

**Paper 1  
Multiple Choice**

Question	Key	Question	Key	Question	Key
1	A	6	A	11	C
2	A	7	C	12	D
3	B	8	B	13	D
4	C	9	D	14	C
5	A	10	A	15	D
16	C	21	A	26	A
17	D	22	A	27	C
18	C	23	D	28	A
19	C	24	A	29	C
20	A	25	A	30	B

**Notes:**

Candidates found **Questions 1, 2, 5, 9, 11, 18, 24, 26** and **27** relatively challenging.

**Question 1**

Percentage uncertainty in  $L$  needed to be subtracted from, rather than added to, the percentage uncertainty in  $g$ .

**Question 2**

Distance is the total magnitudes of the areas of the triangles defined by the graph lines and the time axes.

**Question 9**

Those who chose option **C** confused between angular displacement and linear displacement.

**Question 11**

Those who chose option **D** assumed wrongly that the spacecraft must start from rest.

**Question 17**

Those who chose **B** found the centre-to-fringe distance instead of fringe-fringe distance. This requires a doubling of the new centre-fringe distance.

**Question 23**

Those who chose either **B** or **C** assumed wrongly that current must split equally at the junction

**Question 24**

Those who chose option **B**, omitted a factor of 2 either from omitting the  $\sin 30^\circ$  factor or from missing that the magnetic force is exerted on the coil at double the distance away from the pivot as is the weight.  
Those who chose option **D** treated the coil as consisting of a single turn rather than 50.

**Question 27**

Those who chose option **D** neglected to consider the effect of half-wave rectification.

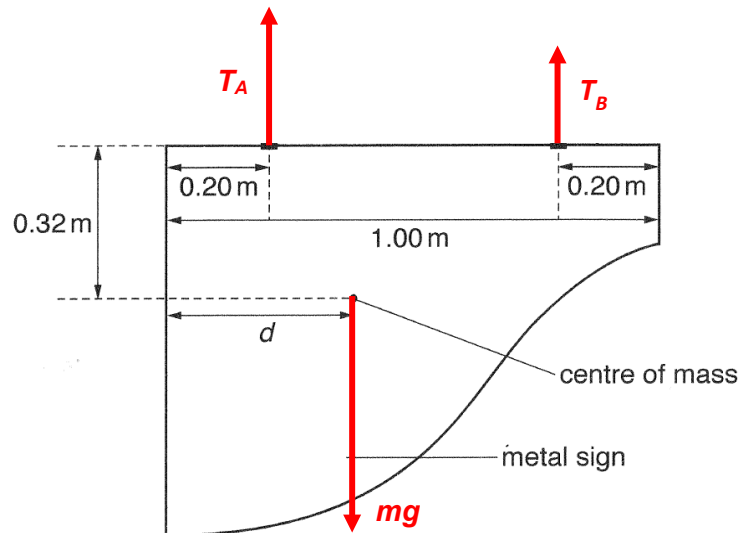
**Paper 2**  
**Structured Questions**

Qns	Marks
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- 1(a) when a body is in rotational equilibrium, the sum of clockwise moments about any point must be equal to the sum of anticlockwise moments about the same point.

**B1**

1(b)(i)



As metal sign is in translational equilibrium,

$$T_A + T_B = mg$$

$$= (4.5)(9.81)$$

$$T_A + T_B = 44.145 \text{ --- (1)}$$

Since the perpendicular distance of  $T_A$  is smaller than that of  $T_B$  from the centre of mass,  $T_A > T_B$

therefore  $\frac{T_B}{T_A} = \frac{3}{7} \text{ --- (2)}$

**M1**

Solving (1) and (2):

$$T_A = 31 \text{ N}$$

$$T_B = 13 \text{ N}$$

**A1**

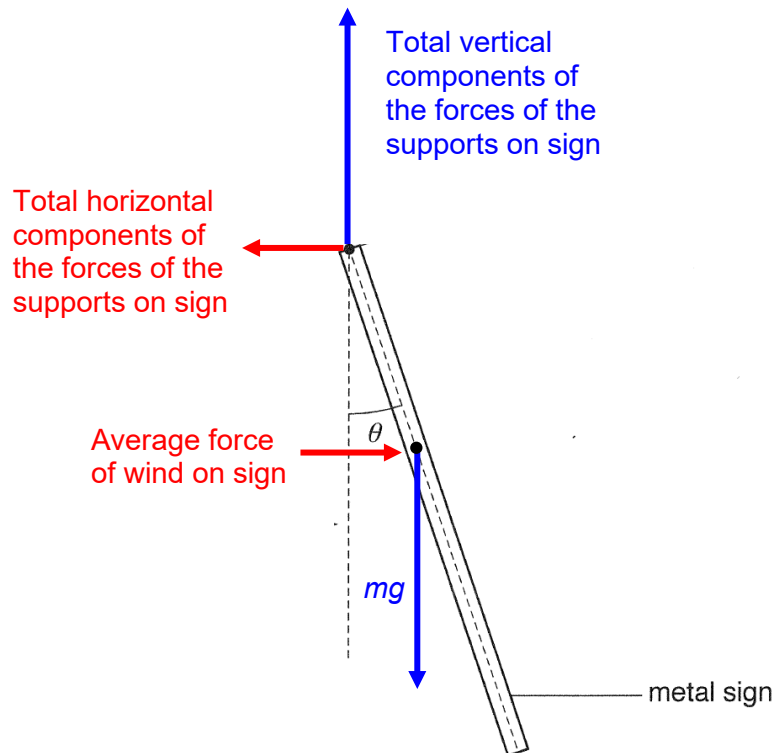
**Notes:** Be careful not to get the  $\frac{T_B}{T_A} = \frac{3}{7}$  values the wrong way around.

- 1(b)(ii) Taking moments about the centre of mass,  
 $T_A (d - 0.20) = T_B (1.00 - d - 0.20)$   
 $31 (d - 0.20) = 13 (1.00 - d - 0.20)$   
 $d = 0.38 \text{ m}$

**C1**

**A1**

Qns	Marks
1(c)	



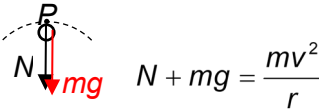
wind exerts a horizontal force on the sign to the right

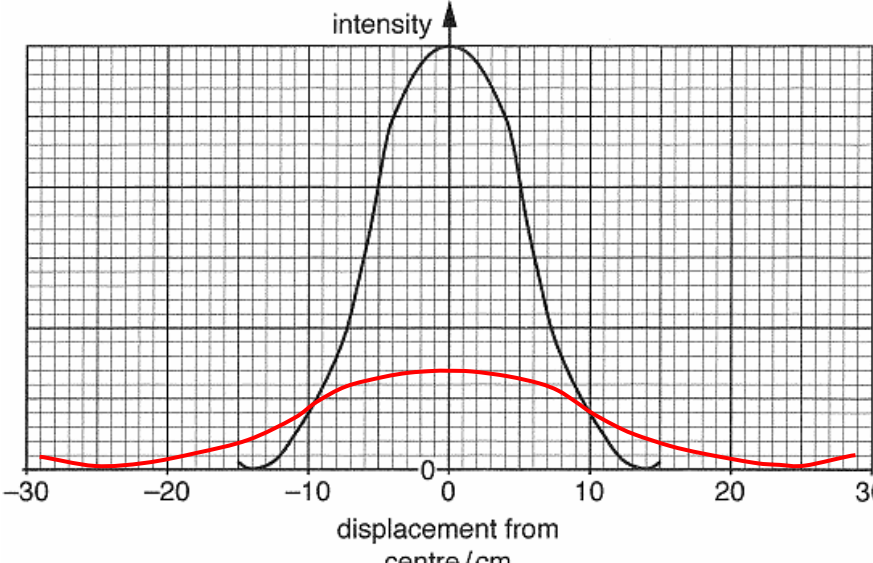
to maintain translational equilibrium of the metal sign, force that each support provides on the sign must have a horizontal component to balance the rightward force.

**B1**

**Notes:** Do not simply state that a horizontal force is needed as wind is horizontal. Remember to state explicitly that this force is to maintain translational equilibrium.

Common misconception: Some may attribute the horizontal force as resulting from N3L applied to the wind force. From N3L, the sign is the one exerting an equal and opposite force on the wind, this force is not a force acting on the sign by the support.

Qns	Marks
<b>2(a)</b> the change in length of a material is directly proportional to the force applied on it, provided that the limit of proportionality is not exceeded.	<b>B1</b>
<b>2(b)</b> elastic potential energy stored = area under load-compression graph $= \frac{1}{2}(85 \times 10^{-3})(6.8)$ $= 0.29 \text{ J}$	<b>M1</b>  <b>A1</b>
<b>2(c)</b> loss in elastic PE = gain in KE and gravitational PE	<b>B1</b>
$EPE_i - 0 = \left( \frac{1}{2}mv^2 - 0 \right) + mgh$ $0.29 - 0 = \frac{1}{2}(42 \times 10^{-3})v^2 + (42 \times 10^{-3})(9.81)(0.40)$ $= 2.4 \text{ ms}^{-1}$	<b>M1</b>  <b>A1</b>
<b>Notes:</b> Be careful not to forget the GPE too.	
<b>2(d)(i)</b>	
	
At minimum speed, normal contact force $N = 0$ , Hence weight provides centripetal force.	<b>B1</b>
Thus $mg = \frac{mv_{\min}^2}{r}$	<b>M1</b>
$v_{\min} = \sqrt{rg}$ $= \sqrt{(0.20)(9.81)}$ $= 1.4 \text{ m s}^{-1}$ $v_{\min} = 1.4 \text{ m s}^{-1}$	<b>A1</b>
<b>2(d)(ii)</b>	
$v_{\min} = \sqrt{rg}$ $v_{\min} \text{ is independent of mass and hence does not change}$	<b>B1</b>

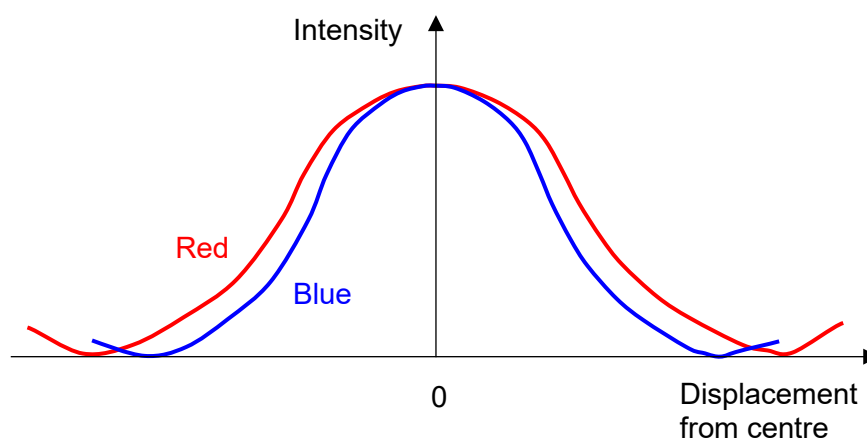
Qns	Marks
<b>3(a)</b> a wave spreads out after passing through a slit or around the edge of an obstacle [do not accept spreading “through” an obstacle, “bending” of waves, “splitting” of waves]	<b>B1</b>
<b>3(b)</b> $\sin \theta = \frac{\lambda}{b}$ For very small angle $\theta$ , $\sin \theta \approx \tan \theta = \frac{0.14}{2.7}$ $\frac{0.14}{2.7} = \frac{\lambda}{12 \times 10^{-6}}$ $\lambda = 6.2 \times 10^{-7} \text{ m}$	<b>M1</b> <b>M1</b> <b>A1</b>
<b>3(c)</b> 	<b>B1</b> <b>B1</b>  <b>B1</b> <b>B1</b>

$\sin \theta = \frac{\lambda}{b}$ , a narrower slit (smaller  $b$ ) means a larger  $\theta$ . more spreading of the waves. broader central maxima.

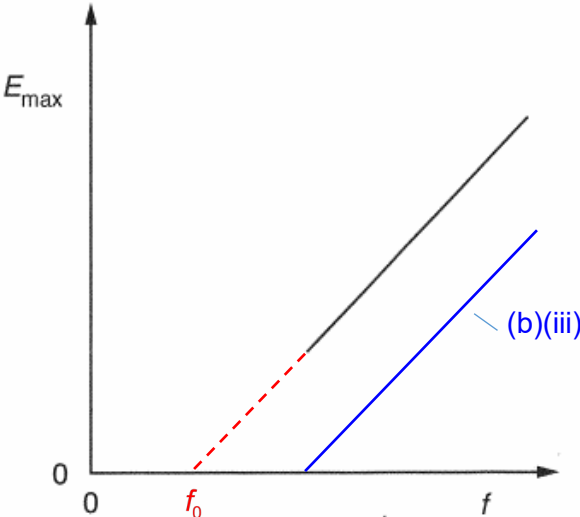
less light passes through, lower overall intensity

**3(d)(i)**  $\sin \theta = \frac{\lambda}{b}$ , a longer wavelength  $\lambda$  would mean a larger  $\theta$  for the angular positions of the first minima.  
The central maximum would be broader.

Qns		Marks
3(d)(ii)	<p>white light spectrum consists of wavelengths spanning 400 – 700 nm.</p> <p><math>\sin \theta = \frac{\lambda}{b}</math>, amount of spreading depends on wavelength <math>\lambda</math> of the incident light.</p>	B1
	<p>longer wavelengths at the red end spreads more as compared to shorter wavelengths, hence the edges are red</p> <p>at the central region, the different wavelengths overlap to produce white</p>	B1



**Notes:** Remember to use scientific terms such as interference/ overlapping. Common misconception: There is white light at centre as there is no diffraction at the centre.

Qns	Marks
<b>4(a)</b> minimum frequency of electromagnetic radiation for electrons to be emitted from metal surface.	<b>B1</b>
at this frequency, electrons are emitted with zero kinetic energy	<b>B1</b>
<b>4(b)</b>	
	<b>B1</b> <b>(f<sub>0</sub>)</b> <b>B1</b> <b>(b)(iii)</b>
<b>4(b)(ii)</b> gradient is equal to the Planck constant $h$	<b>B1</b>
$hf = \Phi + E_{K,\max} \rightarrow E_{K,\max} = hf - \Phi$	
<b>4(c)(i)</b>	
$\frac{hc}{\lambda} = \Phi + \frac{1}{2}mv_{\max}^2$ $\frac{(6.63 \times 10^{-34})(3.00 \times 10^8)}{(490 \times 10^{-9})} = 2.5(1.60 \times 10^{-19}) + \frac{1}{2}(9.11 \times 10^{-31})v_{\max}^2$ $v_{\max} = 1.1 \times 10^5 \text{ m s}^{-1}$	<b>M1</b> <b>C2</b> <b>A1</b>
<b>4(c)(ii)1</b> blue light has frequency higher than threshold frequency of europium, hence photoelectric effect occurs.	
electrons are emitted from the electroscope, gold leaf and rod become less charged and hence smaller electrostatic repulsion.	<b>B1</b>
frequency of red light is below threshold frequency of europium so no electrons are emitted	
<b>4(c)(ii)2</b> gold leaf rises due to electrostatic repulsion due to net lack of electrons.	<b>B1</b>
even if photoelectric effect occurs, electrons emitted from europium surface will only make the gold leaf and rod more positively charged and hence larger repulsion	<b>B1</b>
<b>Notes:</b> Remember that only electrons are free to move and do not use terms like positive charge cannot be emitted.	

Qns	Marks
5(a)	
volume of 1 mole = $\frac{\text{mass of 1 mole}}{\text{density}}$ $= \frac{63.5 \times 10^{-3}}{8960}$ $= 7.087 \times 10^{-6} \text{ m}^3$	C1
number density of copper atoms = $\frac{N_A}{\text{volume of 1 mole}}$ $= \frac{6.02 \times 10^{23}}{7.087 \times 10^{-6} \text{ m}^3}$ $= 8.49 \times 10^{28} \text{ m}^{-3}$	C1
each atom has 1 conduction electron, so number density of charge carriers is $8.49 \times 10^{28} \text{ m}^{-3}$ .	B1
5(b)	
$P = I^2 R$	C1
$5.0 = I^2 (30)$	C1
$I = 0.41 \text{ A}$	
$I = Anvq$	
$0.41 = \left[ \frac{\pi (0.36 \times 10^{-3})^2}{4} \right] (3.4 \times 10^{28}) (v) (1.60 \times 10^{-19})$	C1
$v = 7.4 \times 10^{-4} \text{ m s}^{-1}$	A1
5(c)	
$V = IR = (nAqv) \left( \frac{\rho L}{A} \right) = nev \rho L$	
same material, so number density of charge carriers $n$ is the same same temperature and material, so resistivity $\rho$ is same	M1
Hence drift velocity is inversely proportional to length	B1
Since length is <u>doubled</u> , drift velocity $v$ is <u>halved</u>	A1
[do not accept quantities <i>increased</i> or <i>decreased</i> ]	



Qns	Marks
<b>6(a)(i)</b> $V_Q = I_Q R_Q$ $V_{out} = V_Q$ $= (27 \times 10^{-3})(90)$ $= 2.4 \text{ V}$	<b>A1</b>
<b>6(a)(ii)</b> before connecting thermistor, $V_P = I_P R_P$ $R_P = \frac{V_P}{I_P} = \frac{\text{e.m.f.} - V_Q}{I}$ $= \frac{9.0 - 2.4}{27 \times 10^{-3}}$ $R_P = 240 \Omega$	<b>C1</b>
after connecting thermistor, resistance of parallel branch with Q $R_{//} = \left( \frac{1}{120} + \frac{1}{90} \right)^{-1}$ $= 51 \Omega$	<b>C1</b>
by potential divider rule, $V_{out} = \frac{51}{51 + 240} (9.0)$ $= 1.6 \text{ V}$	<b>A1</b>
<b>Note:</b> Current in the circuit does not remain at 27 mA when the thermistor is connected as the total resistance of the circuit has changed.	
<b>6(a)(iii)</b> When the temperature of the NTC thermistor is increased, its resistance would decrease.	<b>B1</b>
The total resistance of the thermistor in parallel with Q is thus reduced. By the potential divider rule, $V_{out}$ would also decrease.	<b>M1</b>
<b>OR</b>	<b>A1</b>
(The total resistance increases.)	<b>(M1)</b>
(P.d. across P increases, hence $V_{out}$ decreases)	<b>(A1)</b>

Qns	Marks
6(b)	
$\text{Arc AB} = r\theta$ $= (1.2 \times 10^{-2}) \left( \frac{92}{180} \pi \right)$ $= 0.01927 \text{ m}$	C1
<p>By the potential divider rule,</p> $V_{out} = \frac{0.01927}{6.5 \times 10^{-2}} \times 9.0$ $= 2.7 \text{ V}$	C1 A1

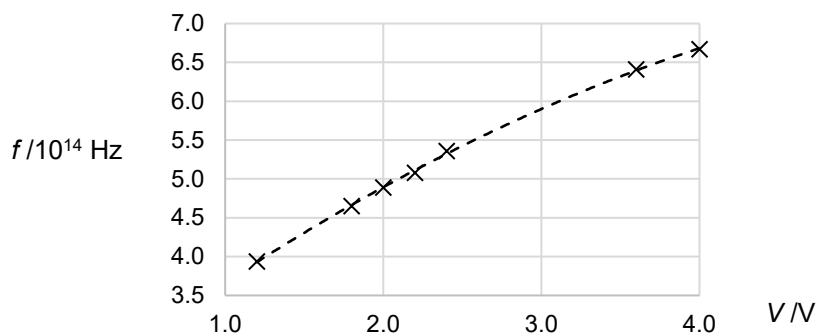
**Note:**

The resistance wire is not a full circle hence its length is not the circumference of the circle (length of resistance wire is already given so there is no need to calculate).

Qns		Marks
7(a)	As the p.d. $V$ across the LED increases, the frequency $f$ of the emitted photons increases (at a decreasing rate).	B1

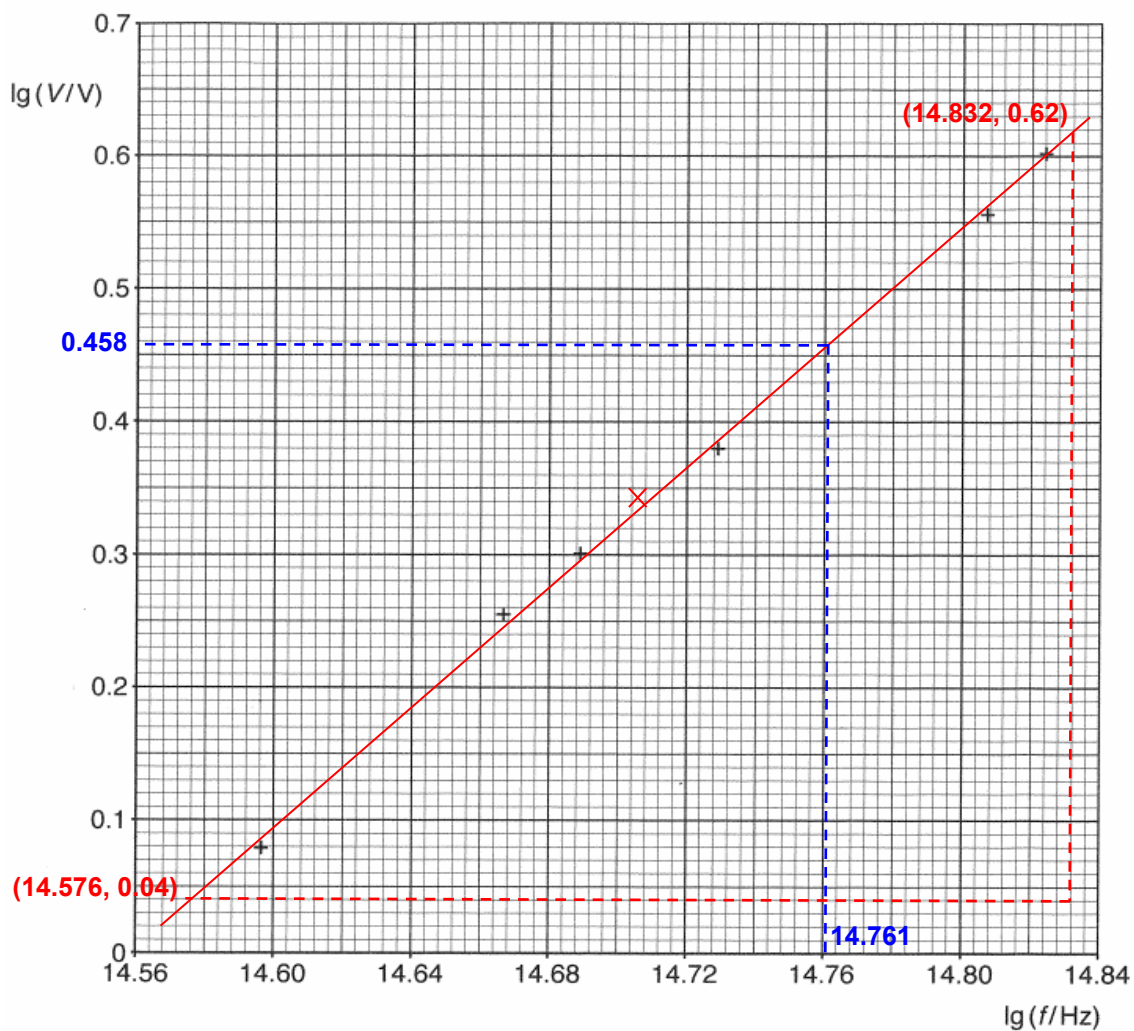
**Note:**

This is not a proportional relationship: when  $V$  is doubled from 2.0 V to 4.0 V,  $f$  is not doubled.



7(b)(i),

(ii)



- Plot accurate to  $\frac{1}{2}$  smallest square.
- Best fit line drawn.

B1  
B1

Qns	Marks
7(b)(iii)	
$V = kf^n$ $\lg V = n \lg f + \lg k$	M1
$\text{gradient} = \frac{y_1 - y_2}{x_1 - x_2} = \frac{0.620 - 0.040}{14.832 - 14.576}$ $= \frac{0.580}{0.256} = 2.27$	
$n = \text{gradient} = 2.27$	A1
7(c)(i)	
$\lg f = \lg\left(\frac{c}{\lambda}\right)$ $= \lg\left(\frac{3.00 \times 10^8}{520 \times 10^{-9}}\right) = 14.761$	M1
From graph, when $\lg f = 14.761$ , $\lg V = 0.458$ Thus, $V = 2.87 \text{ V}$	M1 A1
7(c)(ii)	
$Pt = N(\text{photon energy})$ $(10)(60) = N(3.8 \times 10^{-19})$ $N = 1.6 \times 10^{21}$	C1 A1
7(c)(iii)	
$V = IR$ $(4.5 - 2.87) = (20 \times 10^{-3})R$ $R = 82 \, \Omega$	C1 A1

**Notes:**  $V$  is not the potential difference of the power supply but the potential difference across the series resistor.

7(d)

$$Q = It = (730 \times 10^{-3} \text{ A})(60 \times 60 \text{ s})$$

$$= 2.63 \times 10^3 \text{ C}$$

The total amount of charge available from the power supply is 730 mAh or  $2.63 \times 10^3 \text{ C}$ .

The power supply can provide a current of 730 mAh for 1 hour.

For a varying current, the product of the average current and time = 730 mAh.

B1

B1

**Note:**

Candidates need to state that 730 mAh is the total amount of charge available from the supply.

Qns	Marks
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7(e)

$$\frac{e_{LED}}{e_{lamp}} = \left( \frac{P_{out}}{P_{in}} \right)_{LED} \div \left( \frac{P_{out}}{P_{in}} \right)_{lamp}$$

$$= \frac{800}{10} \div \frac{840}{60}$$

$$= 5.7$$

C1  
A1

7(f)(i)

For roughly the same brightness, LEDs and CFLs require  $\frac{10}{60} \times 100\% = 17\%$

B1

and  $\frac{14}{60} \times 100\% = 23\%$  of the power input required by incandescent lamps respectively.

This means that the power sources of appliances using these lamps (e.g. torches) do not have to be recharged or replaced as often as compared to incandescent lamps.

B1

7(f)(ii)

Consider 50k hours of operation:

Cost	LED	CFL
Electricity	(10 W)(50kh)(\$0.22 / kWh) = \$110.00	(14 W)(50kh)(\$0.22 / kWh) = \$154.00
Lamps	1×(\$35.95) = \$35.95	5×(\$3.95) = \$19.75
Total Cost	\$145.95	\$173.75

M1

M1

Thus, LED lamps are more cost effective and LTA should proceed with the replacement of all CFLs.

A1

7(f)(iii)

Incandescent lamps are less efficient and much of the input power is given off as heat. This could melt the snow that would otherwise cover the traffic lights.

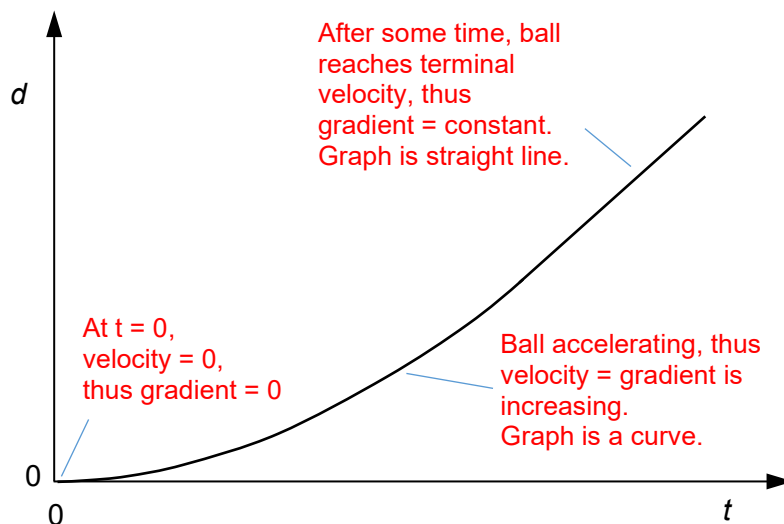
B1

**Paper 3**  
**Longer Structured Questions**

**Qns**

**Marks**

**1(a)**



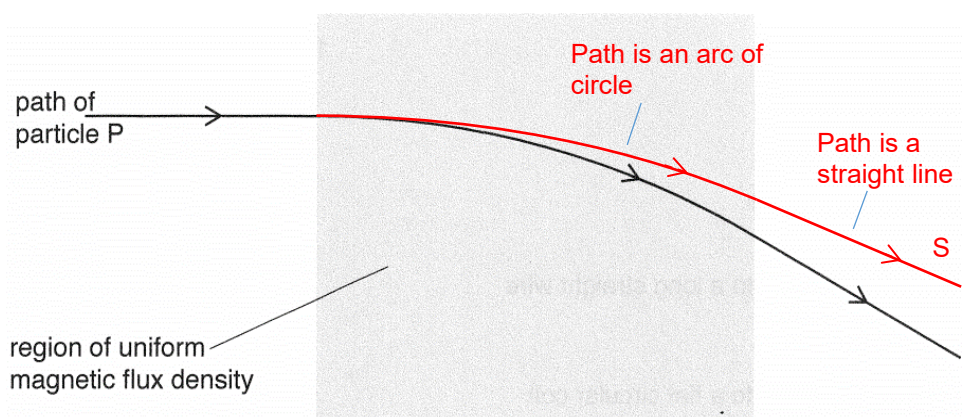
**B2**

[all 3 correct: 2 m. Any 1 missing: 1 m. Else 0 m.]

**Note:**

The question explicitly stated that the ball is falling through air, thus air resistance is not negligible. After some time, the ball would have reached terminal velocity.

**1(b)**



**B2**

[1 mark for each key part of path]

**Note:**

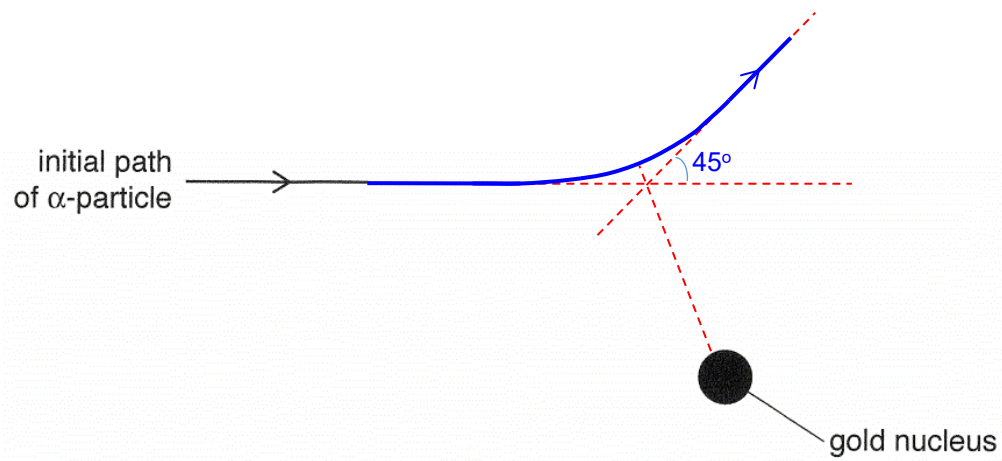
In the magnetic field, we have  $Bqv = m \frac{v^2}{r} \rightarrow r = \frac{mv}{Bq}$ . Thus with twice the speed, particle S would have a path that is an arc of a circle with a larger radius. Once P leaves the magnetic field, its path would be a straight line as there is no longer a magnetic force acting on it.

Candidates are strongly advised to label the different parts of the path with appropriate description.

Qns

Marks

1(c)



- drawing 2 straight lines joined by a curve in between
- appropriate positioning of the point of closest approach

B1  
B1

Qns		Marks
2(a)	a region of space where <u>a mass</u> experiences a <u>gravitational force</u> .	<b>B1</b> <b>B1</b>
2(b)(i)	The diameters of the Sun and Proxima Centauri are about $10^6/10^{13} = 10^{-7}$ and $10^5/10^{13} = 10^{-8}$ times of their separation respectively the <u>two stars can be treated as point masses since their diameters are negligible when compared to their separation</u>	<b>B1</b>
<b>Note:</b>		
Newton's law of gravitation applies to point masses. Thus, the need to justify why the two stars can be considered as point masses.		
Where possible, candidates should quantify their claims in their explanation. For example, finding the ratio of 2 quantities to show that one is very much larger or smaller than the other.		
2(b)(ii)	$F = \frac{Gm_1m_2}{r^2}$ $= \frac{(6.67 \times 10^{-11})(2.0 \times 10^{30})(2.4 \times 10^{29})}{(4.0 \times 10^{13} \times 10^3)^2}$ $= 2.0 \times 10^{16} \text{ N}$	<b>M1</b> <b>A1</b>
2(c)	$a = \frac{F}{m} = \frac{2.0 \times 10^{16}}{2.0 \times 10^{30}} = 1.0 \times 10^{-14} \text{ m s}^{-2}.$ <p>Although <math>F</math> is very large, but because the mass of the Sun is also very large, the resulting acceleration of the Sun is negligible.</p>	<b>M1</b> <b>A1</b>

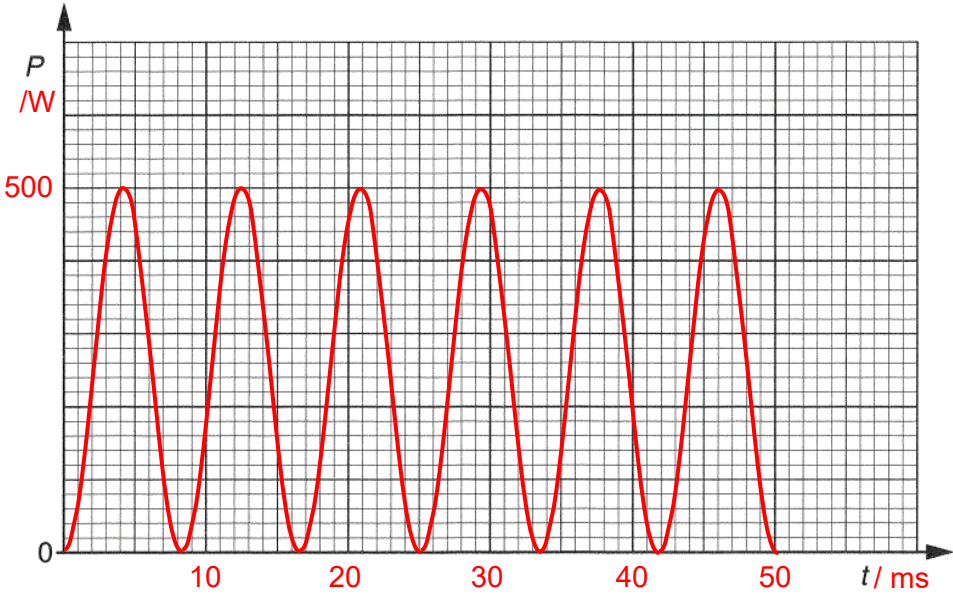
**Note:**

By motion, we can mean velocity and/or acceleration. Since the effect of a force on a body is given by Newton's 2<sup>nd</sup> Law, we discuss acceleration which needs to be worked out.



Qns	Marks
<b>3(a)(i)</b> $E = \left(\frac{\Delta V}{d}\right)$ (where $E$ is Electric field strength, $\Delta V$ is the p.d. between the plates, and $d$ is the plate separation.)	<b>M1</b>
$F = qE$ $= q\left(\frac{\Delta V}{d}\right)$ $= (3.2 \times 10^{-19})\left(\frac{900}{3.6 \times 10^{-2}}\right)$ $= 8.0 \times 10^{-15} \text{ N}$	<b>M1</b> <b>A0</b>
<b>3(a)(ii)</b> $a = \frac{F}{m}$ $= \frac{8.0 \times 10^{-15}}{6.6 \times 10^{-27}}$ $= 1.2 \times 10^{12} \text{ m s}^{-2}$	<b>M1</b> <b>A1</b>
<b>3(b)</b> $+ \rightarrow: s_x = u_x t$ $t = \frac{s_x}{u_x}$ $= \frac{7.5 \times 10^{-2}}{4.1 \times 10^5} = 1.8 \times 10^{-7} \text{ s}$	<b>C1</b>
$+ \downarrow: s_y = u_y t + \frac{1}{2} a_y t^2$ $= 0 + \frac{1}{2} (1.2 \times 10^{12}) (1.8 \times 10^{-7})^2$ $= 1.9 \times 10^{-2} \text{ m}$	<b>C1</b>
The particle could have a vertical displacement of 1.9 cm downwards. This is more than $3.6 / 2 = 1.8$ cm, the vertical distance to the lower plate. Thus, the particle would collide with the lower plate.	<b>A1</b>

Qns		Marks
4(a)(i)	the force per unit length per unit current acting on a conductor carrying a current placed at right angle to the magnetic field.	B1 B1 B1
4(a)(ii)	product of the magnetic flux density normal to the loop, the area of the loop and the number of turns of wire in the loop.	B1 B1
	<b>Note:</b> It is not acceptable to just write that magnetic flux linkage is the “product of magnetic flux and number of turns”, without defining magnetic flux.	
4(b)	When the switch is closed, a direct current (dc) flows in the coil and increases from zero to a steady value. Current sets up increasing magnetic flux through the aluminium ring.	B1
	By Faraday’s Law, the increasing flux linkage through the ring induces e.m.f. in the ring.	B1
	The ring is a closed conducting path, induced current flows in the ring.	B1
	By Lenz’s Law, the induced current produces a magnetic field opposite in direction to the coil’s field to oppose the increasing flux. This results in a repulsive force causing the ring to jump up vertically.	B1
	<b>Note:</b> It is the induced current and not the induced e.m.f. that gives rise to the opposing magnetic field in the ring. Therefore, it must first be established that there is induced current flow, else there would only be induced e.m.f. but no repulsive force.	
4(c)	When the switch is closed, the same e.m.f. is induced in the ring. However, since the ring is an insulator, there is no induced current in the ring to set up the opposing magnetic field. Thus, there is no repulsive force on the ring. The ring will not move.	M1 A1
	<b>Note:</b> There is still induced e.m.f. even though the ring is an insulator.	

Qns		Marks
5(a)	the value of a steady direct current that will dissipate heat at the same average rate in a given resistor	B1 B1
	<p>Note:</p> <p>It is the rate of heating/ energy dissipation that must be considered and that the heating takes place in a resistor.</p>	
5(b)(i)	$V_{rms} = \frac{V_o}{\sqrt{2}} = \frac{170}{\sqrt{2}} = 120 \text{ V}$	B1
5(b)(ii)	$f = \frac{\omega}{2\pi} = \frac{377}{2\pi}$ $= 60.0 \text{ Hz}$	M1 A1
5(b)(iii)	$\langle P \rangle = \frac{(V_{rms})^2}{R}$ $= \frac{120^2}{58} = 250 \text{ W}$	M1 A1
5(c)	 <p> <math>P_o = 2\langle P \rangle = 2(2.5 \times 10^2) = 500 \text{ W}</math> </p> <p>             Period for alternating p.d., <math>T = \frac{1}{f} = \frac{1}{60.0} = 16.7 \text{ ms}</math> </p> <ul style="list-style-type: none"> <li>Correct shape (smooth sine-squared graph)</li> <li>axes clearly labelled correctly with units and values</li> <li>At least 4 cycles of power curve drawn</li> </ul>	B1 B1 B1

Qns		Marks
6(a)	a discrete packet of energy of electromagnetic radiation energy of each photon = <i>Planck constant</i> × <i>frequency</i>	M1 A1
6(b)(i)	$E = \frac{hc}{\lambda} = \frac{(6.63 \times 10^{-34})(3.00 \times 10^8)}{(680 \times 10^{-9})}$ $= 2.9 \times 10^{-19} \text{ J}$	M1 A1
6(b)(ii)	<p>Intensity <math>I = \frac{P}{A} = \frac{NE}{tA}</math></p> $\frac{N}{t} = \frac{IA}{E}$ $= \frac{(3.1 \times 10^3) \left[ \pi \left( \frac{1.2 \times 10^{-3}}{2} \right)^2 \right]}{2.9 \times 10^{-19}}$ $= 1.2 \times 10^{16} \text{ s}^{-1}$	M1 A0
6(c)	<p>Momentum of each photon, <math>p = \frac{h}{\lambda} = \frac{6.63 \times 10^{-34}}{680 \times 10^{-9}} = 9.75 \times 10^{-28} \text{ N s}</math></p> <p><u>Take upward direction as positive.</u> <u>In the normal direction</u>, we have:</p> <p>By Newton's 2<sup>nd</sup> Law, Force = <math>\frac{N}{t}(p_f - p_i)</math></p> <p>Force of surface on reflected photons</p> $= 0.55 \left( \frac{N}{t} \right) [(+p \cos 52^\circ) - (-p \cos 52^\circ)] = 1.10 \left( \frac{N}{t} \right) p \cos 52^\circ \text{ N}$ <p>Force of surface on absorbed photons</p> $= 0.45 \left( \frac{N}{t} \right) [0 - (-p \cos 52^\circ)] = 0.45 \left( \frac{N}{t} \right) p \cos 52^\circ \text{ N}$ <p>Total force of surface on photons = <math>1.10 \left( \frac{N}{t} \right) p \cos 52^\circ + 0.45 \left( \frac{N}{t} \right) p \cos 52^\circ</math></p> $= 1.55 \left( \frac{N}{t} \right) p \cos 52^\circ$ $= 1.55(1.2 \times 10^{16})(9.75 \times 10^{-28}) \cos 52^\circ$ $= 1.1 \times 10^{-11} \text{ N}$ <p>By Newton's 3<sup>rd</sup> Law,</p> <p> Force of photons on surface  =  force of surface on photons </p> $= 1.1 \times 10^{-11} \text{ N}$	M1 M1 M1 M1 M1 A1

Qns	Marks
<p>7(a)(i) When the <b>activity</b> of a radioactive sample is measured (e.g. using a GM counter) <u>under constant external conditions at any instant in time, the count rate always fluctuates</u> (rise and fall irregularly).</p> <p><b>Note:</b> The answer requires an <u>experimental observation</u>, not a definition.</p>	B1
<p>7(a)(ii) The <b>half-lives</b> of similar radioactive samples of the same nuclei measured <u>under different external conditions</u> such as pressure and temperature <u>are the same</u>.</p> <p><b>Note:</b> The answer requires an <u>experimental observation</u>, not a definition.</p>	B1
<p>7(b)(i) From graph, activity dropped from <math>5.8 \times 10^5 \text{ s}^{-1}</math> to <math>0.9 \times 10^5 \text{ s}^{-1}</math> in first 40 days</p> $A = A_0 e^{-\lambda t}$ $0.9 \times 10^5 = 5.8 \times 10^5 e^{-\lambda(40 \times 24 \times 60 \times 60)}$ $\lambda = 5.39 \times 10^{-7} \text{ s}^{-1} \approx 5.3 \times 10^{-7} \text{ s}^{-1}$ <p>OR</p> <p>After 2 half-lives, <math>A = \frac{5.8 \times 10^5}{4} = 1.45 \times 10^5 \text{ s}^{-1}</math></p> <p>From the graph, <math>t = 30</math> days</p> <p>Half-life = <math>30/2 = 15</math> days</p> $\lambda = \frac{\ln 2}{15 \times 24 \times 60 \times 60} = 5.34 \times 10^{-7} \text{ s}^{-1} \approx 5.3 \times 10^{-7} \text{ s}^{-1}$	<p>M1</p> <p>M1</p> <p>A1</p>
<p>7(b)(ii) <math>A_0 = \lambda N_0</math></p> $5.8 \times 10^5 = 5.3 \times 10^{-7} N_0$ $N_0 = 1.094 \times 10^{12}$ <p><math>M = N_0 \times 32u</math></p> $= (1.094 \times 10^{12})(32 \times 1.66 \times 10^{-27})$ $= 5.8 \times 10^{-14} \text{ kg} = 5.8 \times 10^{-11} \text{ g}$ <p>OR</p> $M = \frac{M_m}{N_A} N_0$ $= \frac{32}{6.02 \times 10^{23}} (1.094 \times 10^{12})$ $= 5.8 \times 10^{-11} \text{ g}$	<p>M1</p> <p>A1</p> <p>(A1)</p>

Qns		Marks
8(a)(i)	sum of the <u>kinetic energy due to the random motion of a distribution of molecules</u> and <u>potential energy due to intermolecular forces between the molecules</u>	<b>B1</b> <b>B1</b>
8(a)(ii)	+ $q$ heat supplied to a system + $W$ work done on a system	<b>B1</b> <b>B1</b>
8(b)(i)	A gas that obeys the equation of state $PV = nRT$ at all values of pressure $p$ , volume $V$ , amount of gas in moles $n$ , and thermodynamic temperature $T$ .	<b>B1</b> <b>B1</b>
<b>Note:</b> All symbols used must be defined.		
8(b)(ii)1	$pV = NkT$ $(5.4 \times 10^5)(1.2 \times 10^4 \times 10^{-6}) = N(1.38 \times 10^{-23})(57 + 273.15)$ $N = 1.4 \times 10^{24}$	<b>M1</b> <b>M1</b> <b>A1</b>
8(b)(ii)2	$\langle KE \rangle_{\text{molecule}} = \frac{3}{2} kT$ $= \frac{3}{2} (1.38 \times 10^{-23})(57 + 273.15)$ $= 6.8 \times 10^{-21} \text{ J}$	<b>M1</b> <b>A1</b>
8(b)(ii)3	For an ideal gas, there is no potential energy for the molecules. Thus, $U = N \langle KE \rangle_{\text{molecule}}$ $= (1.4 \times 10^{24})(6.8 \times 10^{-21})$ $= 9.5 \times 10^3 \text{ J}$	<b>M1</b> <b>A1</b>
8(c)(i)	$\Delta U = N \Delta \langle KE \rangle_{\text{molecule}} = N \left( \frac{3}{2} k \Delta T \right)$ $= (1.4 \times 10^{24}) \frac{3}{2} (1.38 \times 10^{-23})(155 - 57)$ $= 2.8 \times 10^3 \text{ J}$	<b>M1</b> <b>C1</b> <b>A1</b>
8(c)(ii)1	Since increase in internal energy = $(+q) + (+w)$ , $(+w)$ must be zero. So the volume of the gas must be constant.	<b>B1</b> <b>B1</b>

Qns	Marks
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**8(c)(ii)2** From **8(c)(i)** and **8(c)(ii)1**,  $2.8 \times 10^3$  J of thermal energy is required to increase the temperature of  $n$  moles of the gas from  $57^\circ\text{C}$  to  $155^\circ\text{C}$ .

$$\text{From } \mathbf{8(b)(ii)1}, n = \frac{N}{N_A} = \frac{1.4 \times 10^{24}}{6.02 \times 10^{23}} = 2.33$$

$$C = \frac{q}{n\Delta T} \quad \text{M1}$$

$$= \frac{2.8 \times 10^3}{(2.33)(155 - 57)} = 12.3 \text{ J mol}^{-1} \text{ K}^{-1} \quad \text{A1}$$

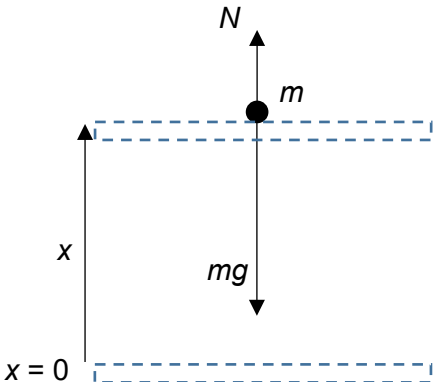
**OR**

$$C = \frac{q}{n\Delta T}$$

$$= \frac{\Delta U}{n\Delta T} \quad (\text{since } \Delta U = q \text{ from } \mathbf{8(c)(ii)1.})$$

$$= \frac{\left(\frac{3}{2}nR\Delta T\right)}{n\Delta T} = \frac{3}{2}R \quad \text{(M1)}$$

$$= \frac{3}{2}(8.31) = 12.5 \text{ J mol}^{-1} \text{ K}^{-1} \quad \text{(A1)}$$

Qns		Marks
9(a)(i)	acceleration (of an object) is always directed opposite to the direction of the displacement ( <b>OR</b> directed towards equilibrium point) and  directly proportional to its displacement from the equilibrium position.	<b>B1</b>  <b>B1</b>
9(a)(ii)1	There are <u>both positive and negative displacements</u> .  <b>Note:</b> The question expects candidates to use the features of the graph in their explanation.	<b>B1</b>
9(a)(ii)2	The graph is <u>curved</u> and <u>not a straight-line graph passing through the origin</u> , thus $a$ is not proportional to $x$ .  <b>Note:</b> Use the features of the graph in the explanation.	<b>B1</b>
9(b)(i)1	Amplitude at the upper position (or Maximum height).  <b>Note:</b> “At maximum amplitude” is not acceptable. There are 2 possible maximum amplitude positions hence the need to be specific.	<b>A1</b>
9(b)(i)2	<div></div> <div><math display="block">F = ma</math><math display="block">mg - N = ma</math><math display="block">= m(\omega^2 x)</math><p>When contact is lost,</p><math display="block">N = 0 \rightarrow x = \frac{g}{\omega^2}</math><p>When <math>\omega</math> is constant and <math>x_0</math> increased gradually, contact would first be lost when</p><math display="block">x_0 = \frac{g}{\omega^2} = \frac{9.81}{(2\pi \times 13)^2}</math><math display="block">= 1.47 \times 10^{-3} \text{ m} = 1.47 \text{ mm}</math></div>	<b>M1</b>  <b>M1</b>      <b>A1</b>
9(b)(ii)	A pebble has a larger mass $m$ . However, the minimum amplitude $x_0$ for which the pebble loses contact with the platform is given by $x_0 = \frac{g}{\omega^2}$ which is independent of $m$ . Thus, $x_0$ would be the same.	<b>M1</b> <b>A1</b>



Qns

Marks

9(c)(i)1

$$\begin{aligned}
 E_T &= (E_K)_{\max} \\
 &= \frac{1}{2}mv_o^2 = \frac{1}{2}m\omega^2 x_o^2 \\
 &= \frac{1}{2}(1.2)(2\pi \times 2.5)^2(3.4 \times 10^{-2})^2 \\
 &= 0.17 \text{ J}
 \end{aligned}$$

M1

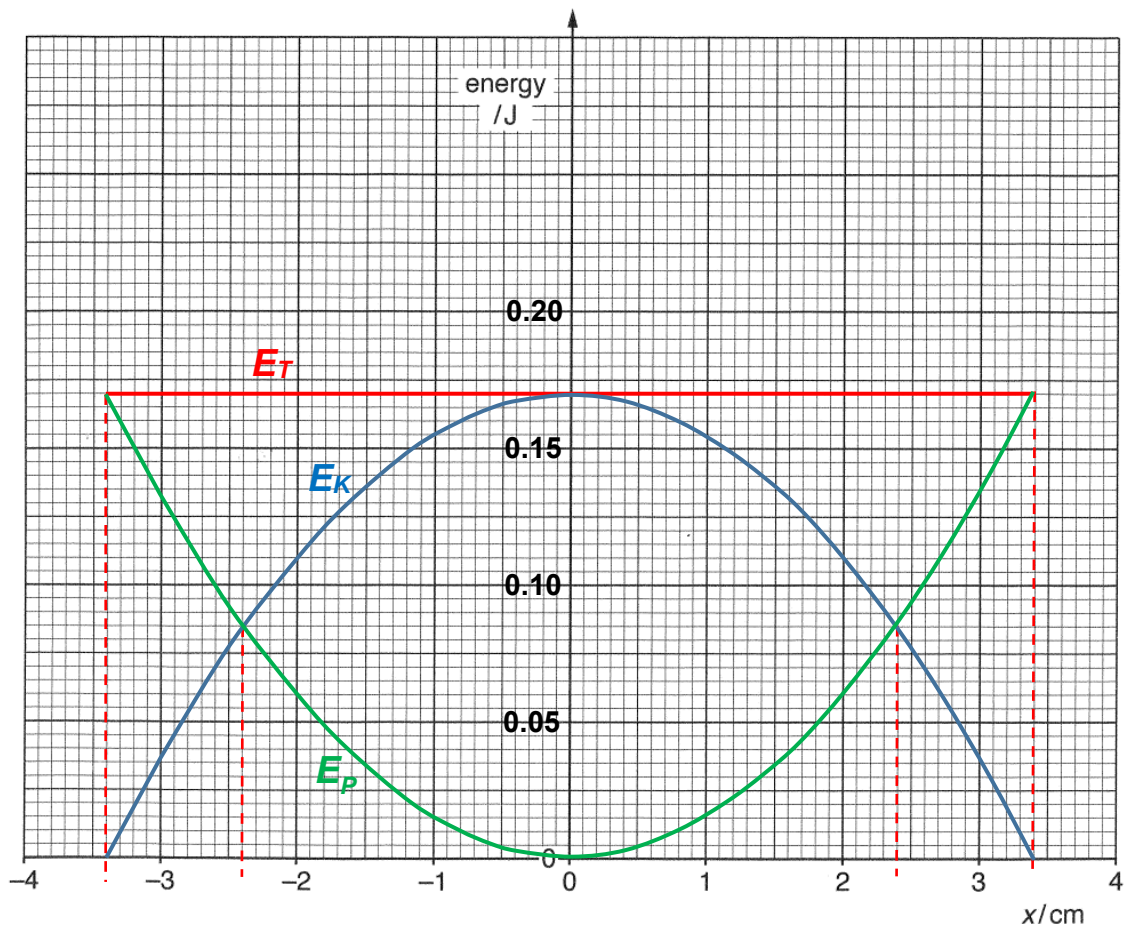
A1

9(c)(i)2

$$\begin{aligned}
 \text{When } E_K &= E_P, \\
 E_T &= E_P + E_K = 2E_K \\
 (E_K)_{\max} &= 2E_K \\
 \frac{1}{2}m\omega^2 x_o^2 &= 2\left(\frac{1}{2}m\omega^2(x_o^2 - d^2)\right) \\
 d &= \frac{x_o}{\sqrt{2}} = \frac{3.4}{\sqrt{2}} = 2.4 \text{ cm}
 \end{aligned}$$

M1

A1

9(c)(ii)  
1,2,3

- Energy axis clearly labelled
- Shape of KE and PE graphs quadratic, smooth curve
- KE and PE graphs intercept at  $x = \pm 2.4 \text{ cm}$
- TE at 0.17 J
- All graphs from  $x = -3.4 \text{ cm}$  to  $+3.4 \text{ cm}$

B1

B2

B1

B1

B1