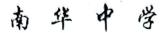
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NAN HUA HIGH SCHOOL

PRELIMINARY EXAMINATION 2022

Subject

Mathematics

Paper

4048/01

Level

Secondary Four Express

Date

17 August 2022

Duration

2 hours

READ THESE INSTRUCTIONS FIRST

Write your name, class and index number on all the work you hand in.

Write in dark blue or black pen.

You may use a HB pencil for any diagrams or graphs.

Do not use staples, paper clips, glue, correction fluid or correction tape.

Answer all questions.

If working is needed for any question it must be shown with the answer.

Omission of essential working will result in loss of marks.

The use of an approved scientific calculator is expected, where appropriate.

If the degree of accuracy is not specified in the question, and if the answer is not exact, give the answer to three significant figures. Give answers in degrees to one decimal place.

For π , use either your calculator value or 3.142, unless the question requires the answer in terms of π .

The number of marks is given in brackets [] at the end of each question or part question. The total of the marks for this paper is 80.

For Examiner's Use					

This paper consists of 23 printed pages.

Page 1 of 23

PartnerInLearning 314 Compound interest

Total amount =
$$P\left(1 + \frac{r}{100}\right)^n$$

Mensuration

Curved surface area of a cone = πrl

Surface area of a sphere = $4\pi r^2$

Volume of a cone =
$$\frac{1}{3} \pi r^2 h$$

Volume of a sphere =
$$\frac{4}{3} \pi r^3$$

Area of triangle
$$ABC = \frac{1}{2}ab\sin C$$

Arc length = $r\theta$, where θ is in radians

Sector area =
$$\frac{1}{2}r^2\theta$$
, where θ is in radians

Trigonometry

$$\frac{a}{\sin A} = \frac{b}{\sin B} = \frac{c}{\sin C}$$

$$a^2 = b^2 + c^2 - 2bc \cos A$$

Statistics

$$Mean = \frac{\sum fx}{\sum f}$$

Standard deviation =
$$\sqrt{\frac{\sum fx^2}{\sum f} - \left(\frac{\sum fx}{\sum f}\right)^2}$$

Answer all questions.

1	Wri	The number of people living in a town is given as 60 000, correct to 2 significant figures. Write down values for the smallest and largest possible number of people who could be in the town.					
	low	uniter and the second of the s					
		·= · · · · · · · · · · · · · · · · · ·					
		Answer smallest possible number = [1]					
		largest possible number =[1]					
2	(a)	Use prime factors to explain why 135×200 is a perfect cube.					
		entifier in arth madic, the entrance					
		Answer and the state of the sta					
		Side Bigle of the second					
		Land All of the Committee					
		[2]					
	(b)	The lowest common multiple of x and 135 is $2 \times 3^4 \times 5 \times 7$. Find the smallest possible value of x.					
		Answer $x =$					

3 Write the following numbers in order of size, starting with the smallest.

$$\left(\frac{3}{10}\right)^2$$
, $-\frac{21}{90}$, 90%, -0.23 , $\sqrt{0.3}$

Answer[2]

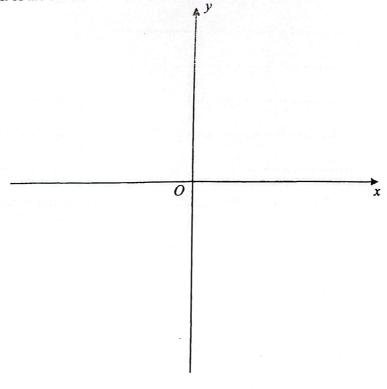
4 Factorise $\frac{6a-15a^2+20ab-8b}{25a^3-4a}$ completely.

[3]

5 Rearrange the formula $\frac{1}{a} - \frac{1}{2b} = \frac{1}{3c}$ to make b the subject.

Answer
$$b = \dots$$
 [2]

Sketch the graph of y = (3-x)(x+2) on the axes below. Indicate clearly the coordinates of the points where the graph crosses the axes and the turning point of the curve.



[2]

7	The	scale of a map is 8 cm: 2 km.			
	(a)	Write this scale in the form $1:n$.		ja ja syntresytt kysist – je je 💯	
		¥ in		, s , , , , , , , , , , , , , , , , , ,	r11
	(b)		Answer	1:	[1]
	(0)	The actual area of a lake is 90 000 m ² . Calculate the area, in square centimetres,	of the lake	on the map.	
		The inferigence gauge to be superior to the garden			
				am²	[2]
			Answer	cm ²	[2]
8	The	is the mean of 5 positive numbers a , b , c , a sum of their squares is 360. Each of the null the new standard deviation.	<i>l</i> and <i>e</i> . umbers is no	ow multiplied by 2.	
	Tine	the new standard deviation.			
		•			
,					
				•	
			Answer		[3]
			22151101		243
Jan. 136.	The state			Page 6 of 23	_

9	One solution of the equation	(k+1)	$)x^{2} +$	kx = 1	5 is	x = -3	}
---	------------------------------	-------	------------	--------	------	--------	---

(a) Find the value of k.

Answer $k = \dots$ [1]

(b) Find the second possible value of x.

Answer $x = \dots$ [1]

10 The cash price of a washing machine is \$840.

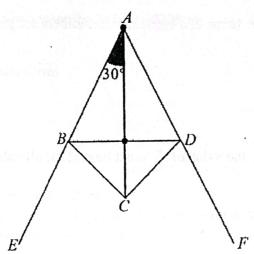
If paid by hire purchase scheme, the deposit is 15% of the cash price and the subsequent 24 equal monthly payments is \$33.50.

Calculate the interest rate per annum.

Answer% [3

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11



The diagram above shows a kite ABCD where angle $BAC = 30^{\circ}$. EB, BD and DF are three sides of a regular polygon. ABE and ADF are straight lines. The ratio of angle CBE to angle CBD is 3: 2.

(a) Calculate the number of sides of the polygon.

Answer[2]

(b) Find angle BCD.

Answer[2]

Page 8 of 23

12	(a)	The first four	terms in a sequence of numbers	are given	below
----	-----	----------------	--------------------------------	-----------	-------

$$T_1 = 2^2 + 7$$

$$T_2 = 3^2 + 12$$

$$T_3 = 4^2 + 17$$

$$T_4 = 5^2 + 22$$

Explain why the value of T_n must be odd for all values of n.

Answer			
F-920			
۷		•••••	
	•••••		[2]

(b) The product of the first n terms of a sequence is given by $2n^2 + 3n$. Find the 12^{th} term of this sequence.

Answer	 [2]

13	The th	nickness of a layer of ice in a water body is 0.00205 m.
	(a)	Write 0.00205 in standard form.
-		
		Answer[1]
	(b)	The ice covers an area of 1.60×10^5 m ² . Assuming that all the ice melts and ignoring the expansion of volume when water freezes, calculate the volume of water, in litres.
		in the second se
		Answer l [2]
	(c)	A thunderstorm occurs and rainwater is falling at an average rate of 5×10^{-1} litres per second over the water body.
		Calculate the percentage increase in the volume of water in the water body after two hours.
	•	

Answer [2]

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- 14 Given that the coordinates of A is (2,-3), $\overrightarrow{AB} = \begin{pmatrix} -5 \\ 7 \end{pmatrix}$ and $\overrightarrow{FE} = k \begin{pmatrix} 2.5 \\ -3.5 \end{pmatrix}$.
 - (a) Find the value of k if ABFE is a parallelogram.

Answer[1]

(b) Find the coordinates of B.

Answer[1]

(c) C is the point (6,-10). Justify if A, B and C are collinear.

Answer [2]

15 A tour agency records the total number of people buying tour packages to Thailand and Vietnam in the months of November and December.

In November, 144 people bought the Thailand tour package and 100 people bought the Vietnam tour package.

In December, 208 people bought the Thailand tour package and 180 people bought the Vietnam tour package.

Thailand Vietnam

This information can be represented by the matrix,
$$\mathbf{M} = \begin{pmatrix} 144 & 100 \\ 208 & 180 \end{pmatrix}$$

November December

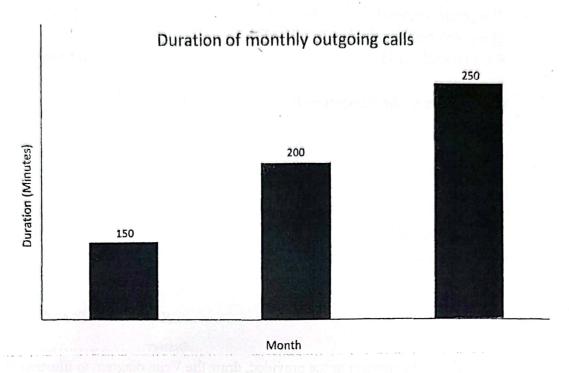
(a) The price of the Thailand and Vietnam package is \$890 and \$750 respectively. Represent the price of the tour package by a 2×1 column matrix K.

Answer
$$\mathbf{K} = \begin{bmatrix} 1 \end{bmatrix}$$

(b) Evaluate the matrix R = MK.

(c)	State what the elements of R represent.
	da faggi kin og ar made skrift har prægen skriptgare i skript af til strette et skript
	Answer
(d)	Evaluate $\frac{1}{2}(1 \ 1) \mathbf{R}$ and explain what the answer represents.
	Trainer enstance for
	Answer
	All Wei
	•••••••••••••••••••••••••••••••••••••••
	[2]

Peter draws this graph to show the duration of his monthly outgoing calls (in minutes) for the last three months.



State one aspect of the graph that may be misleading and explain how this may lead to a misinterpretation of the graph.

Answer			
	• • • • • • • • • • • • • • • • • • • •		
		••••	
			[2]

17 $\xi = \{ \text{integer } x : 0 < x \le 20 \}$

 $P = \{ perfect square \}$

 $Q = \{ \text{even number which solves } 3x > 11 \}$

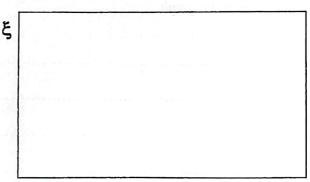
 $R = \{ \text{ multiple of 4} \}$

(a) (i) List all the elements in P.

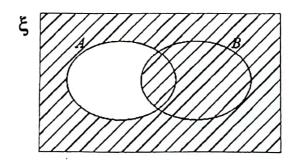
Answer	 [1]

(ii) Find $n(P' \cap Q)$.

(iii) On the answer space provided, draw the Venn diagram to illustrate the relationship between sets P, Q and R. [2]



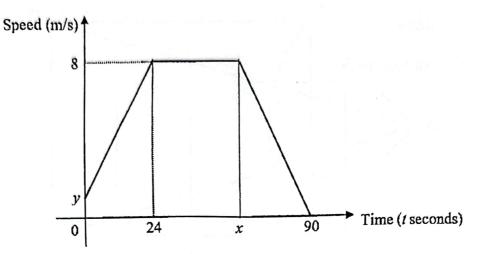
(b) Use set notation to describe the set shaded in the Venn diagram below.



Answer[1	4nswer	[1]
----------	--------	-----

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The diagram shows the speed-time graph for a cyclist's journey for a period of 90 seconds.
 The cyclist accelerates at 0.25 m/s² in the first 24 seconds.
 He then travels at a constant speed of 8 m/s for a distance of 288 m.



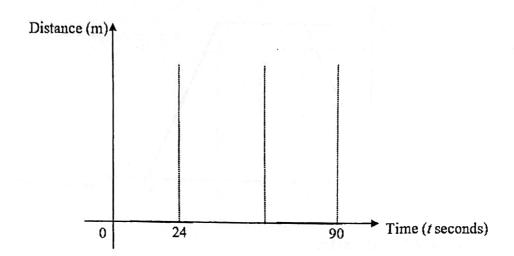
(a) Find the values of x and y.

Answer
$$x = \dots$$
 [2]

(b) On the grid provided, complete the distance-time graph of the journey from t = 0 to t = 90 seconds.

Answer

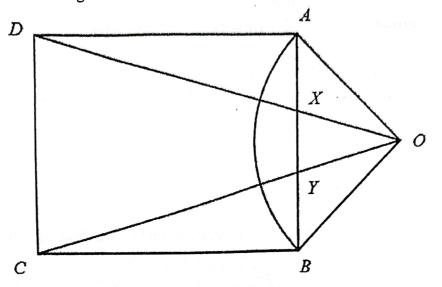
[3]



19 In the diagram, ABCD is a rectangle.

OAB is a sector of a circle, centre O.

OXD and OYC are straight lines.



(a) Show that triangle *OAD* is congruent to triangle *OBC*. Give a reason for each statement you make.

[3]

Answer

(b) Show that triangle OXY is similar to triangle ODC. Give a reason for each statement you make.

[2]

Answer

(c) The area of triangle *ODC* is 36 times that of the area of triangle *OXY*. Find the ratio of the area of quadrilateral *DCYX* to area of triangle *OAB*.

Answer

[1]

Page 19 of 23

The ages of 18 swimmers and 11 cyclists in a sports carnival race were recorded. The results are shown in the stem-and-leaf diagram.

				Swimmers				Cyc	clists				
41	4	3	2 9	1 x 9	1 5 4 8	0 5 1 8	2 2 3 3 4		1 7 9	2	2	3	3
					3	4	1 4	1 0					

Key (Swimmers)
1 | 2 means 21 years old

Key (cyclists)
2 | 3 means 23 years old

(a) Given that the median age of the swimmers is 26 years old, find the value of x.

 $inswer \quad x = \dots$ [1]

(b) Find the interquartile range of the cyclists' age.

swer[2]

Take two comments comparing the ages of the swimmers and the cyclists.	
nswer	

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ar not all land. This waxey at a supposition with the en-	
•••••••••••••••••••••••••••••••••••••••	
	[2]

[2]

The plan of a triangular-shaped garden, PQR, is such that QR = 9.5cm and ∠PQR = 30°. PQ has been drawn for you.

(a) Construct triangle PQR in the space provided.
(b) (i) Construct the perpendicular bisector of R and P.
(ii) Construct the bisector of angle QPR.
(c) A bench S needs to be built inside the garden such that it is nearer to PR than to PQ

and $SR \ge 3$ cm. Shade the region where S could be possibly built.

P Q

Adam invested \$P in a savings account X with interest compounded quarterly at the rate of 1.5% per annum.

Ben invested P in a savings account Y, paying simple interest at the rate of x% per year.

At the end of 5 years, Ben made 10% more than Adam.

Mary would like to invest \$P for 20 years.

She believes that savings account Y is better as Ben made more money than Adam.

Justify with clear mathematical working, whether Mary is correct.

[4]

– End of Paper –

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