Name:	Class:	Class Register Number:

中正中学

CHUNG CHENG HIGH SCHOOL (MAIN)

PRELIMINARY EXAMINATION 2024
SECONDARY 4

MATHEMATICS 4052/02

Paper 2 **Tuesday 20 August 2024**

2 hours 15 minutes

Candidates answer on the Question Paper

READ THESE INSTRUCTIONS FIRST

Write your name, class and index number in the spaces at the top of this page.
Write in dark blue or black pen.
You may use an HB pencil for any diagrams or graphs.
Do not use paper clips, glue or correction fluid.

Answer **all** questions.
The number of marks is given in brackets [ ] at the end of each question or part question.

If working is needed for any question it must be shown with the answer. Omission of essential working will result in loss of marks. The total number of marks for this paper is 90.

The use of an approved scientific calculator is expected, where appropriate. If the degree of accuracy is not specified in the question, and if the answer is not exact, give the answer to three significant figures. Give answers in degrees to one decimal place.
For π, use either your calculator value or 3.142.

For Examiner's Use	
Question Number	Marks Obtained
1	
2	
3	
4	
5	
6	
7	
8	
9	
Total Marks	

This document consists of **23** printed pages and **1** blank page.

Mathematical Formulae

Compound interest

$$\text{Total amount} = P\left(1+\frac{r}{100}\right)^n$$

Mensuration

$$\text{Curved surface area of a cone} = \pi r l$$

$$\text{Surface area of a sphere} = 4\pi r^2$$

$$\text{Volume of a cone} = \frac{1}{3}\pi r^2 h$$

$$\text{Volume of a sphere} = \frac{4}{3}\pi r^3$$

$$\text{Area of triangle } ABC = \frac{1}{2}ab\sin C$$

$$\text{Arc length} = r\theta \text{, where } \theta \text{ is in radian}$$

$$\text{Sector area} = \frac{1}{2}r^2\theta \text{, where } \theta \text{ is in radian}$$

Trigonometry

$$\frac{a}{\sin A} = \frac{b}{\sin B} = \frac{c}{\sin C}$$

$$a^2 = b^2 + c^2 - 2bc\cos A$$

Statistics

$$\text{Mean} = \frac{\Sigma fx}{\Sigma f}$$

$$\text{Standard deviation} = \sqrt{\frac{\Sigma fx^2}{\Sigma f} - \left(\frac{\Sigma fx}{\Sigma f}\right)^2}$$

TURN OVER FOR QUESTION 1

1 **(a)** The table shows the total electricity consumption in Singapore over three years.

Year	2020	2021	2022
Total Electricity Consumption in Gigawatt Hours (GWh)	50 779	53 483	54 884

(i) In 2021, the electricity consumed by households took up 15.5% of the total electricity consumption. Calculate the amount of electricity consumed by households in 2021, correct to two significant figures.

Answer …… GWh [1]

(ii) Calculate the percentage increase in the total electricity consumption from 2020 to 2022.

Answer ……% [2]

(iii) Express the 2020 electricity consumption in kilowatt hours (kWh), leaving your answer in standard form, correct to two significant figures.

Answer …… kWh [1]

(b) A microprocessor is in the shape of a cube where the sides are 5 mm in length.

(i) Find the maximum number of microprocessors that can be placed into a container with dimensions 10 cm by 2 cm by 8 cm.

Answer …… [2]

(ii) A model of the microprocessor was made to a scale of 10 : 1. Given that the surface area of microprocessor is 150 mm^2, find the surface area of the model microprocessor in square centimetres.

Answer …… cm^2 [2]

2 **(a)** Solve $2x-7=3(1-3x)$.

Answer $x =$ ..... [2]

(b) Solve the inequalities $7x-1<13$ and $\frac{x+1}{2} \geq -2(x-2)$.

Answer ..... [3]

(c) Rearrange the formula $y=\frac{x^2+5}{7x^2}$ to make x the subject.

Answer $x =$ ..... [3]

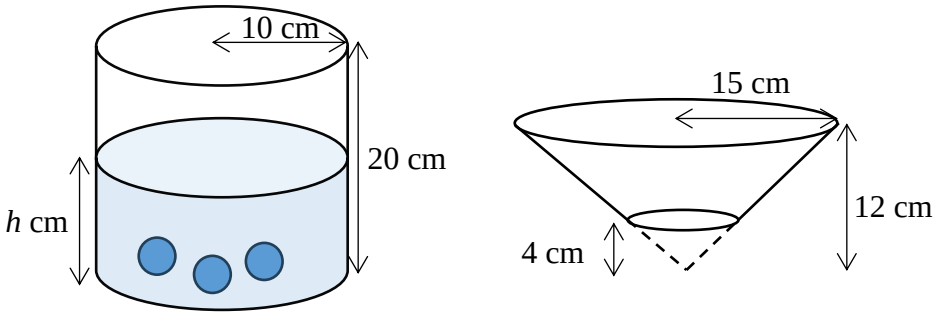
(d) Solve the equation $\frac{2x}{1-x} - 3 = \frac{1}{2x-3}$.

Give your solutions correct to two decimal places.

Answer x = ……. or ……. [5]

3 The diagram shows two open containers, a right cylinder and an inverted frustum. The right cylinder has a base radius of 10 cm and a height of 20 cm. The frustum is formed by cutting a smaller cone off the bottom of a larger cone. The smaller cone that was cut off has a height of 4 cm. The larger cone has a base radius of 15 cm and a height of 12 cm.

Three identical spherical marbles, each of radius 3 cm, are placed into the cylindrical container and water is poured in to a depth of h cm.



(a) Find the volume of each marble, leaving your answer in terms of π.

Answer …… cm^3 [1]

(b) Find the volume of the frustum, leaving your answer in terms of π.

Answer …… cm^3 [3]

(c) All the water from the cylinder, without the marbles, is then poured into the empty frustum, filling it completely without any overflow.

Find the value of h, correct to two decimal places.

Answer h = …… [3]

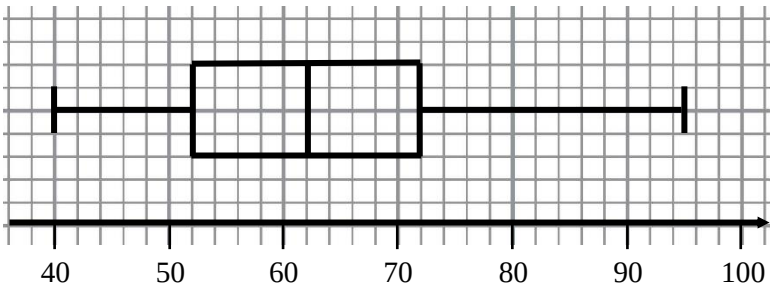
(d) The exterior surface area of each container is painted.
Find the total area painted.

Answer …… cm^2 [6]

4 **(a)** 12 students from class *A* took a Mathematics test.
The table below shows the test marks of the students. However, **two** of the students' marks are covered with ink.

40	95	84	47	63
52	63	55	52	61

(i) Given that the box-and-whisker plot below shows the distribution of the results, explain why the information may not be sufficient to find the missing marks of the two students.



Mathematics Test Marks

Answer

……

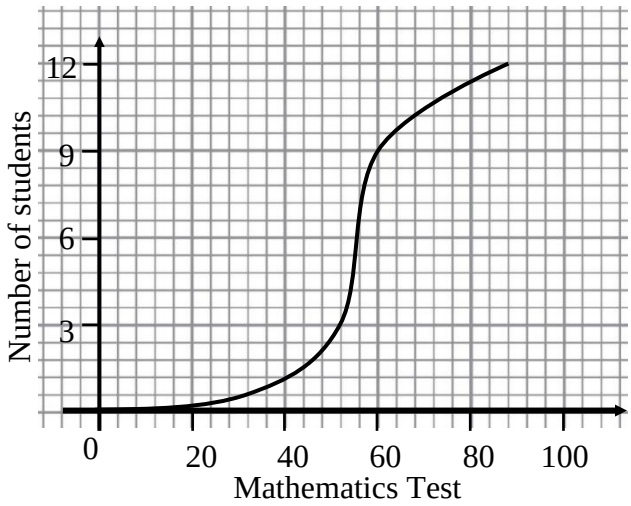
……

…… [1]

(ii) Given further that the modal mark is 63, find the two missing marks.

Answer …… and …… [2]

(iii) 12 students from class *B* also took the same Mathematics test. The distribution of their test marks is shown on the cumulative frequency graph.



Make a comment comparing the averages and a comment comparing the distribution of the Mathematics Test marks between the two classes.
Use figures to support your answers.

Answer

……

……

……

…… [3]

(b) Alice rolled a six-sided die, *X*, 100 times. Bala rolled another six-sided die, *Y*, 80 times. The number of times they each obtained a '6' is recorded in the table.

Die	Number of rolls	Number of times '6' is obtained
X	100	16
Y	80	18

(i) Find the probability of rolling a '6' by Alice and Bala respectively.

Answer P(obtaining a '6' by Alice) = ……... [1]

P(obtaining a '6' by Bala) = ……... [1]

(ii) One of the dice is biased. Using your answers in **(b)(i)**, determine which die, *X* or *Y*, is likely to be the unbiased 6-sided die. Explain your answer.
Answer

……

…… [1]

5 **(a)** Complete the table of values for $y = \frac{2}{x^2} - 2x$.

Values are given to one decimal place where appropriate.

x	−3	−2	−1	−0.5	−0.4	0.5	1	2	3
y		4.5	4	9	13.3	7	0	−3.5	−5.8

[1]

(b) On the grid opposite, draw the graph of $y = \frac{2}{x^2} - 2x$ for $-3 \le x \le 3$. [3]

(c) **(i)** On the same grid, draw the graph of $y + x = 6$ for $-3 \le x \le 3$.

[1]

(ii) Write down the x-coordinates of the points where the line intersects the curve.

Answer $x =$ …… and …… [2]

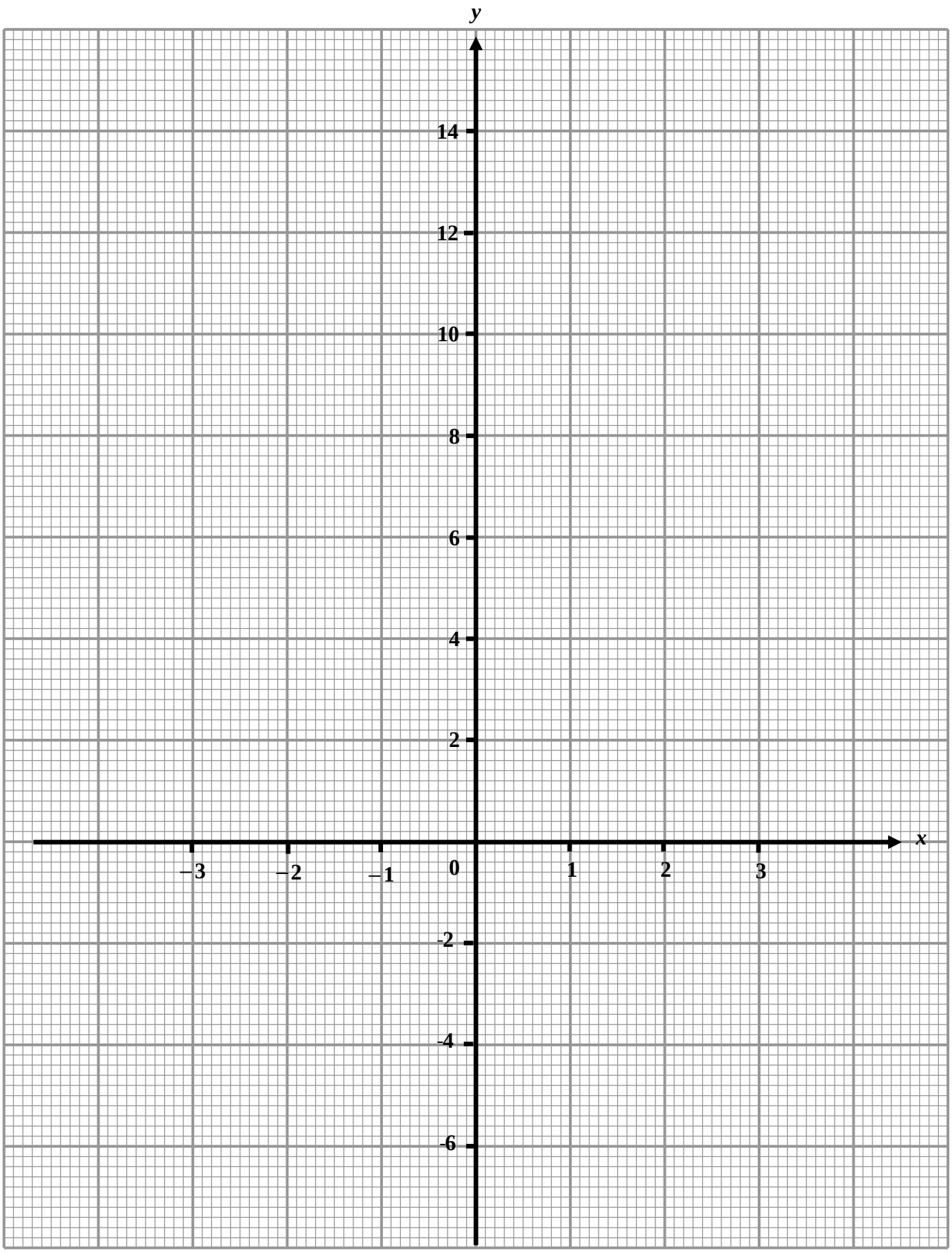
(iii) These values of x are solutions of the equation $x^3 + Ax^2 + B = 0$.

Find the value of A and of B.

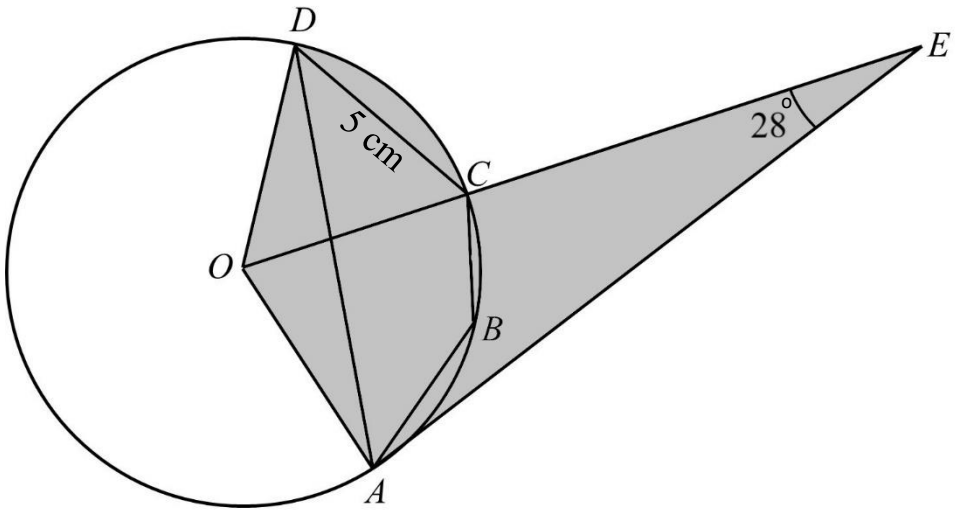
Answer $A =$ ……

$B =$ ……

[3]


y
14
12
10
8
6
4
2
x
−3
−2
−1
0
1
2
3
-2
-4
-6

6



A, *B*, *C* and *D* are points on the circle with centre *O* and radius 5 cm.
AE is a tangent to the circle at *A* and *OE* is a straight line that passes through *C*.
Angle *OEA* = 28° and *CD* = 5 cm.

(a) Find, giving a reason for each step of your working,

(i) angle *OAD*,

Answer Angle *OAD* = ……° [3]

(ii) angle *ABC*.

Answer Angle *ABC* = ……° [2]

(b) Find the area of the shaded region.

Answer …… cm^2 [4]

7 **(a)** *A*, *B*, *C* and *D* are four points such that the coordinates of *A* and *C* are $(4,2)$ and $(10,-34)$ respectively. $\overrightarrow{AB}=\begin{pmatrix}-9\\-12\end{pmatrix}$ and $\overrightarrow{AD}=\begin{pmatrix}24\\-12\end{pmatrix}$.

(i) Find the coordinates of *B*.

Answer (…… , ……) [1]

(ii) Find $\left|\overrightarrow{AB}\right|$.

Answer $\left|\overrightarrow{AB}\right|$ = …… units [1]

It is given that *E* is a point on *BD* such that $\overrightarrow{BE}=\frac{1}{3}\overrightarrow{BD}$.

(iii) Show that *A*, *C* and *E* are collinear.
Answer

[4]

(b) A is the point $(2,6)$, B is the point $(-4,-2)$ and C is the point $(6,-2)$. A line L passes through point C and is parallel to AB.

(i) Find the equation of line L.

Answer …… [2]

Point D lies on line L such that $AD // BC$.

(ii) Find the coordinates of point D.

Answer D (…… , ……) [2]

(iii) Show that $ABCD$ is a rhombus.

Answer

[2]

8 **(a)** The figure shows the first three figures of a sequence formed by sticks of the same size.

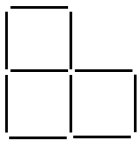


Figure 1

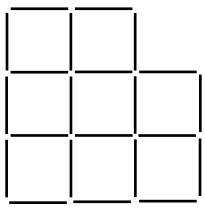


Figure 2

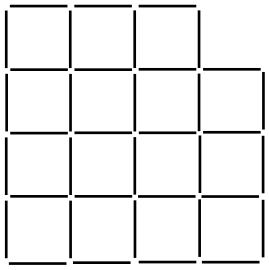


Figure 3

The number of small squares formed in each of the figures is recorded in the table.

Figure Number	Number of Squares
1	$(1+1)^2-1$
2	$(2+1)^2-1$
3	$(3+1)^2-1$

(i) Find the number of small squares formed in Figure 5.

Answer …… [1]

(ii) Find, in terms of n, an expression for the number of squares in Figure n.

Answer …… [1]

(iii) Explain why the sum of the number of squares in two consecutive figures is always odd.

Answer

……

…… [2]

(b) The table below shows the n^{th} terms of 4 sequences.

Sequence number	n^{th} term
1	$4n+3$
2	$7n+1$
3	$14n$
4	$8n-1$

For each sequence, are the numbers in the sequence always multiples of 7, sometimes multiples of 7 or never multiples of 7?

Write down the letter 'A', 'S' or 'N' to represent your answer.

A Always multiples of 7

S Sometimes multiples of 7

N Never multiples of 7

Answer

Sequence 1 ……

Sequence 2 ……

Sequence 3 ……

Sequence 4 …… [2]

9 Sam is a 40-year-old man who earns a gross salary of $8000 a month. He is a Singaporean and an employee of a Singapore firm. Sam is required to put a certain percentage of his monthly gross salary into his Central Provident Fund (CPF) account.

CPF is a mandatory (social security) savings scheme funded by contributions from employers and employees. The table below shows the CPF contribution rates by employers and employees.

Employee's age (Years)	**CPF Contribution Rates from 1 January 2024 (Monthly gross salary > $750)**		
	Total (% of gross salary)	**By Employer (% of gross salary)**	**By Employee (% of gross salary)**
55 and below	37	17	20
Above 55 to 60	31	15	16
Above 60 to 65	22	11.5	10.5
Above 65 to 70	16.5	9	7.5
Above 70	12.5	7.5	5

(a) Find the amount of money Sam's employer must contribute to his CPF monthly.

Answer $…… [1]

Sam wants to plan his monthly savings and has tabulated his monthly expenditure as shown in the table. He hopes to save at least 20% of his salary each month after CPF deductions.

Expenditure	**Amount ($)**
Food and Groceries	820
Transportation	90
Insurance and Healthcare	1000
Phone and Internet Subscriptions	80
Utilities	300
Housing Loan	1000
Leisure and Entertainment (movies, sports, books subscription fees, dining etc)	1580

(b) Determine whether Sam is able to achieve his saving goals by clearly showing your calculations.

……

…… [4]

(c) After a year of saving, Sam decides to invest $15 000 of his savings for a period of 5 years. He comes up with 2 investment plans.

Plan A

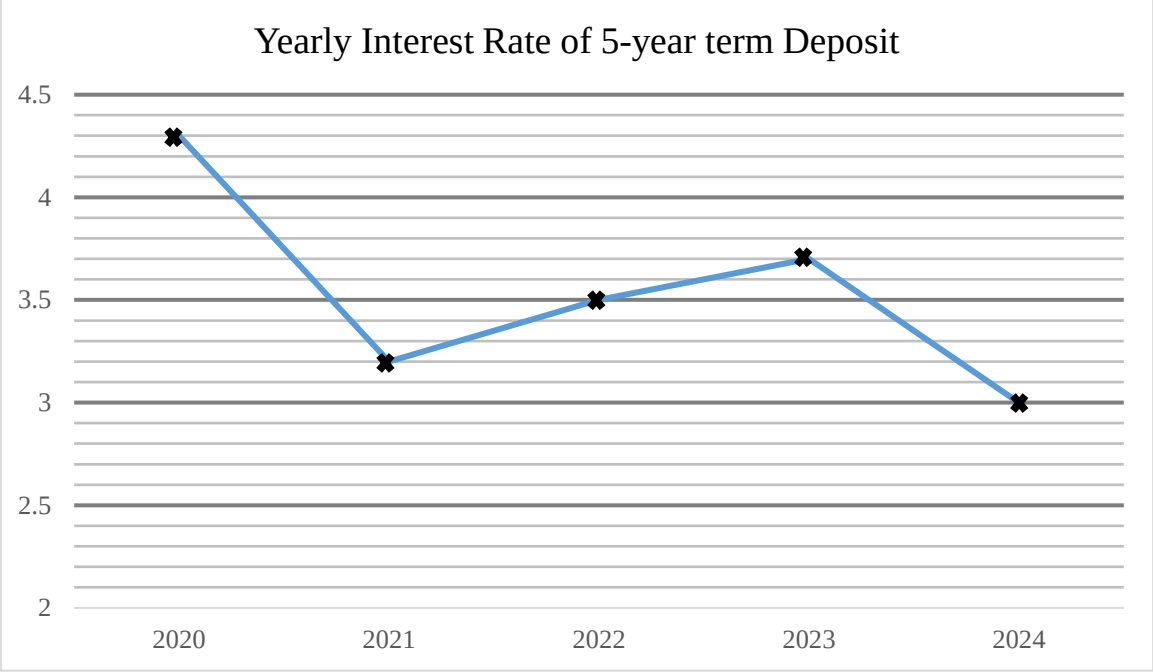
Sam can invest his money in a 5-year savings bond at the beginning of 2025. The interest rate for the 5-year term is shown in the table. The savings bond compounds annually.

Year from issue date	1	2	3	4	5
Interest per year %	3.19	3.19	3.20	3.28	3.31

Plan B

Sam can invest his money at the beginning of 2025 into an insurance company's fixed deposit account for a period of 5 years, compounded yearly. The interest rate is fixed over the duration of the investment and is determined by the year of issuance.
For example: If Sam had invested his money in 2020, over a period of 5 years, his investment plan would be at an interest of 4.3% compounded yearly over the period of 5 years.

However, the interest rate for 2025 is not yet available. Sam finds the information about the interest rates offered by the insurance company for the last 5 years.



Determine which plan Sam should choose.

Justify the decision you make and show your calculations clearly.

……

……[5]

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