III) chloride formed.

Solution

$$\text{No. of moles of P}_4 \text{ given} = \frac{125}{31.0 \times 4} = 1.0081 \text{ mol}$$

$$\text{No. of moles of Cl}_2 \text{ given} = \frac{323}{35.5 \times 2} = 4.5493 \text{ mol}$$

$$\frac{\text{No. of moles of P}_4}{\text{No. of moles of Cl}_2} = \frac{1}{6}$$

$$\begin{aligned} \text{No. of moles of P}_4 \text{ needed if all the Cl}_2 \text{ is used up} &= \frac{1}{6} \\ &= \frac{1}{6} \times 4.5493 = 0.75822 \text{ mol} \end{aligned}$$

Since no. of moles of P₄ given is > no. of moles of P₄ needed,
P₄ is in excess and Cl₂ is the limiting reactant.

OR

$$\frac{\text{No. of moles of } \text{Cl}_2}{\text{No. of moles of } \text{P}_4} = \frac{6}{1}$$

$$\text{No. of moles of } \text{Cl}_2 \text{ needed if all the } \text{P}_4 \text{ is used up} = \frac{6}{1} \times 1.0081 = 6.0486$$

Since no. of moles of Cl_2 given 5 no. of moles of Cl_2 needed,
 Cl_2 is the limiting reactant and P_4 is in excess.

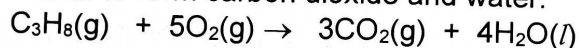
$$\frac{\text{No. of moles of } \text{PCl}_3}{\text{No. of moles of } \text{Cl}_2} = \frac{4}{6}$$

$$\begin{aligned} \text{No. of moles of } \text{PCl}_3 &= \frac{4}{6} \times 4.5493 \\ &= 3.0329 \end{aligned}$$

$$\begin{aligned} \text{Mass of } \text{PCl}_3 &= 3.0329 \times [31.0 + 3(35.5)] \\ &= 3.0329 \times 137.5 \\ &= 417.9 \text{ g (35.5)} \end{aligned}$$

Example 3 [involving gases]

Propane gas, C_3H_8 , burns in air to form carbon dioxide and water.



In an experiment, 10.0 cm^3 of propane was burnt in 70.0 cm^3 of oxygen.

- Which of the two reacting gases were in excess? Calculate the volume of the excess gas remaining at the end of the experiment.
- Calculate the volume of carbon dioxide gas produced.

Solution

(a) From equation,

$$\frac{\text{No. of moles of } \text{O}_2}{\text{No. of moles of } \text{C}_3\text{H}_8} = \frac{5}{1}$$

According to Avogadro's Law, $\frac{\text{volume of } \text{O}_2}{\text{volume of } \text{C}_3\text{H}_8} = \frac{5}{1}$

$$\text{Volume of } \text{O}_2 \text{ needed if all the } \text{C}_3\text{H}_8 \text{ is used up} = 50.0 \text{ cm}^3$$

Since volume of O_2 given 70.0 volume of O_2 needed,
 C_3H_8 is in excess and O_2 is the limiting reactant.

$$\begin{aligned} \text{Volume of excess } \text{O}_2 &= (70.0 + 10.0) - 50.0 \\ &= 30.0 \text{ cm}^3 \end{aligned}$$

$$(b) \frac{\text{number of moles of } \text{O}_2}{\text{number of moles of } \text{C}_3\text{H}_8} = \frac{5}{1}$$

$$\frac{\text{Volume of } \text{O}_2}{\text{volume of } \text{C}_3\text{H}_8} = \frac{5}{1}$$

$$\begin{aligned} \text{Volume of } \text{CO}_2 &= \frac{3}{5} \times 10.0 \\ &= 6.0 \text{ cm}^3 \end{aligned}$$

Quick Check 3

- 1 3.60 g of magnesium was burnt in 2.40 dm³ of oxygen at r.t.p. Calculate the mass of magnesium oxide formed.



From equation,

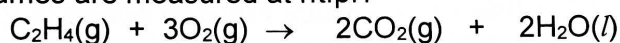
$$\frac{\text{No. of moles of O}_2}{\text{No. of moles of Mg}} = \frac{1}{2}$$

According to Avogadro's Law, $\frac{\text{Volume of O}_2}{\text{Volume of Mg}} = \frac{1}{2}$

$$\text{Volume of Mg} = 2.40 \text{ dm}^3 \times 2$$

$$\begin{aligned} \text{No. of moles of Mg} &= \frac{4.80 \text{ dm}^3}{24} \\ &= 0.200 \text{ mol} \end{aligned}$$

- 2 15.0 cm³ of ethene (C₂H₄) was burnt in 80.0 cm³ of oxygen. What is the volume of the resulting gas mixture if all volumes are measured at r.t.p.?



8.1 Concentration of Solutions

- The concentration of a solution tells us the **amount** of **solute** in a unit volume of a solution. There are two ways of measuring the concentration:

- The **mass (in grams) of solute in 1 dm³ of solution** (g/ dm³)
A concentration of 10.0 g/dm³ means there are **10.0 g** of solute in every **1 dm³** of solution.

$$\text{Concentration in g/dm}^3 = \frac{\text{mass of solute in g}}{\text{volume of solution in dm}^3}$$

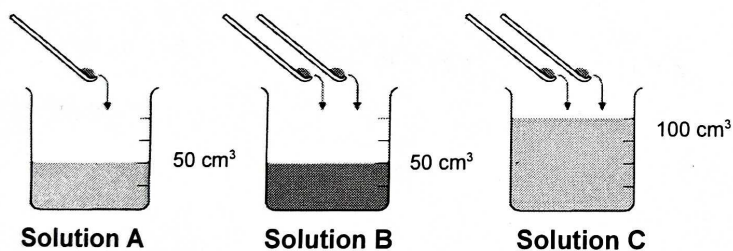
- The **moles of solute in 1 dm³ of solution** (mol/ dm³) is known as the **molar concentration** or **molarity**.
A sodium hydroxide solution with a concentration of 0.500 mol/dm³ has **0.500** moles of NaOH dissolved in every **1 dm³** of solution.

$$\text{Concentration in mol/dm}^3 = \frac{\text{number of moles of solute in mol}}{\text{volume of solution in dm}^3}$$

- A convenient formula involving molar concentration and concentration in g/dm³

$$\text{Concentration in mol/dm}^3 = \frac{\text{concentration in g/dm}^3}{\text{molar mass of solute in g/mol}}$$

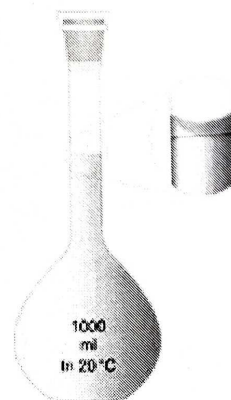
Comparing concentrations



- Solution A and B have the same **volume**, but Solution **B** has **twice** the amount of **solute** as Solution **A** and thus has twice the concentration of Solution **A**.
- Solution B and C have the same amount of **solute**, but Solution **C** has **twice** the volume as Solution **B** and thus has half the concentration of Solution **B**.

Standard Solution

- A **standard solution** is a solution of **known concentration**.
- It is usually made by dissolving a known mass of solute in a known volume of solution in a volumetric flask.



Example 1

A 200 cm³ solution contains 10.0 g of potassium hydroxide, KOH. Calculate the concentration of potassium hydroxide in (a) g/dm³, and (b) mol/dm³.

Solution

$$\begin{aligned}\text{(a) Concentration of KOH solution} &= \frac{\text{mass of solute}}{\text{volume of solution}} \\ &= \frac{10.0}{0.2} \times \frac{1000}{1000} \\ &= 50.0 \text{ g/dm}^3\end{aligned}$$

$$\text{(b) Molar mass of KOH} = 39.1 + 16.0 + 1.0 = 56.1 \text{ g/mol}$$

$$\begin{aligned}\text{Concentration of KOH solution} &= \frac{\text{concentration in g/dm}^3}{\text{molar mass}} \\ &= \frac{50.0}{56.1} \\ &= 0.891 \text{ mol/dm}^3\end{aligned}$$

(c) Alternative answer

$$\begin{aligned}\text{Number of moles of KOH} &= \frac{\text{mass}}{\text{molar mass}} \\ &= \frac{10.0}{39.1 + 16.0 + 1.0} = 0.17825 \text{ mol (5 s.f.)} \\ \text{Concentration of KOH solution} &= \frac{\text{number of moles of solute}}{\text{volume of solution}} \\ &= \frac{0.17825}{0.2} \\ &= 0.891 \text{ mol/dm}^3 \text{ (3 s.f.)}\end{aligned}$$

Example 2

What mass of H₂SO₄ must be dissolved in 250 cm³ of solution to prepare a 0.200 mol/dm³ solution?
↳ 0.25

$$\begin{aligned}\text{No. of moles of H}_2\text{SO}_4 &= \text{concentration (mol/dm}^3\text{)} \times \text{volume} \\ &= 0.200 \times 0.25 \\ &= 0.05 \text{ mol}\end{aligned}$$

$$\begin{aligned}\text{Mass of H}_2\text{SO}_4 &= \text{no. of moles} \times \text{molar mass} \\ &= 0.05 \times [2(1.0) + 32.1 + 4(16.0)] \\ &= 4.905 \text{ g}\end{aligned}$$

Quick check 4

1 Calculate the concentration of the following solutions, in mol/dm³:

- (a) 0.200 mol of potassium hydroxide in 4.00 dm³ of solution.
(b) 0.0100 mol of sulfuric acid in 50.0 cm³ of solution.

$$\begin{aligned}\text{a) Concentration of KOH solution} &= \frac{0.200}{4.00} \\ &= 0.0500 \text{ mol/dm}^3\end{aligned}$$

$$\begin{aligned}\text{b) Concentration of H}_2\text{SO}_4 \text{ solution} &= \left(\frac{0.0100}{50.0} \right) \div 0.05 \\ &= 0.0004 \text{ mol/dm}^3\end{aligned}$$

- 2 Calculate the number of moles of
 (a) NaOH in 25.0 cm³ of 0.400 mol/dm³ NaOH
 (b) NaCl in 500 cm³ of 0.0200 mol/dm³ NaCl
 (c) H₂SO₄ in 2.00 dm³ of 4.90 g/dm³ of H₂SO₄

a) Number of moles of NaOH

$$= \frac{25.0}{1000} \times 0.400$$

$$= 0.0100 \text{ mol}$$

b) Number of moles of NaCl

$$= \frac{500}{1000} \times 0.0200$$

$$= 0.0100 \text{ mol}$$

c) Molar concentration of H₂SO₄

$$= \frac{4.90}{(2 \times 1.0732 + 4 \times 16.0)}$$

$$= 0.049949 \text{ mol/dm}^3$$

\nearrow No. of moles of H₂SO₄
 = concentration \times volume
 = 0.049949 \times 2

- 3 Calculate the mass of = 0.0999 mol

(a) HCl in 200 cm³ of 1.00 mol/dm³ hydrochloric acid.

(b) HNO₃ in 1000 cm³ of 0.100 mol/dm³ nitric acid.

a) Molar mass of HCl = 36.5

g/dm³ of HCl = 36.5 \times 100

$$= 36.5 \text{ g/dm}^3$$

$$200 \text{ cm}^3 = 0.2 \text{ dm}^3$$

$$\text{Mass of HCl} = 36.5 \times 0.2$$

$$= 7.3 \text{ g}$$

b) 1000 cm³ = 1 dm³

Molar mass of HNO₃

$$= 63$$

$$\text{g/dm}^3 \text{ of HNO}_3 = 63 \times 0.100$$

$$= 6.3$$

$$\text{Mass of HNO}_3 = 6.3 \times 1$$

$$= 6.30 \text{ g}$$

- 4 What mass of potassium hydroxide must be dissolved in 100 cm³ of solution to prepare a 0.400 mol/dm³ solution?

$$0.400 \text{ mol/dm}^3$$

$$100 \text{ cm}^3 = 0.1 \text{ dm}^3$$

$$\text{Number of moles of KOH required} = 0.400 \times (0.1)$$

$$= \cancel{0.40} 0.0400 \text{ mol}$$

$$\text{Mass of KOH} = 0.04 \times 56.105$$

$$= 2.2442 \text{ g}$$

$$= 2.24 \text{ g (3 s. f.)}$$

9 Percentage Yield and Percentage Purity

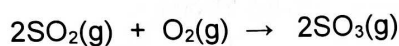
9.1 Percentage Yield

- (d) The amount of product formed in a reaction is known as the yield.
(e) The **theoretical yield** is the amount of product calculated from the equation.
(f) The **experimental yield** is the amount of product that is actually obtained in the experiment.
(g) In any reaction, the experimental yield is almost always **lower** than the theoretical yield.

$$\text{Percentage yield} = \frac{\text{Experimental yield}}{\text{Theoretical yield}} \times 100 \%$$

Example 1

128 g of sulfur dioxide, SO_2 , was reacted with oxygen to produce sulfur trioxide, SO_3 .
The equation for the reaction is:



140 g of SO_3 was produced in the reaction. Calculate the percentage yield of the SO_3 .

Solution

$$\text{No. of moles of } \text{SO}_2 = \frac{128}{32.1 + 2(16.0)} = 1.9969 \text{ (5 s.f.)}$$

$$\text{From the equation, } \frac{\text{no. of moles of } \text{SO}_3}{\text{no. of moles of } \text{SO}_2} = \frac{2}{2} = \frac{1}{1}$$

$$\begin{aligned} \text{No. of moles of } \text{SO}_3 &= 1 \times 1.9969 \\ &= 1.9969 \text{ mol} \end{aligned}$$

$$\begin{aligned} \text{Theoretical mass of } \text{SO}_3 \text{ produced} &= \text{no. of moles} \times \text{molar mass} \\ &= 1.9969 \times (32.1 + 3 \times 16.0) \\ &= 159.95 \text{ g} \end{aligned}$$

$$\begin{aligned} \% \text{ yield of } \text{SO}_3 &= \frac{\text{Experimental yield of } \text{SO}_3}{\text{Theoretical yield of } \text{SO}_3} \times 100 \% \\ &= \frac{140}{159.95} \times 100 \% \\ &= 87.5 \% \end{aligned}$$

9.2 Percentage Purity

- Sometimes, substances are not pure and the percentage purity needs to be calculated.

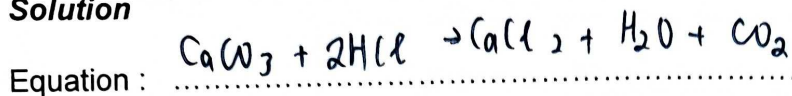
$$\text{Percentage purity} = \frac{\text{mass of pure substance}}{\text{mass of impure sample}} \times 100 \%$$

Example 1

An impure sample of calcium carbonate (CaCO_3) contains calcium sulfate as an impurity. When excess hydrochloric acid was added to 6.00 g of the sample, 1200 cm^3 of gas were produced (measured at r.t.p.).

Calculate the percentage purity of the calcium carbonate sample.

Solution



(Note: Only CaCO_3 will react with hydrochloric acid but not the CaSO_4 impurity)

Question : Why is hydrochloric acid added in excess? To ensure all the CaCO_3 is reacted

$$\text{No. of moles of CO}_2 \text{ produced} = \frac{\text{Volume}}{\text{molar volume}} \\ = \frac{1200}{24000} = 0.0500 \text{ mol}$$

$$\text{From equation, } \frac{\text{no. of moles of CaCO}_3}{\text{no. of moles of CO}_2} = \frac{1}{1}$$

$$\text{no. of moles of CaCO}_3 \text{ reacted} = \frac{1}{1} \times 0.0500 \text{ mol} \\ = 0.0500 \text{ mol}$$

$$\text{Mass of CaCO}_3 \text{ reacted} = \text{no. of moles} \times \text{molar mass} \\ = 0.0500 \times (40.1 + 12.0 + 3 \times 16.0) \\ = 5.005 \text{ g}$$

$$\% \text{ purity of CaCO}_3 \text{ in sample} = \frac{\text{mass of pure CaCO}_3}{\text{mass of impure sample}} \times 100 \% \\ = \frac{5.005}{6.00} \times 100 \% \\ = 83.4 \%$$

Quick Check 5

- 1 In the oxidation of 1 mole of ethanol ($\text{C}_2\text{H}_6\text{O}$), 1 mole of ethanoic acid ($\text{C}_2\text{H}_4\text{O}_2$) is obtained. If 9.20 g of ethanol is used and the mass of ethanoic acid obtained is 9.00 g, calculate the percentage yield of ethanoic acid.

$$\frac{\text{Number of moles of C}_2\text{H}_6\text{O}}{\text{Number of moles of C}_2\text{H}_4\text{O}_2} = \frac{1}{1}$$

$$\text{No. of moles of C}_2\text{H}_4\text{O}_2 \text{ produced} = \frac{\text{mass}}{\text{molar mass}} \\ = \frac{9.00}{2(12.0) + 4(1.0) + 2(16.0)} \\ = 0.1500 \text{ mol}$$

Expected yield of ethanoic acid

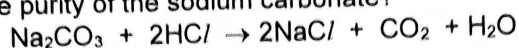
$$= \frac{9.20}{2(12.0) + 6(1.0) + 16.0} \\ = 0.2000 \text{ mol}$$

Chemistry / Stoichiometry & Mole Concept

Percentage yield of ethanoic acid

$$= \frac{0.1500}{0.2000} \times 100 \% \\ = 75 \%$$

- 2 0.500 g of impure sodium carbonate is dissolved in excess dilute hydrochloric acid. The volume of carbon dioxide collected, measured at r.t.p., is found to be 105 cm³. What is the percentage purity of the sodium carbonate?



$$\begin{aligned} \text{No. of moles of CO}_2 \text{ produced} &= \frac{\text{Volume}}{\text{molar volume}} \\ &= \frac{0.105}{24.0} \\ &= 0.004375 \text{ mol (5sf)} \end{aligned}$$

10.1 Volumetric Analysis - Calculations for Titration

Titration is a method of volumetric analysis. It is used to **determine the concentrations of solutions**.

Titration involves measuring volumes of solutions and calculations using

- a solution of **unknown** concentration;
- a solution of **known** concentration.

Refer to Acid, Bases and Salts chapter on salt preparation using titration method.

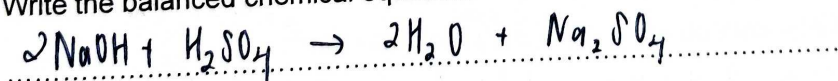
Example 1

30.0 cm³ of 0.100 mol/dm³ sodium hydroxide solution reacted completely with 25.0 cm³ of sulfuric acid in a titration. Calculate the concentration of sulfuric acid in

- mol/dm³,
- g/dm³.

Solution

Step 1: Write the balanced chemical equation.



Step 2: Find the number of moles of NaOH

$$\rightarrow 30.0 \text{ cm}^3 = 0.03$$

No. of moles of NaOH = concentration (mol/dm³) x volume in dm³

$$\begin{aligned} &= 0.100 \times 0.0300 \\ &= 0.00300 \text{ mol} \end{aligned}$$

Step 3: Find the ratio of the number of moles of H_2SO_4 to the number of moles of NaOH .

$$\frac{\text{No. of moles of } \text{H}_2\text{SO}_4}{\text{No. of moles of } \text{NaOH}} = \frac{1}{2}$$

Step 4: Use the ratio to find the number of moles of H_2SO_4 produced.

$$\begin{aligned} \text{No. of moles of } \text{H}_2\text{SO}_4 &= \frac{1}{2} \times \text{no. of moles of } \text{NaOH} \\ &= \frac{1}{2} \times 0.00300 \\ &= 0.00150 \text{ mol} \end{aligned}$$

Step 5: Find the concentration of H_2SO_4 in mol/dm^3 .

$$\begin{aligned} \text{Concentration of } \text{H}_2\text{SO}_4 &= \text{no. of moles of } \text{H}_2\text{SO}_4 \div \text{volume in } \text{dm}^3 \\ &= 0.00150 \div 0.03 \\ &= 0.05 \text{ mol/dm}^3 \end{aligned}$$

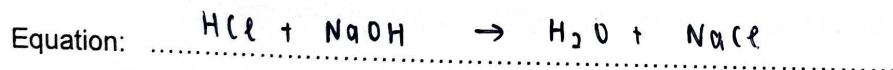
Step 6: Find the concentration of H_2SO_4 in g/dm^3 .

$$\begin{aligned} \text{Concentration of } \text{H}_2\text{SO}_4 (\text{g/dm}^3) &= \text{concentration of } \text{H}_2\text{SO}_4 (\text{mol/dm}^3) \times \text{molar mass} \\ &= 0.05 \text{ mol/dm}^3 \times (2 \times 1.0 + 32.1 + 4 \times 16.0) \\ &= 5.89 \text{ g/dm}^3 \end{aligned}$$

Example 2

In a titration, it was found that 15.0 cm^3 of a solution of hydrochloric acid will exactly neutralise 25.0 cm^3 of a 1.20 g/dm^3 solution of sodium hydroxide. Find the concentration of the hydrochloric acid solution in mol/dm^3 .

Solution



$$\begin{aligned} \text{Concentration of } \text{NaOH} (\text{mol/dm}^3) &= \text{concentration (g/dm}^3) \div \text{molar mass} \\ &= 1.20 \text{ g/dm}^3 \div (23.0 + 16.0 + 1.0) \\ &= 0.0300 \text{ mol/dm}^3 \end{aligned}$$

$$\begin{aligned} \text{No. of moles of } \text{NaOH} &= \text{concentration (mol/dm}^3) \times \text{volume (dm}^3) \\ &= 0.0300 \text{ mol/dm}^3 \times 0.025 \text{ dm}^3 \\ &= 0.00075 \text{ mol} \end{aligned}$$

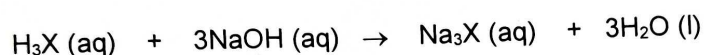
$$\frac{\text{No. of moles of } \text{HCl}}{\text{No. of moles of } \text{NaOH}} = \frac{1}{1}$$

$$\begin{aligned}\text{No. of moles of HCl} &= \text{no. of moles of NaOH} \\ &= 0.00075 \text{ mol}\end{aligned}$$

$$\begin{aligned}\text{Concentration of HCl} &= \text{no. of moles of HCl} \div \text{volume in dm}^3 \\ &= 0.00075 \text{ mol} \div 0.015 \\ &= 0.5 \text{ mol/dm}^3\end{aligned}$$

Example 3

2.80 g of an acid, H_3X , were dissolved in water and made up to 250 cm^3 . A 25.0 cm^3 portion of this solution was neutralised by 28.6 cm^3 of 0.300 mol/dm^3 sodium hydroxide solution according to the equation:



Calculate

- the mass of the acid in 1 dm^3 of solution,
- the number of moles of the acid in 1 dm^3 of solution,
- the relative molecular mass of the acid.

Solution

$$(a) \text{ Mass of acid in } 1 \text{ dm}^3 = \text{mass} \div \text{volume in dm}^3$$

$$= 2.80 \div 0.25$$

$$= 11.2 \text{ g}$$

$$(b) \text{ No. of moles of NaOH} = \text{concentration (mol/dm}^3) \times \text{volume in dm}^3$$

$$= 0.300 \times 0.0286$$

$$= 0.00858 \text{ mol}$$

$$\frac{\text{No. of moles of H}_3\text{X}}{\text{No. of moles of NaOH}} = \frac{1}{3}$$

$$\begin{aligned}\text{No. of moles of H}_3\text{X} &= \frac{1}{3} \times 0.00858 \\ &= 0.00286 \text{ mol}\end{aligned}$$

$$\text{No. of moles of H}_3\text{X in } 1 \text{ dm}^3 = \text{no. of moles} \div \text{volume in dm}^3$$

$$= 0.00286 \div 0.025$$

$$= 0.1144 \text{ mol (4 s.f.)}$$

$$= 0.114 \text{ mol (3 s.f.)}$$

$$(c) \text{ Molar mass of H}_3\text{X} = \text{concentration (g/dm}^3) \div \text{concentration (mol/dm}^3)$$

$$= 11.2 \div 0.1144$$

$$= 97.9 \text{ g/mol}$$

$$\text{Relative molecular mass of H}_3\text{X} = 97.9$$

Example 4

16.0 g of **impure** sodium carbonate are dissolved in 1 dm³ of solution. A 25.0 cm³ portion of this solution required 30.0 cm³ of 0.200 mol/dm³ hydrochloric acid for reaction in a titration. Calculate the percentage purity of the sodium carbonate.

Solution

$$\begin{aligned} \text{No. of moles of HCl} &= \text{concentration (mol/dm}^3) \times \text{volume in dm}^3 = 0.200 \times 0.0300 \\ &= 0.00600 \text{ mol} \end{aligned}$$

$$\frac{\text{No. of moles of Na}_2\text{CO}_3}{\text{No. of moles of HCl}} = \frac{1}{2}$$

$$\begin{aligned} \text{No. of moles of pure Na}_2\text{CO}_3 \text{ in } 25.0 \text{ cm}^3 \text{ of solution} &= \frac{1}{2} \times 0.00600 \\ &= 0.00300 \text{ mol} \end{aligned}$$

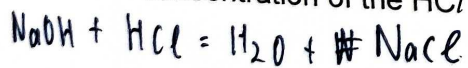
$$\begin{aligned} \text{No. of moles of pure Na}_2\text{CO}_3 \text{ in } 1 \text{ dm}^3 \text{ of solution} &= \frac{\text{no. of moles}}{\text{volume in dm}^3} \\ &= \frac{0.00300}{0.0250} \\ &= 0.120 \text{ mol} \end{aligned}$$

$$\begin{aligned} \text{Mass of pure Na}_2\text{CO}_3 \text{ in } 1 \text{ dm}^3 &= \text{no. of moles in } 1 \text{ dm}^3 \times \text{molar mass} \\ &= 0.120 \times (2 \times 23.0) + (12.0) + (16 \times 3) \\ &= 0.120 \times 106 \\ &= 12.72 \text{ g} \end{aligned}$$

$$\begin{aligned} \% \text{ purity of Na}_2\text{CO}_3 \text{ in sample} &= \frac{\text{mass of pure Na}_2\text{CO}_3}{\text{mass of impure Na}_2\text{CO}_3} \times 100 \% \\ &= \frac{12.72}{16.0} \times 100 \% \\ &= 79.5 \% \end{aligned}$$

Quick Check 6

32.0 cm³ of 0.100 mol/dm³ NaOH reacts with 25.0 cm³ of HCl in a titration. Calculate the concentration of the HCl in (a) mol/dm³, and (b) in g/dm³.



$$\begin{aligned} \text{Number of moles of NaOH} &= 0.032 \times 0.100 \\ &= 0.0032 \text{ mol} \end{aligned}$$

$$\frac{\text{No. of moles of HCl}}{\text{No. of moles of NaOH}} = \frac{1}{1}$$

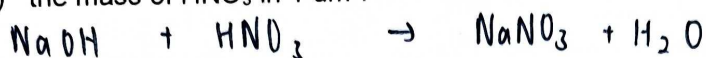
$$\therefore \text{No. of moles of HCl} = 0.0032 \text{ mol}$$

$$\begin{aligned} \text{a) Concentration of HCl in mol/dm}^3 &= 0.0032 \div \left(\frac{25.0}{1000} \right) \\ &= 0.128 \text{ mol/dm}^3 \end{aligned}$$

$$\text{b) Concentration of HCl in } \frac{\text{mass}}{\text{g/dm}^3}$$

$$\begin{aligned} &= 0.128 \times (1.0 + 35.5) \\ &= 4.672 \text{ g/dm}^3 \end{aligned}$$

- 2 A solution of NaOH contains 6.00 g/dm^3 of NaOH. 20.0 cm^3 of the NaOH reacts completely with 40.0 cm^3 of HNO_3 . Calculate
- the concentration of NaOH in mol/dm^3 .
 - the number of moles of HNO_3 in 1 dm^3 .
 - the mass of HNO_3 in 1 dm^3 .



$$\begin{aligned}\text{Mass of NaOH} &= \frac{20.0}{1000} \times 6.00 \text{ g/dm}^3 \\ &= 0.12 \text{ g}\end{aligned}$$

0.12g

- 3 7.40 g of a sample of impure potassium carbonate was dissolved in water and made up to 1 dm^3 . 20.0 cm^3 of this solution required 19.80 cm^3 of 0.0500 mol/dm^3 sulfuric acid for neutralisation. What is the percentage purity of the potassium carbonate?



- 4 In a titration experiment, 22.5 cm^3 of 7.00 g/dm^3 nitric acid neutralised 20.0 cm^3 of an alkali, XOH , containing 5.00 g of alkali per dm^3 . Calculate the relative atomic mass of X.

ANSWERS TO QUICK CHECK

Quick Check 1 (pg 21 - 22)		Quick Check 4 (pg 30 - 31)	
1(a)	6.36 g	1(a)	0.0500 mol/dm ³
1(b)	1.20 dm ³	1(b)	0.200 mol/dm ³
2(a)	2Mg + CO ₂ → 2MgO + C	2(a)	0.0100 mol
2(b)(i)	0.593 dm ³	2(b)	0.0100 mol
2(b)(ii)	1.99 g	2(c)	0.0999 mol
3	40.9 g	3(a)	7.30 g
Quick Check 2 (pg 24)		3(b)	6.30 g
1(a)	20.0 cm ³	4	2.24 g
1(b)	60.0 cm ³	Quick Check 5 (pg 33 - 34)	
2(a)	500 cm ³	1	75.0 %
2(b)	680 cm ³	2	92.8 %
Quick Check 3 (pg 28)		Quick Check 6 (pg 37 - 38)	
1	5.97 g	1(a)	0.128 mol/dm ³
2	65.0 cm ³	1(b)	4.67 g/dm ³
		2(a)	0.150 mol/dm ³
		2(b)	0.0750 mol
		2(c)	4.73g
		3	92.4 %
		4	23.0

Mole Concept Summary Exercise

