

Answer all the questions.

- 1 An isosceles triangle ABC has a length $AB = AC = (5p - 2q)$ cm and $BC = (3p + q)$ cm. Find the perimeter of triangle ABC in terms of p and q .

$$\begin{aligned} \text{perimeter} &= 2(5p - 2q) + 3p + q \quad \text{--- (M1)} \\ &= 10p - 4q + 3p + q \\ &= (13p - 3q) \text{ cm.} \end{aligned}$$

[A4:]

$$\begin{aligned} \text{Perimeter} &= 5p - 2q + 5p - 2q + 3p + q \quad \text{--- cm} \\ &= (13p - 3q) \text{ cm} \# \end{aligned}$$

Answer ... $13p - 3q$... cm [2] (M)

- 2 If $3(x - y)^2 = 51$ and $xy = 21$, find the value of $x^2 + y^2$.

$$\begin{aligned} 3(x^2 - 2xy + y^2) &= 51 \quad \text{(M1): correct expansion.} \\ x^2 - 2xy + y^2 &= 17 \\ x^2 - 2(21) + y^2 &= 17 \quad \text{--- (M1)} \\ x^2 + y^2 &= 17 + 42 \\ &= 59 \# \end{aligned}$$

$$\begin{aligned} [A4:] \\ 3(x^2 - 2xy + y^2) &= 51 \quad \text{[M1]: expansion} \\ 3x^2 - (xy + xy) &= 51 \\ 3x^2 - 6(21) + 3y^2 &= 51 \quad \text{--- [M1]} \\ 3x^2 + 3y^2 &= 51 + 126 \\ 3x^2 + 3y^2 &= 177 \\ x^2 + y^2 &= 59 \# \end{aligned}$$

Answer ... 59 ... (M) [3]

- 3 Expand and simplify each of the following expression.

(a) $(3a-2b)(5a+b)$

$$= 15a^2 + 3ab - 10ab - 2b^2 \text{ --- (M1)}$$

$$= 15a^2 - 7ab - 2b^2 \#$$

Answer $15a^2 - 7ab - 2b^2$ [2]
 L (A1)

(b) $(2x+3y)^2 + 3x^2 - xy$

$$= 4x^2 + 12xy + 9y^2 + 3x^2 - xy \text{ --- (M1) : correct expansion.}$$

$$= 7x^2 + 11xy + 9y^2 \#$$

Answer $7x^2 + 11xy + 9y^2$ [2]
 L (A1)

- 4 (a) Solve the equation $2x^2 + x = 15$.

$2x$	-5	$-5x$
x	3	$6x$
$2x^2$	-15	x

$$2x^2 + x - 15 = 0.$$

$$(2x-5)(x+3) = 0 \text{ --- (M1)}$$

$$2x = 5 \quad \text{or} \quad x = -3 \#$$

$$x = 2\frac{1}{2} \#$$

* Penalise in front under Presentation if student did not write '= 0', 'or.'

Answer $x = 2\frac{1}{2} \text{ or } -3$ [2]
 L (A1) : both correct.

- (b) Hence, solve the equation $4(y-1)^2 + 2(y-1) = 30$.

$$4(y-1)^2 + 2(y-1) = 30$$

$$2(y-1)^2 + (y-1) = 15 \text{ --- (M1)}$$

$$\text{let } x = y-1.$$

$$\therefore \underline{y-1 = 2\frac{1}{2}} \quad \text{or} \quad \underline{y-1 = -3} \text{ --- (M1) : eq.}$$

$$y = 3\frac{1}{2} \# \quad y = -2 \#$$

Answer $y = 3\frac{1}{2} \text{ or } -2$ [3]
 L (A1) : both correct.

- 5 Aqil's father is x^2 years old while Aqil is x years old now. In $5x$ years' time, Aqil's father is twice as old as him.

(a) Form an equation in x and show that it reduces to $x^2 - 7x = 0$.

[2]

$$\begin{aligned} x^2 + 5x &= 2(x + 5x) && \text{--- (M1)} \\ x^2 + 5x &= 12x \\ x^2 - 7x &= 0. \text{ (shown) } \end{aligned} \quad \left. \vphantom{\begin{aligned} x^2 + 5x &= 2(x + 5x) \\ x^2 + 5x &= 12x \\ x^2 - 7x &= 0. \end{aligned}} \right\} \text{ (A1): simplify and show}$$

(b) Solve the equation $x^2 - 7x = 0$.

$$\begin{aligned} x(x-7) &= 0 && \text{--- (M1)} \\ \underline{x=0 \text{ (rej)}} &\text{ or } \underline{x=7} && \text{--- (A1): both solutions must be shown.} \end{aligned}$$

Answer $x = \dots\dots\dots 7 \dots\dots\dots$ [2]

↳ Do not penalise if student also included 0 as an answer.

(c) Hence, find the age of Aqil's father now.

$$\begin{aligned} \text{Age} &= 7^2 \\ &= 49. \end{aligned}$$

Answer $\dots\dots\dots 49 - \text{(B1)} \dots\dots\dots$ years old [1]

6 Factorise each of the following expressions completely.

(a) $2x^3 - 50x$

$$= 2x(x^2 - 25) \text{ --- (M1)} \quad \left. \begin{array}{l} \\ \end{array} \right\} \begin{array}{l} * a^2 - b^2 = (a+b)(a-b) \\ \\ \end{array}$$

$$= 2x(x+5)(x-5) \quad \#$$

Answer ... $2x(x+5)(x-5)$ [2]
 L (A1)

(b) $6y^2 + 9y - 42$

$$= 3(2y^2 + 3y - 14) \text{ --- (M1)}$$

$2y$	7	$7y$
y	-2	$-4y$
$2y^2$	-14	$3y$

$$= 3(2y+7)(y-2) \quad \#$$

[A4]:

$$6y^2 + 9y - 42 = \underline{(3y-6)(2y+7)} \text{ --- [M1]}$$

$$= \underline{3(y-2)(2y+7)} \quad \#$$

Answer ... $3(2y+7)(y-2)$ [2]
 L (A1)

(c) $2ax - 5bx + 15by - 6ay$

$$= x(2a - 5b) + 3y(5b - 2a) \text{ --- (M1)}$$

$$= x(2a - 5b) - 3y(2a - 5b)$$

$$= (x - 3y)(2a - 5b) \quad \#$$

Answer ... $(x-3y)(2a-5b)$ [2]
 L (A1)

- 7 The variable x and y are connected by the equation $y = 2x^2 + 6x - 3$. Some values of x and the corresponding values of y are given in the table.

x	-4	-3	-2	-1	0	1
y	5	-3	p	-7	-3	5

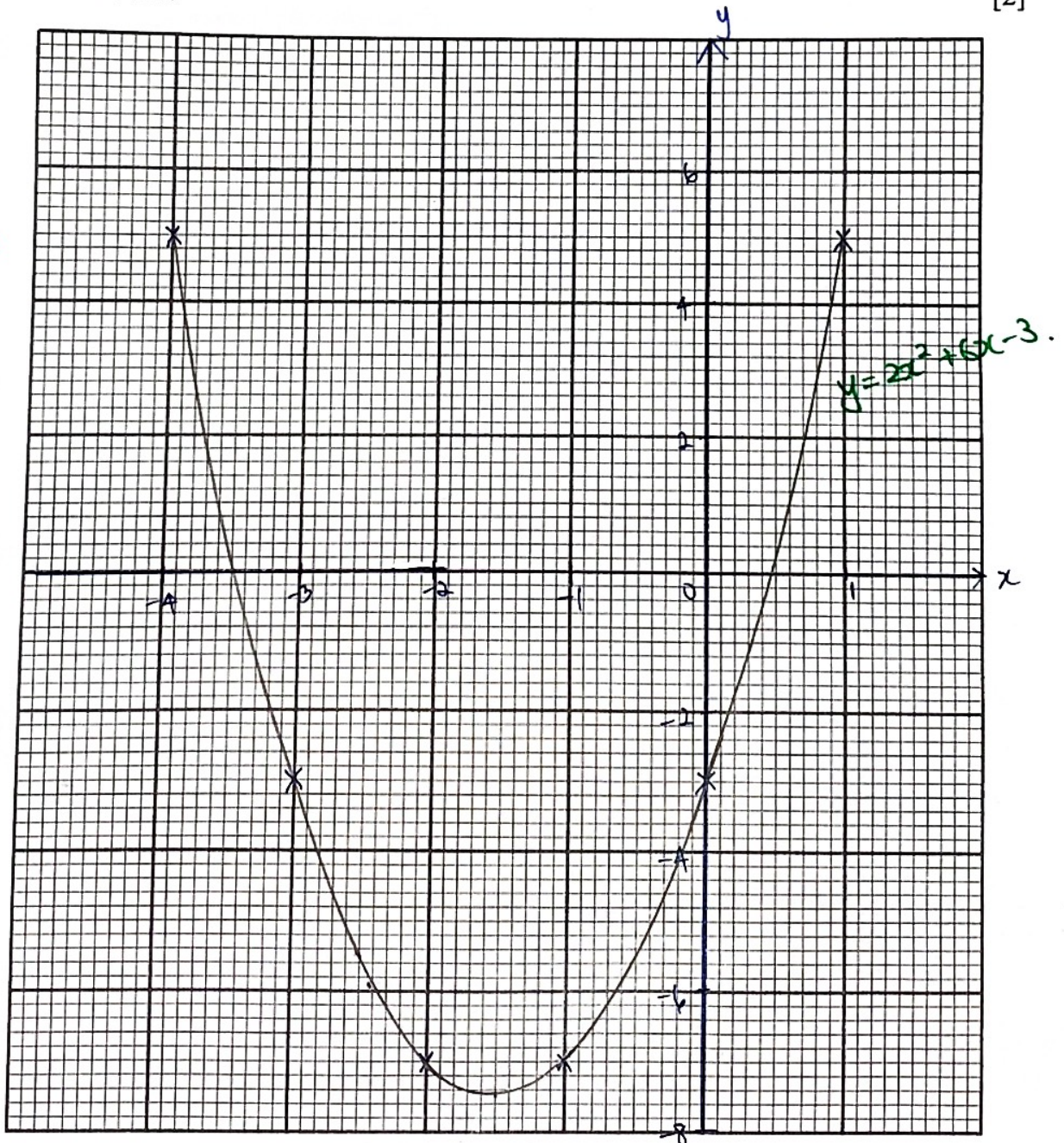
- (a) Find the value of p .

$$p = 2(-2)^2 + 6(-2) - 3$$

$$= -7$$

Answer $p = \dots -7 \dots$ [1]

- (b) On the graph grid below, using a scale of 2 cm to represent 1 unit on the x -axis and 1 cm to represent 1 unit on the y -axis, draw the graph of $y = 2x^2 + 6x - 3$ for $-4 \leq x \leq 1$. [2]



(M1): correct scale
(A1): correct plots
+ smooth curve.

(c) Use your graph in (b) to find

(i) the value of y when $x = -2.5$

Answer $y = \dots -5.5 (\pm 0.2) [1]$ — (B1)
 $(-5.7, -5.6, -5.4, -5.3)$.

(ii) the equation of the line of symmetry of the graph

Answer $\dots x = -1.5 (\pm 0.1) [1]$ — (B1)
 $(-1.4, -1.45, -1.55, -1.6)$.

END OF PAPER