

## **CHS Y1 Notes**

### **Arranged according to CHS Order of Learning**

- 1.Primes,HCF,LCM (TB Chapter 1)
- 2.Integers,Rational Numbers and Real Numbers (TB Chapter 2)
- 3.Approximation and Estimation (TB Chapter 3)
- 4.Percentage (TB Chapter 8)
- 5.Ratio and Rate (TB Chapter 9)
- 6.Basic Algebra and Manipulation (TB Chapter 4)
- 7.Linear Equations (TB Chapter 5),Simple Inequalities (Sec 2 TB Chapter 2)
- 8.Linear Functions and Graphs (TB Chapter 6)
- 9.Number Patterns (TB Chapter 7)
- 10.Basic Geometry (TB Chapter 10)
- 11.Polygons and Geometrical Constructions (TB Chapter 11)
- 12.Pythagoras Theorem (Sec 2 TB Chapter 9)
- 13.Perimeter and Area of Plane Figures (TB Chapter 12)
- 14.Volume and Surface Area of Prisms and Cylinders (TB Chapter 13)
- 15.Volume and Surface Area of Pyramids,cones and Sphere (Sec 2 TB Chapter 11)
- 16.Statistical Data Handling (TB Chapter 14)
- 17.Statistical Diagrams (Sec 2 TB Chapter 13)
- 18.Averages of Statistical Data (Sec 2 TB Chapter 14)

## **Primes. HCF, LCM**

### **Prime Number**

- Number that only has 2 factors and is a whole number greater than 1,such as 2, 3, 7, 13

### **Understanding Prime Factorisation**

- Used to express a composite number as a product of its prime factors,using a factor tree or long division
- When Prime Factorisation is performed some factors are repeated,eg  $8=2 \times 2 \times 2$ , with the factor 2 appearing 3 times
- Use concise notation to represent the product
- Notation with number above the below number is called index notation,read as 8 to the power of 3
- Number located at the top right hand corner called the index,number at the level is called base
- Index shows the number of times the base is multiplied by itself
- Use Ladder Method to find prime factorization of a number,start with smallest prime factor of the number and divide,keep dividing till you get 1 then times all the numbers

### **Square roots and Cube roots**

- 9 can be expressed as product of 2 identical numbers,  $9=3 \times 3=3^2$
- Since  $3^2=9$ , 9 is the square of 3, we can also say 3 is the positive square root of 9 and it is denoted 9 square root=3
- 8 can be expressed as a product of 3 identical numbers as  $8=2 \times 2 \times 2=2^3$ , since  $2^3=8$ , 8 is called cube of 2
- We can also say 2 is the positive cube root of 8 and denoted cube root 8=2
- For square numbers, power of prime factors must be divisible by 2
- For cube numbers, power of prime factors must be divisible by 3

### **Highest common factor and Lowest common multiple**

#### **Highest common factor**

- Largest common factor of a group is called HCF

756 expressed as a product of its prime factors is  $2^2 \times 3^3 \times 7$ , 360 expressed as a product of its prime factors is  $2^3 \times 3^2 \times 5$ , find hcf of 360 and 756

Method 1

$$360=2^3 \times 3^2 \times 5$$

$$756=2^2 \times 3^3 \times 7$$

$$\text{HCF}=2^2 \times 3^2$$

- Compare both numbers when expressed as a product of its prime factors then look for common factors (best squared/cubed)

#### **LCM**

- Find using prime factorisation

756 expressed as a product of its prime factors is  $2^2 \times 3^3 \times 7$ , 360 expressed as a product of its prime factors is  $2^3 \times 3^2 \times 5$ , find LCM of 360 and 756

$$360=2^3 \times 3^2 \times 5$$

$$756=2^2 \times 3^3 \times 7$$

$$\text{LCM}=2^3 \times 3^3 \times 5 \times 7$$

- Between  $2^3$  and  $2^2$  bring down bigger number, then bring down everything else

## **2. Integers, Rational Numbers and Real Numbers**

### **Negative Numbers**

#### **Negative Integers**

- Whole numbers are 1,2,3,4, known as positive integers
- Negative integers are -5,-4,-3
- Zero is neither positive nor negative integer

#### **Number line**

- All negative numbers to the left of zero, while All positive numbers to the right of zero
- Numbers are arranged in ascending order

#### **How to draw a number line**

- Draw horizontal line and mark zero point

- Use 1 cm ruler to mark points 1,2,3 at equal unit length to the right of 0 and -1,-2,-3, on left of 0
- Draw arrow heads on both ends of the lines

### **Addition and subtraction involving negative numbers (personal methods, idk if in syllabus)**

#### **Addition**

##### **Method 1**

- Use a number line
- Draw number line beginning at 0
- For negative numbers move that many spaces to the left
- For positive numbers move that many spaces to the right
- Examples -5+4
- Beginning at 0, -5 negative so move 5 spaces to the left, after that move 4 spaces to the right

##### **Method 2**

Use absolute value (outside the syllabus but still useful)

- Addition of large numbers
- Look at the signs
- If signs of the numbers you are adding are the same they are alike (go in the same direction)
- Therefore add up those two numbers and keep their sign

##### *Example*

$1 + -2 = -3$  (add 1 and 2 then keep negative sign)

- However if the signs of the numbers you are adding are different subtract absolute value of the 2 numbers
- Which number has a higher absolute value?
- The answer will have the same sign that this number had at the beginning

### **Subtracting Positive and negative numbers**

- Subtraction and Addition are opposites of each other, so we can change a subtraction problem by using the additive inverse or opposite

##### **Example**

$5 - 4$

- Additive inverse of 4 is -4 which we can change to a addition problem, so it's  $5 + -4 = 1$

##### **Example**

$7 - 10$

- Additive inverse of 10 is -10

$7 - 10 = 7 + (-10) = -3$

##### **Example**

A bird is flying at 42m above sea level and a fish is swimming 12 metres below sea level. How many meters apart are the fish and bird?

Birds height 42m

Fish height -12m

Subtract,  $42 - (12) = 42 + 12 = 54$

### **Multiplying and dividing positive and negative numbers**

- Multiply or divide the numbers, then count number of negative numbers
- If there an odd number of negative numbers answer is negative
- If there an even number of negative numbers answer is positive

## **3. Approximation and Estimation**

### **Approximation**

- Process of rounding off a given number to give approximate value

### **Significant figures**

- Round numbers to a required number of Significant Figures

### **Five rules to identify significant digits**

- All non zero digits are significant (eg 192 has 3 SF)
- All zeroes between non zero digits are significant (eg 32047 has 5 SF)
- In a decimal, all zeros after a non zero are significant (eg 0.10 has 2 SF)
- In a decimal all zeroes before a non zero are non significant (eg 0.010 has 2 SF)
- In whole numbers zeroes at the end may or may not be significant, it depends on how numbers are approximated

### **Example**

A piece of paper weighs 0.0004503g, round it to 1dp, 2dp, 3dp

1dp-0.0

2dp-0.00

3dp-0.000

0.0004503

4 is the 1st SF

And so on

508175.62

5 is 1st SF, 0 is 2nd SF, 8 is 3rd SF

### **Rounding and Truncation errors**

- Truncate means cut off the end, eg square root 162=12.72792206
- If we round if the answer to 3dp its 12.728, However if we truncate the answer at 3dp, it is 12.727
- There is no rounding off

### **Example**

2 divide by 3 on calculator has a few options

- If calculator shows 0.66666666666667 answer was rounded
- If calculator shows 0.66666666666666 answer was truncated

### **Conclusion**

- Accurate numerical value cannot be achieved when the number in an expression is rounded off too early

- In practice if a problem requires an answer that is corrected to 3sf we should store the intermediate working values in our calculator or round them off to more SF eg 5 SF
  - This will increase the accuracy of our final answer

### **Estimation**

- Process of guessing value of an unknown quantity

### **Summary**

- 3 situations when approximation is used
  - Actual value known but not used for various reasons eg actual value not necessary, easier to rmb an approximated value, too messy to write a long string of numbers, impossible for calculators to store all digits of non exact number
  - Exact value cannot be obtained
  - Actual value too troublesome/impossible to obtain

## **4. Percentage**

- Natural math extension of fractions, ratio and proportion
- All percentages are expression of relationship based on 100
- Every fraction, ratio and proportion expressed as a percentage
- Percentages also expressed where decimals are required, eg 66.96%
- Calculation of various rates by way of percentages is a backbone of wide range of math applications inc taxes, interest, grades, sports statistics, etc

### **Percentage Change and Reverse Percentage**

- Change in the value of an item expressed as a percentage increase or decrease in the original value
- To calculate the percentage increase, increase in value of a quantity from its original value must be known
- $\text{Increase} = \text{New Value} - \text{Original Value}$
- $\text{Percentage Increase} = \frac{\text{Increase}}{\text{Original Value}} \times 100\%$
- New value can be found using  $\text{New Value} = \text{Original Value} \times (100\% + \text{percentage increase})$
- To calculate percentage decrease,
- $\text{Decrease} = \text{Original Value} - \text{New Value}$
- $\text{Percentage Decrease} = \frac{\text{Decrease}}{\text{Original Value}} \times 100\%$
- $\text{New Value} = \text{Original Value} \times (100\% - \text{Percentage Decrease})$

### **Percentage and Percentage Point in practical situations**

#### **Profit and Loss**

- Goods produced at a certain cost, when they are sold at a price higher than cost price a profit is made
- When goods are sold at a price lower than the cost price a loss is made
- $\text{Profit} = \text{Selling price} - \text{Cost price}$

- $\text{Loss} = \text{Cost price} - \text{Selling price}$
- Profit or loss usually expressed as a percentage of the cost price
- $\text{Profit (or loss)} / \text{cost price} \times 100\%$
- Note in some cases profit or loss can be expressed as a percentage of the selling price

### **Discount**

- Items sold at lower price (sale price)
- Difference between original selling price, or marked price and sale price is called discount
- $\text{Discount} = \text{Marked Price} - \text{Sale Price}$
- Similarly discount often given as percentage of marked price
- $\text{Discount} / \text{marked price} \times 100\%$
- In general sales price also found using  $\text{Sale price} = \text{Marked price} \times (100\% - \text{percentage discount})$

### **GST**

- $\text{Total amount payable} = \text{Marked price} - \text{Discount} + \text{Service Charge} + \text{GST}$
- $\text{Service Charge} = \text{Service Charge (in \%)} \times (\text{Marked price} - \text{Discount})$
- $\text{GST payable} = \text{GST (in \%)} \times (\text{Marked price} - \text{Discount} + \text{Service Charge})$
- Commission is where an agent is paid on buying something for a party

## **5. Ratio and Rate**

- Used to compare 2 or more quantities of the same kind, measured in the same units
- Ratio of a to b is denoted by a:b represented by fraction  $a/b$  where  $b \neq 0$
- In general a ratio is said to be in its simplest form a:b when a and b are integers with no common factors other than 1
- From similar or equivalent ratios can be obtained by multiplying or dividing both parts by the same constant
- $x:y = hx:hy = x/k:y/k$ , where h and k not equal not 0
- $x:y, hx:hy$  and  $x/k:y/k$  equivalent ratios
- Using ratios to compare 2 quantities of the same unit is equivalent to using fractions to compare the 2 quantities eg  $a:b=5:7$  equal to  $a/b=5/7$
- Ratios can also be used to represent relationship of more than 2 quantities
- Ratio involving 3 quantities cannot be written as a fraction
- However it can be simplified by multiplying or dividing each term by the same constant

### **Rate**

- Involves 2 quantities and it is a way to measure how one quantity per unit another quantity

- 2 types of rate, constant rate and average rate
- Pulse rate an example of average rate and work wage an example of constant rate

### **Simple interest**

- When money is deposited into a bank the bank will pay interest for the use of money deposited
- Interest in 1 year expressed as a percentage of a deposit called a annual interest rate
- Amount received after a year depends on annual interest rate
- Formula for calculating simple interest is  $I = PRT/100$  where I=interest, P=principal sum, R=rate of interest per annum, T=time or period of loan/deposit
- Note that to obtain total amount=principal+interest

### **Hire purchase**

- Common scenario where a buyer cannot afford to pay the asked price for an item as a lump sum but can afford to pay an initial sum known as deposit, and the rest (loan amount) in monthly repayments known as installments
- Usually buyer has to pay more than the cash price due to interest charged to the balance (cash price-deposit)
- Interest rate is the flat rate as there is no reduction in interest cost after paying off each installment

### **Currency Exchange**

- Exchange rate is the current market price for which one currency can be exchanged for another
- Calculated both on principal amount as well as the accumulated interest over time
- Rates change over time depending on supply and demand
- Refer to sell column if you want to BUY the foreign currency with SGD
- Refer to buy column if you want to SELL the foreign currency for SGD

### **Income Tax**

- If a person's income over a certain amount, he or she has to pay income tax to the government
- Income tax calculated based on tax rate table
- Note rates in the table vary every year
- Chargeable income is total income minus allowable deductions, approved donations and reliefs
- Chargeable income=annual income-tax reliefs

### **Speed**

- Speed of an object defined as distance traveled by the object per unit time
- Special type of rate
- $\text{Speed} = \text{Distance} / \text{Time}$

- Speed of an object indicates how fast its moving
- Expressed in diff units eg m/s,km/h,cm/s etc

### **Conversion of Units of speed**

- Common ones used are km/h and m/s
- Not easy to compare speeds measured in different units
- Recall  $1\text{km}=1000\text{m}$  and  $1\text{h}=60\text{ min}=3600\text{s}$

### **Average speed**

- Object said to be traveled at constant or uniform speed if its speed does not change throughout the journey
- This is unlikely and speed of an object may vary during its course of motion,hence avg speed is calculated
- Average speed is defined as total distance traveled by an object per unit time
- $\text{Average Speed}=\text{Total Distance Traveled}/\text{Total Time}$

## **6. Basic Algebra and Algebraic Manipulation**

- In algebra letters eg x are used to represent numbers and variables
- A variable represents an unknown value
- Algebraic expression involves number and letters connected with operation symbols like +,-,for example  $9x-7$ , $mxn$  are algebraic expressions  
-In the term  $3x$ ,3 is the coefficient of the term x

### **Evaluating Algebraic expressions**

- Evaluating an algebraic expression is the process of finding the value of the expression when its variables are given certain values
- Use common math sense

### **Addition and subtraction of linear terms**

#### **Like terms and unlike terms**

##### **a)Definition:Terms**

- In a algebraic expression,parts separated by the plus and minus signs called terms
- In the expression  $5y-8x+3$ ,the terms are  $5y$ ,- $8x$  and 3

##### **b)Definition:Coefficient**

- The number part,including the sign is called the coefficient of its variable part
- Term  $5y$ , coefficient 5
- Term  $-8x$ , coefficient -8
- When two terms have identical variable parts called like terms,but when two terms have different variable part they are called unlike terms
- For example  $2a$  and  $4a$  are like terms as they contain the same variable part a
- This is regardless of the coefficient they are multiplied with



- On the other hand  $3a$  and  $b/5$  are unlike terms because they contain different unknowns  $a$  and  $b$

### **Simplifying Algebraic Expressions**

- Divide using common factors

### **Addition and subtraction of linear expressions**

- 2 like terms may be combined together when we add or subtract them, for example given two like terms  $2a$  and  $4a$  their sum will give  $6a$
- However given two unlike terms  $2a$  and  $4b$  their sum will give  $2a+4b$  and they cannot be further simplified

### **Substitution**

- Substitute it with a number to obtain an exact value after simplifying

### **Expansion and Factorisation of Linear Expressions**

- In algebraic multiplication and division, we simply express the product of two terms  $a$  and  $b$ , as  $ab$  and their division to be  $a/b$ . In this section, we want to look at the product between a term and a set of algebraic expressions such as  $a(b+c)$

### **Factorisation**

#### **Simplifying using factorisation**

- 3 women were at the market purchasing fruits for a party. They bought a total of 21 apples and 15 pears. They decided to divide the costs equally amongst themselves. Given that each apple costs  $\$x$  and each pear  $\$y$ , find the amount each woman has to pay
- By reversing the distributive law of algebraic expansion, take out the highest common factor of 21 and 15 and form a new expression involving brackets. This process is known as factorisation.
- Answer  $3(7x+5y)$

#### **Factorisation by grouping**

- To factorise an algebraic expression of the form  $ac+ad+bc+bd$ , we should group the four terms into appropriate groups, where the two terms in each group have a common factor. Then we can extract the common factor of each group.
- $ac+ad+bc+bd=(ac+ad)+(bc+bd)=a(c+d)+b(c+d)=(a+b)(c+d)$
- This method is known as factorisation by grouping because we group the four terms into appropriate groups first

### **Linear expression with fractional coefficients**

- In the linear expression  $\frac{2}{3}x + \frac{4}{5}y$ ,  $\frac{2}{3}$  and  $\frac{4}{5}$  are the fractional coefficient of the variables  $x$  and  $y$  respectively
- $a-\frac{1}{2}$  and  $2b-\frac{3}{4}$ , which can be written  $\frac{1}{2}(a-1)$  and  $\frac{1}{4}(2b-3)$  respectively, are the other examples of linear expressions with fractional coefficients.
- The procedure for simplifying linear equations with fractional coefficient is similar to that of simplifying ordinary numerical fractions
- Note when simplifying expressions involving fractions, it is important to ensure that the denominator is the same

- Remember to use brackets when combining two fractions

### **Summary**

- Mathematical operations which have multiple steps can be easily and neatly presented in algebraic terms
- Two terms of the same product of letters are considered like terms
- Constants, which are numbers without any letters, are like terms on their own
- In algebra we use symbols eg  $x$ ,  $p$ , and  $pq$  to represent numbers
- The linear expression  $3x-4+pq+7$  consists of four terms, namely  $3x$ ,  $-4p$ ,  $pq$  and  $7$
- In addition and subtraction of algebraic terms only like terms could be further simplified
- The distributive law of algebraic expression states that  $a(b+c+\dots+z)=ab+ac+\dots+az$  where there can be infinitely many terms in the bracket, in particular  $a(b+c)=ab+ac$
- Factorisation is the process of expressing an algebraic expression as a product of two or more algebraic expressions, it's the reverse of expansion
- Algebraic fractions can be added or subtracted together by having a common denominator

## **7. Linear Equations and Simple Inequalities**

- $3x+5=4$  is a linear equation (highest power of unknown)
- $x^2+3=9x$  is a quadratic equation (sec 2)
- $x^3=27$  is a cubic equation (sec 3)

### **Definition of a linear equation**

- $2c+3=11$  is an equation
- Equal sign means that total value of the left hand side (LHS) of the equation must be the same value as the right hand side (RHS) of the equation (11)
- To solve  $2c+3=11$  means to find the value of  $c$  such that the values on both sides of the equations are equal (LHS=RHS)
- For example if  $c$  is substituted with 3,  $LHS=2(3)+3=9$  not equal RHS
- If  $c$  is substituted for 4,  $LHS=2(4)+3=11=RHS$
- Hence we can say that  $c=4$  satisfies the equation and that  $c=4$  is known as the solution or root of the equation
- A simple equation in one variable (usually  $x$ ) is known as a linear equation in the form  $ax+b=c$  where  $a$ ,  $b$  and  $c$  are constants and  $a$  not equal to 0
- Non linear equations include  $x^2=9$

### **General strategy for solving Linear Equations in one variable**

- If the equations contains a fraction,multiply both sides by the lowest common multiple (LCM) of the denominator(s) to clear the equation of fractions
- Use the distributive property to remove brackets if they occur
- Simplify each side of the equations by combining like terms
- Obtain all variable terms on LHS of the equation,while RHS should contain only numbers
- Solve for the variable
- Check the solution by substituting it into the original equation

### **Solving Fractional Equations**

- A fractional equation is an equation that contains fraction terms
- If the variable is present in the denominator of a term in the equation,it is important to note that solutions cannot include those that will make the denominator zero
- Hence in solving fractional equations, we must check the solutions.

### **Example**

$$x + \frac{x}{4} = 15$$

- $\frac{x}{1} + \frac{x}{4} = 15$
- $4x + \frac{x}{4} = 15$
- $4 \times \frac{5x}{4} = 15 \times 4$
- $5x = 60, x = 12$

### **Applications of linear equations in real world situations**

#### **To solve**

- Understand the problem and identify the unknown quantity
- Use a letter to represent the unknown quantity to be found (eg x)
- Express other quantities in terms of x
- Form an equation based on the given information in the problem
- Solve the equation
- Check if the solution obtained satisfies the conditions of the original problem

### **Mathematical Formulae**

- The area of a rectangle written as a formula is  $A = lb$  or  $A = l \times b$ , where A denotes the area, l denotes the length and b denotes the breadth
- In general a formula expresses a rule in algebraic terms
- It makes use of variables to write instructions for performing a calculation

### **Simple Inequalities**

- Algebraic inequality is expressed when an algebraic expression is separated from a number, variable or another algebraic expression by a greater than sign, less than sign, greater than or equal to sign or less than or equal to sign

- Inequalities can be used to determine upper and lower bounds for a possible range of values, eg the idea that it takes less than 15 min to boil an egg can be expressed as  $t < 15$

#### **Addition and subtraction**

- The addition property of inequalities states that there is no change in an inequality if the same real number is added to both sides of it
- The subtraction property of inequalities states that there is no change in an inequality if the same real number is subtracted from both sides of it

#### **Multiplication and division**

- Multiplication property of inequalities states that there is no change in an inequality if both sides of the inequality are multiplied by the same positive real number
- The multiplication property of inequalities states that there is change in the inequality sign if both sides of the inequality are multiplied by the same negative real number
- The division property of inequalities states that there is no change in an inequality if both sides of the inequality are divided by the same positive real number
- The division property of inequalities states that there is change in inequality sign if both sides are divided by the same real negative number

#### **IN SHORT**

- If  $x > y$  and  $d < 0$  (d negative no) then  $dx < dy$  and  $x/d < y/d$
- If  $x > y$  and  $c > 0$  then  $cx > cy$  and  $x/c > y/c$

## **8. Linear Functions and Graphs**

### **Coordinates**

- The ordered pair  $(a,b)$  are such that  $a$  refers to a point to the horizontal (eastings) axis while  $b$  refers to the point on the vertical (northings) axis
- Quadrant is a part of a graph paper
- $x$  axis is the horizontal axis
- $y$  axis is the vertical axis
- Origin is where 2 axis meet
- Coordinates must be enclosed in brackets

### **Functions and Linear functions**

- Function can be considered as a machine
- Takes an input, applies a rule to it and then produces an output
- Function is a relationship between 2 variables  $x$  and  $y$  such that every input  $x$  produces exactly 1 output  $y$
- Function connecting  $x$  and  $y$  can be represented by an equation of the form  $y = ax + b$  where  $a$  and  $b$  are constants
- The plotted points join to form a straight line

- We say that the function is a linear function eg  $y=2x+1$

### How do we draw graphs of linear functions

- Create a table of values, with a minimum of 3 points
- Draw the axes (limits depend on the x and y values in the table of values)
- Plot the points (make sure each point is being marked out according to the correct sequence of a point which is x coordinate followed by y coordinate)
- Join the points with a straight line, check all points lie on the straight line, if any point does not lie on the line check calculations etc
- Label the graph by writing the equation beside the line

### Gradient

- Measures steepness of a straight line graph
- Positive and Negative gradient
- Positive gradient—as x increases, y increases, it is sloping upwards from left to right
- By definition gradient of a line is the ratio of the vertical change to the horizontal change of a triangle we draw with 2 points on the line
- $\text{Rise/run} = \text{vertical change/horizontal change} = \frac{y_2 - y_1}{x_2 - x_1} = \text{gradient}$
- Also  $y = mx + c$

### Special cases

- Line parallel to x axis (horizontal) gradient = 0
- Line parallel to y axis gradient = undefined

## 9. Number Patterns

- Number sequence is an ordered list of numbers
- Each no. in a sequence is called a term
- Terms usually identified by  $T_1, t_2, t_3$  etc

### General term of a number sequence

- To find any term in a sequence we need to find the general term or the nth term

#### Example

Position n	1	2	3	4	5
Term $t_n$	2	5	8	11	14

Plus 3

Therefore we can express each term as follows

$T_2$	$2+3$	$2+1 \times 3$
$T_3$	$2+3+3$	$2+2 \times 3$

By looking at the term above, we can infer

$$T_n = 2 + (n+1) \times 3$$

$$= 2 + 3n - 3 = 3n - 1$$

### Conclusion

- Nth term of a sequence is called  $T_n$ /general term of the sequence
- By substituting suitable values of  $n$ , every term in a sequence could be generated
- $T_n = a + n \times b$  where  $a$  is the common difference +  $b$  where  $b$  is the zeroth term

## 10. Basic Geometry

- Point (no dimension, no size)
- Line segment (part of line by joining 2 points A and B, infinite number of points)
- Line (infinite number of points, no width, indefinite breadth length thickness)
- Ray (part of a line with only 1 endpoint)
- Plane (has a flat surface, has no thickness)

### Types of angles

- Acute angle (measures less than 90 deg)
- Right angle (90 deg)
- Obtuse angle (greater than 90 deg)
- Reflex angle (angle more than 180 deg, less than 360 deg)
- When 2 lines intersect at right angles they are perpendicular to each other

### Complementary and supplementary angles

- Adjacent angles (angles sharing a vertex and common side)
- Complementary angles (2 angles summing up to 90 deg)
- Supplementary angles (2 angles summing up to 180 deg)
- Note: Overlapping angles are not adjacent angles

### Properties of angles formed by intersecting lines

Properties	Abbreviation
Sum of adjacent angles on a straight line is 180 deg	Adj angles on a st line
Sum of all angles at a point is 360 deg	Angles at a point
When 2 lines intersect, the vertically opp angles are equal	Vert opp angles

### Properties of angles formed by parallel lines and transversal

#### Parallel lines

- 2 lines on the plane
- Do not intersect

#### Transversal

- Line cuts/intersects other line

### More angle properties

- When a transversal intersects a pair of parallel lines, 3 types of angles are formed
- Corresponding angles-corr angles (parallel lines C)
- Alternate angles-alt. Angles (Z)
- Interior angles-int. Angles

## 11. Polygons and Geometrical Constructions

### Triangles

- Can be classified according to sides and angles

#### Sides

Desc	3 sides with diff length	2 sides of equal length	3 sides of equal length
Name	Scalene triangle	Isosceles triangle	Equilateral triangle

#### Angles

Desc	All angles less than 90deg	1 angle=90deg	1 angle >90deg, but less than 180deg
Name	Acute triangle	Right angled tri	Obtuse angled tri

### Angle properties of triangles

Properties	Abbreviation
Base angles of isosceles triangle are equal	Base angles of isos. Triangle
Each angle is 60deg	Angles of equilateral triangle
Angle sum of a triangle is 180	Angle sum of triangle
Exterior angle of tri = to sum of interior angles	Ext. angle of triangle

### Quadrilaterals

- All plane figures with 4 sides and 4 angles are quadrilaterals

### Trapezium

- Has at least one pair of parallel sides

### Square

- Has 2 pairs of parallel sides

- Far sides equal
- Has 4 right angles
- Opposite angles equal
- Equal diagonals
- Perpendicular to each other
- Bisect each other (cut into 2 equal parts)
- Bisect interior angles

### **Rhombus**

- 2 pairs of parallel side
- 4 sides equal
- Opposite angles are equal
- Perpendicular to each other
- Bisect each other
- Bisect interior angles

### **Rectangle**

- Has 2 pairs of parallel sides
- Opposite sides are equal
- 4 right angles
- Opposite angles are equal
- Equal diagonals
- Diagonals bisect

### **Parallelogram**

- Has 2 pairs of parallel sides
- Opposite sides are equal
- Opposite angles are equal
- Diagonals bisect each other

### **Kite**

- 2 pairs of equal adjacent sides
- Opposite sides may or may not be parallel
- Must cut each other @right angles
- 1 diagonal bisects the interior angles

### **For Constructing lines (parallel or perpendicular)**

- Draw arcs
- No arcs no marks

### **Perpendicular bisector**

- Bisector cuts something into 2 equal parts
- Line which is perpendicular to and divides the line segment into two equal parts

### **Angle Bisector**

- Line drawn from vertex of the angle such that it divides the angle into smaller angles
- Any point along the angle bisector of an angle has equal perpendicular distances from the arms of the angle



### **Interior and exterior angles of a polygon**

- One interior and one exterior angle = 180 degrees
- Sum of interior angles of a regular n-sided polygon =  $(n-2) \times 180$  (angle sum of polygon)
- Size of each interior angle of regular n sided polygon =  $(n-2) \times 180 / n$  (angle sum of polygon)
- Sum of exterior angles of a polygon = 360 degrees (exterior angle sum of polygon)

## **12. Pythagoras Theorem**

### **Introduction**

- $a^2 + b^2 = c^2$
- $a^2 + b^2$  squared root = c
- Longest side of a right angle triangle is called the hypotenuse (side vertically opposite the right angle)

### **Converse of the Pythagoras Theorem**

- If the square of the longest side is equal to the sum of the squares of the other two sides then the opposite the longest side is a right angle
- Given Triangle ABC, computing  $AC^2 = \text{finding } AB^2 + BC^2$ , if  $AC^2 = AB^2 + BC^2$ ,  $\angle C = 90$  degrees

## **13. Perimeter and Area of Plane Figures**

### **Formulas**

- Area of square =  $x^2$  where x = length of a side
- Perimeter of square =  $4x$
- Area of rectangle =  $l \times b$  where l = length and b = breadth
- Perimeter of rectangle =  $l + b + l + b = 2(l + b)$
- Area of triangle =  $\frac{1}{2}bh$  where b = base and h = height
- Perimeter of triangle =  $a + b + c$
- Area of circle =  $\pi \times \text{radius} \times \text{radius}$
- Circumference =  $2 \times \pi \times \text{radius} = \pi \times \text{diameter}$  where diameter =  $2 \times \text{radius}$
- Area of Parallelogram =  $b \times h$
- Perimeter of parallelogram = sum of 4 sides
- Area of Trapezium =  $\frac{1}{2} \times h \times (a + b)$
- Perimeter of Trapezium = Sum of 4 sides

## **14. Volume and Surface Area of Prism and Cylinder**

### **Nets**

- Show surface area of the solids
- Area determined by looking at the shape of the surface
- Volume refers to the space occupied by the solid
- Given that the side of the cube is  $x$  cm, volume of cube  $= x^3$
- $6x^2$
- Volume of cuboid  $= l \times b \times h$
- Surface area of Cuboid  $= 2x(lb+lh+bh)$

#### **Volume and Surface area of Prism**

- Top and bottom of the prism is called base of the cuboid
- Bases are parallel to each other and are identical rectangles
- Any horizontal cross section of the cuboid is parallel to them and is also a rectangle identical to them
- Cuboid has uniform cross section
- Volume of prism  $=$  base area  $\times$  height
- Surface area of prism  $=$  perimeter of base  $\times$  height  $+ (2 \times$  Base area)

#### **Volume and surface area of Cylinder**

- Uniformed Cross section
- Volume of cylinder  $=$  Base Area  $\times$  Height  $= \pi \times r^2 \times$  height
- Surface area of closed cylinder  $= 2 \times \pi \times$  radius  $\times$  height  $+ 2 \times \pi \times$  radius

### **15. Volume and Surface Area of other Polygons**

- Volume of Pyramid  $= \frac{1}{3} \times$  Base area  $\times$  Height
- SA of Pyramid  $=$  Add areas of triangle (x4) and base
- Volume of Cone  $= \frac{1}{3} \times \pi \times$  radius<sup>2</sup>  $\times$  height
- SA of Cone  $= \pi \times$  radius  $\times$  slanted height  $+ \pi \times$  radius<sup>2</sup>
- Volume of Sphere  $= \frac{4}{3} \times \pi \times$  radius<sup>3</sup>
- SA of Sphere  $= 4 \times \pi \times$  radius<sup>2</sup>

### **16. Linear Graphs and Simultaneous Linear Equations**

- Linear equations in 2 unknowns  $x$  and  $y$  is an equation of the form where  $a, b, c$  are numbers and  $a$  and  $b$  are not both zero
- A pair of simultaneous linear equations in 2 variables can be solved by:
  - 1) Elimination
  - 2) Substitution
  - 3) Graphical, where point of intersection is the solution
- A pair of simultaneous linear equations has an infinite number of solutions if the graphs of the two equations are identical
- A pair of simultaneous linear equations has no solution if the graphs of the two equations are parallel

