

2023 4N Prelim P1 MS

1	$\frac{3}{11}$ $\sqrt[3]{0.02}$ 0.25 $0.\dot{2}$	B2 Deduct 1 mark for each error
2a	$2 : 5$	B1
2b	$\frac{1200}{150} \times 100\%$ $= 800\%$	M1 A1
3	$-2x < -8$ $x > 4$ Smallest prime = 5	M1 A1
4	$P = \frac{k}{x^2}$ $20 = \frac{k}{(2.5)^2}$ $k = 125$ $P = \frac{125}{5^2}$ $= 5$	M1 A1
5a	Acute $x = \sin^{-1}(0.7) = 44.4$ Obtuse $x = 180 - 44.4 = 135.6^\circ$	B1
5b	$y = 180 - 123 = 57^\circ$	B1
6a	$m = 4(-5)^2 - 5$ $= 95$	B1
6b	$m = 4a^2 - 5$ $m + 5 = 4a^2$ $\frac{m+5}{4} = a^2$ $\pm \sqrt{\frac{m+5}{4}} = a$ $a = \pm \sqrt{\frac{m+5}{4}}$	M1 (isolate a^2) A1

7a	$x = 180 - 140 = 40$ They are interior angles between 2 parallel lines	B1 (mention interior and parallel)
7b	Angle a = 62 (base angles of isos tri) $Y = 180 - 62$ (interior angles, // lines) = 118	M1 A1 Deduct 1 mark if missing/ no reason
8	The trend may not be decreasing There are missing data for the months of March to June and August.	B2
9	$\frac{PQ}{7.5} = \frac{2x}{1.5x}$ $\frac{PQ}{7.5} = \frac{4}{3}$ PQ = 10 cm	M1 (or find scale factor = 4/3) A1
10	$x = 2(x + 3)$ $x = 2x + 6$ $-6 = x$ $x = -6$	M1 (expand) A1
11	$1592.19 = 1500(1 + \frac{r}{100})^5$ $1.06146 = (1 + \frac{r}{100})^5$ $1.06146^{\frac{1}{5}} = 1 + \frac{r}{100}$ $1.06146^{\frac{1}{5}} - 1 = \frac{r}{100}$ R = 1.20% (3sf)	M1 M1 (remove power 5) or attempt to solve A1
12ai	$405 = 3^4 \times 5$	B1
12aii	$HCF = 3^2 \times 5 = 45$	B1
12b	$Q^3 = (2^3 \times 5^{6n})^2$ $Q^3 = 2^6 \times 5^{12n}$ $Q = 2^2 \times 5^{4n}$	M1 A1
13	Remainder = 11/20 Food and shopping = 60% of (11/20) * 100% = 33%	M1 (find remainder) M1 (or find 40%) A1

14a	See BUY rate as bank is buying CAD 1 CAD = 1.0028 SGD 250 CAD = 250 x 1.0028 = 250.70 SGD	M1, A1																								
14b	See SELL rate as bank is selling JYP 100 JPY = 0.9447 SGD 500 SGD = 500/0.9447 X 100 = 52926.855 = 52927 JYP	M1 A1																								
15a	<table><tr><td>Pattern number</td><td>Black arrows</td><td>White arrows</td><td>Total</td></tr><tr><td>1</td><td>4</td><td>2</td><td>6</td></tr><tr><td>2</td><td>7</td><td>4</td><td>11</td></tr><tr><td>3</td><td>10</td><td>6</td><td>16</td></tr><tr><td>4</td><td>13</td><td>8</td><td>21</td></tr><tr><td>5</td><td>16</td><td>10</td><td>26</td></tr></table>	Pattern number	Black arrows	White arrows	Total	1	4	2	6	2	7	4	11	3	10	6	16	4	13	8	21	5	16	10	26	B1
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15bi	2n	B1																								
15bii	5n+1	B1																								
15c	5n + 1 = 615 5n = 614 n = 122.8 He is not correct as n is not a whole number when total has 615 arrows.	M1 A1																								
16a	$\frac{k - (-1)}{3 - k} = 3$ $\frac{k + 1}{3 - k} = 3$ $k + 1 = 9 - 3k$ $4k = 8$ $k = 2$ P is (2, -1)	M1 M1 or (attempt) to solve A1																								
16b	$y = mx + c$ $-3 = 3(5) + c$ $-3 = 15 + c$ $-18 = c$ $y = 3x - 18$	M1 A1																								

17a	<table border="1"> <tr> <td>16</td><td>20</td><td>24</td></tr> <tr> <td>20</td><td>25</td><td>30</td></tr> <tr> <td>24</td><td>30</td><td>36</td></tr> </table>	16	20	24	20	25	30	24	30	36	B2 Deduct 1 for each error
16	20	24									
20	25	30									
24	30	36									
17bi	P (prime) = $6/36 = 1/6$	B1									
17bii	P(at most 20) = $1-6/36 = 5/6$	B1									
17biii	P(irrational) = 0	B1									
18a	$x^2 - 6x - 16$ $= x^2 - 6x + \left(\frac{-6}{2}\right)^2 - 16 - \left(\frac{-6}{2}\right)^2$ $= (x-3)^2 - 25$ a = -3 and b = -25	M1 A1 OR B2									
18bi	x = 3	B1									
18bii	When y = 0, $(x-3)^2 - 25 = 0$ $(x-3)^2 = 25$ $x-3 = \pm\sqrt{25}$ $x = \pm\sqrt{25} + 3$ X = 8 or -2	M1 (solve) A1									
19a	No he is not correct as the line AB has a positive gradient so it should be upward sloping.	M1 (positive m) A1 (upward slope)									
19b	$x = \frac{-4+2}{2} = -1$ $y = -(-1+4)(-1-2) = 9$ Max pt (-1, 9)	M1 (find x coord) or any other method A1									
20a	$L = \sqrt{5^2 + 18^2} = \sqrt{349}$ Curved area = $\pi r L = \pi(5)(\sqrt{349})$ $= 293.4489707$ $= 293 \text{ cm}^2$	M1 M1 A1									
20b	$293.4489707 = \frac{\theta}{360} \times \pi(\sqrt{349})^2$ $\theta = 96.4 \text{ (1dp)}$	M1 A1									

	Or $\frac{1}{2}(\sqrt{349})^2 \theta = 293.4489707$ $\theta = 1.68\text{rad} = \frac{1.68}{\pi} \times 180^\circ$ $= 96.4^\circ$	
21	See construction	[4]