

SECONDARY 4 PRELIMINARY EXAMINATION MATHEMATICS

Paper 1

4048/01

1 September 202	0 (Tuesday)		2 hour	rs
CANDIDATE NAME				
CLASS	INDEX NUMBER			
READ THESE I	NSTRUCTIONS FIRST	For F	xaminer	's Use
	the page until you are told to do so.	Q1	2	5 030
Write your name.	class and index number in the spaces above.	Q2	2	
	e or black pen in the space provided.	Q3	2	
		Q4	2	
You may use a pe	encil for any diagrams or graphs.	Q5	2	
Do not use staple	s, paper clips, glue or correction fluid.	Q6	3	
		Q7	3	
INFORMATION	N FOR CANDIDATES	Q8	3	
Answer all the qu		Q9	3	
_		Q10	3	
If working is need	ded for any question it must be shown with the answer.	Q11	3	
0 ' ' ' C	vi-1 viin a will marelt in loss of marks	Q12	4	<u> </u>
Omission of essential working will result in loss of marks.		Q13	4	
The use of on	annroyed scientific calculator is expected where	Q14	4	
The use of an approved scientific calculator is expected, where appropriate.		Q15	4	
appropriate.		Q16	4	
If the degree of	accuracy is not specified in the question, and if the	Q17	5	
	ct, give the answer to three significant figures.	Q18	5	
	degrees to one decimal place.	Q19	5	
	1	Q20	5	
For π , use either	er your calculator value or 3.142, unless the question	Q21	6	
	ver in terms of π .	Q22	6	
•		Total	/	80
each question or	marks is given in brackets [] at the end of part question. of marks for this paper is 80.			

This document consists of $\underline{21}$ printed pages including the Cover Sheet.

4048 MATHEMATICS O LEVEL (2016)

MATHEMATICAL FORMULAE

Compound interest

Total amount =
$$P\left(1 + \frac{r}{100}\right)^n$$

Mensuration

Curved surface area of a cone = πrl

Surface area of a sphere = $4\pi r^2$

Volume of a cone = $\frac{1}{3}\pi r^2 h$

Volume of a sphere $=\frac{4}{3}\pi r^3$

Area of triangle $ABC = \frac{1}{2}ab \sin C$

Arc length = $r\theta$, where θ is in radians

Sector area $=\frac{1}{2}r^2\theta$, where θ is in radians

Trigonometry

$$\frac{a}{\sin A} = \frac{b}{\sin B} = \frac{c}{\sin C}$$

$$a^2 = b^2 + c^2 - 2bc\cos A$$

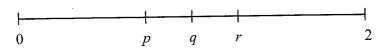
Statistics

$$Mean = \frac{\sum fx}{\sum f}$$

Standard deviation =
$$\sqrt{\frac{\sum fx^2}{\sum f} - \left(\frac{\sum fx}{\sum f}\right)^2}$$

Answer all the questions.

1 The numbers p, q and r are represented on the number line.



The values of p, q, and r are listed below.

$$\left(-\frac{2}{3}\right)^0$$
 $\frac{\pi}{2}$ $\frac{5}{8}$ $\sqrt{5}$

(a) Find p, q and r.

Answer
$$p = \dots$$
 $q = \dots$ $q = \dots$ [1]

(b) Write down the irrational number(s).

4	Г13
Answer	 [1]

2 A Shinkansen train 273 m long passes through a tunnel 2 km long. The average speed of the train is 240 km/h.

Calculate the time taken for the train to pass through the tunnel completely. Give your answer in seconds.

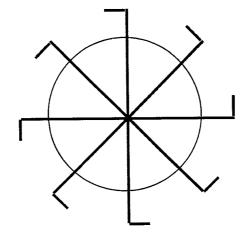
Answerseconds [2]

3 It is given that $w = \frac{4a - 3b}{b + c}$.

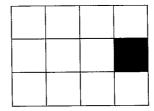
Express b in terms of w, a and c.

Answer
$$b = \dots$$
 [2]

4 (a) The diagram shows a simplified view of a waterwheel.

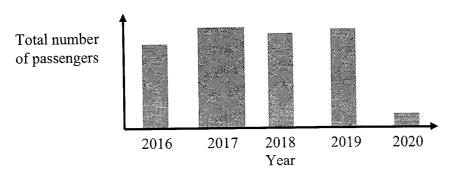


(b) Shade one more square on the diagram, such that the diagram has two lines of symmetry.



[1]

5 The chart shows the total number of passengers at Changi Airport in the years 2016 to February 2020.



State one feature of the chart that may be misleading and explain why.

.....

.....

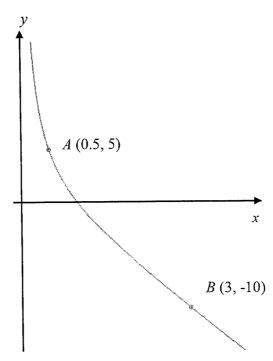
[2]

- 6 Simplify
 - $(a) a^2b \times a^{-2}b^5,$

Answer [1]

Answer[2]

7 The sketch below shows the graph of $y = \frac{p}{x} + qx + 1$. The points A(0.5, 5) and B(3, -10) lie on the graph. Find the values of p and q.

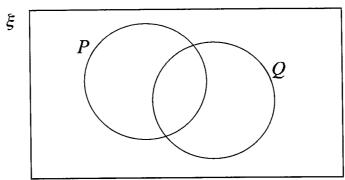


Answer $p = \dots$ [3]

- 8 $\xi = \{\text{integers } x: 1 \le x \le 20\}$
 - $P = \{\text{prime numbers}\}\$
 - $Q = \{\text{multiples of 3}\}\$
 - (a) List the element(s) in $P \cap Q$.
- Answer[1]
- (b) Circle the correct statement from the list below.
 - 0 0 DI / (OI
 - $P \subset Q$ $Q \cap P' \neq \phi$
- $(Q \cup P)' = \{1\}$

[1]

(c) On the Venn diagram, shade the region that represents $P \cup Q'$.



[1]

9 Jen wants to buy a vacuum cleaner costing \$480.

Covey Norm departmental store has a payment plan for customers to pay a deposit of \$100 and then 24 monthly payments, each of 4% of the original cost of the vacuum cleaner.

How much more than the original cost will Jen pay if she uses the payment plan?

Answer \$......[3]

10 The scale drawing in the answer space below shows a piece of land ABCD.

The owner of the land decides to use part of the land to build a nursery based on the following requirements:

- (i) The nursery is closer to the line AB than AD
- (ii) The nursery is closer to the point D than C

By constructing an angle bisector and a perpendicular bisector, shade the area of the land where the nursery will be built.

Answer

A

C

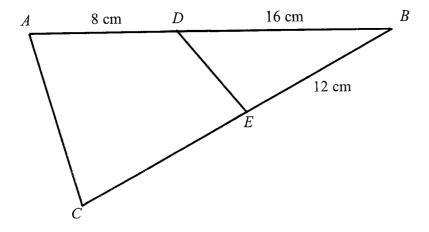
Sketch the graph of $y = 9 - (x - 1)^2$ on the axes below. Indicate clearly the coordinates of the points where the graph crosses the axes and the maximum point on the curve.

Answer

[3]

12 In the diagram D and E are points on AB and BC respectively such that angle BDE = angle BCA.

BD = 16 cm, DA = 8 cm and BE = 12 cm.



(a) Show that triangle BDE and triangle BCA are similar.

Answer (a) In triangle BDE and triangle BCA	
	[2]

(b) Hence, find EC.

Answer
$$EC = \dots$$
 [2]

			11		
13	(a)	(i)	Express 84 as the product of its prime fac	tors.	
			Answer		[1]
		(ii)	The number $\frac{84h}{g}$ is a perfect square. h and g are prime numbers such that $h < g$. Find the value of h and the value of g.	g.	
			Answer	h = g =	[1]
	(b)		two numbers, except 360 and 24, that have and a highest common factor of 24.	a lowest common multiple of	

Answer [2]

14	Factorise completely

		2
(a)	2ax-x-a+2x	_
(a)	$\Delta u x - x - u + \Delta x$	

	ro1
Answer	 [2]

(b) $4y^3 - 16yx^2$.

Answer[2]

15	A polygon has n sides. Two of its exterior angles are 21° and 54° . The remaining exterior angles are 15° each. Find				
	(a)	the value of n ,			
				÷	
	·	•.	Answer	<i>n</i> =	[2]
	(b)	the sum of interior angles of the polygo	on.		
			Answer		[2]

16	(a)	4 skilled workers can complete a job in 5 days. 5 semi-skilled workers can
		complete the same job in 6 days. How long does it take 1 skilled worker and
		1 semi-skilled worker to complete the same job if they work together?

(b) It is given that y is directly proportional to the square of x and y = p for a particular value of x. Express y in terms of p when this value of x is halved.

Answer
$$y = \dots$$
 [2]

17	The 1	The ratio of the base areas of two geometrically similar cylinders is 9:25.				
	(a)	If the surface area of the smaller cylinder is 480 cm ² , what is the surface area of the larger cylinder?				
	-	Answer cm ²	[2]			
	(b)	Find the ratio of the heights of the two cylinders.				
		Answer	[1]			
	(c)	Both cylinders are filled with silica. The mass of the silica in the larger cylinder is 36 kg. Find the mass of silica in the smaller cylinder.				
		<i>Answer</i> kg	[2]			

18	A is the point	(3, 2)	and B is the point	(9, -1)
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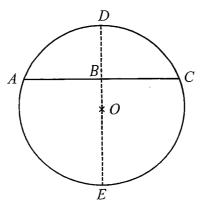
(a) Find the length of the line AB.

Answerunits [2]

(b) Find the equation of the straight line that is parallel to AB, and passes through point C(-4, 0).

Answer[3]

The diagram shows a circle, centre O, radius 16 cm. B is the mid-point of the chord AC, DE is a diameter and BE = 25 cm.



(a) Calculate angle AOC in radian.

4	[2]
Answer	 F-1

(b) Hence, find the area of the segment *ABCE*.

The time taken to complete a task by two groups of students, Group 1 and Group 2, were recorded.

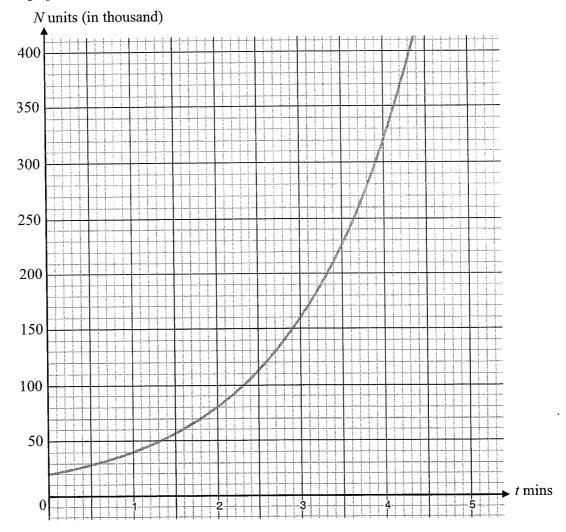
The results are shown in the dot diagram.

Time (in hours) taken to complete a task

				•								
min.		•	TOTAL SAFE SAFE SAFE SAFE SAFE SAFE SAFE SAFE	Inner philatric and page		gir ka luntan nam	kilikasa yang op <u>op</u> any	man sangguna sang			● Group 1	
0	1	2	3	4	5	6 ○	7	8	9	10	O Group 2	
		0		0		0	0					
				0			0					
a)	Write do	own the	e media	n time t	aken b	y Grouj	o 1.					
						Ai	nswer			•••••	hours	[1]
(b)	Write de	own the	e range	of the t	ime tak	cen by C	Group 2	•				
						A	nswer				hours	[1]
(c)		e taken									e range of e? Justify	
[b	ecause							•••••	
										•••••		[2]
(d)	Whicl					onsister				er.		
Answ												
												[1]

The number of bacteria, N units (in thousand), in a food item after t minutes, are connected by the equation $N = 40(2^{t-1})$.

The graph $N = 40(2^{t-1})$ is drawn on the grid below.



(a) Use the graph to estimate the range of values of t such that 80 < N < 320.

Answer	 [1]

(b) (i) By drawing a tangent, find the gradient of the curve at (1, 40).

Answer[2]

	(ii)	Hence, state what the tangent at (1, 40) represents.
Answ	ver	[1]
	(iii)	The food item is not safe to be consumed when the number of bacteria is at least 800% from its original amount.
		Using the graph, determine after how long the food item is no longer safe to be consumed.
	·	
		Answermin [2]

In the diagram, ABC represents a horizontal triangular garden.

CB = 5 m.

Angle ACB = 64° and the bearing of A from B is 280°.

N

B

Calculate the bearing of B from A.

Answer

'a [1]

(b) A vertical tree, BT, has its base at B.

The angle of depression of the point C when viewed from the top of the tree is 24°.

(i) Find the height of the tree.

(ii) David measured the largest angle of elevation of the top of the tree as seen from the path AC.Calculate this angle of elevation.

Answer ° [3]

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·		
•		



PRELIMINARY EXAMINATION SECONDARY 4

MATHEMATICS Paper 1		4048/01
1 September 2020 (Tuesday)		2 hours
CANDIDATE SOLUTION NAME		
CLASS INDEX NUMBER	[]	
READ THESE INSTRUCTIONS FIRST	For Ex	For Examiner's Use
Do not turn over the page until you are told to do so.	<u>Q</u> 1	2
Write your name, class and index number in the spaces above.	02	2
Write in dark blue of mack pen in the space province.	3 6	2
You may use a pencil for any diagrams or graphs.	05	2
Do not use staples, paper clips, glue or correction fluid.	Q,	3
	07	3
INFORMATION FOR CANDIDALES	96	w
and the second of the second o	Q10	3
If working is needed for any question it thust be shown with the answer.	01	. 3
Omission of essential working will result in loss of marks.	013	4 4
Ž,	014	4
	015	4
	Q16	4 د
If the degree of accuracy is not specified in the gression, and it is	Q18	5
Cive answers in degrees to one decimal place.	Q19	5
City of the case o	Q20	5
For π , use either your calculator value or 3.142, unless the question	021	6
requires the answer in terms of π .	022	6
"the manufact of marks is critical in branchets [] at the end of		Yanan ayayaya da ayaya da ay
stion.		

This document consists of 21 printed pages including the Cover Sheet.

The total number of marks for this paper is 80.

4048 MATHEMATICS O LEVEL (2016)

MATHEMATICAL FORMULAE

Compound interest

Total amount =
$$P\left(1 + \frac{r}{100}\right)^n$$

Mensuration

Curved surface area of a cone = nrl

Surface area of a sphere = 4πr²

Volume of a cone
$$=\frac{1}{3}\pi r^2 h$$

Volume of a sphere $=\frac{4}{3}m^3$

Area of triangle
$$ABC = \frac{1}{2}ab\sin C$$

Are length =
$$r\theta$$
, where θ is in radians

Sector area $=\frac{1}{2}r^2\theta$, where θ is in radians

Trigonomeny

$$\frac{a}{\sin A} = \frac{b}{\sin B} = \frac{c}{\sin C}$$

$$a^2 = b^2 + c^2 - 2bc\cos A$$

Statistics

$$Mean = \frac{\sum fx}{\sum f}$$

Standard deviation =
$$\sqrt{\frac{\sum fx^2}{\sum f} - \left(\frac{\sum fx}{\sum f}\right)^2}$$

Answer all the questions.

-	The numbers p , q and r are represented on the number line.	
	0 p q r 2	andrew a desire
	The values of p , q , and r are listed below.	
	$\binom{-2}{3}$ $\frac{\pi}{2}$ $\frac{5}{8}$ $\sqrt{5}$	
	= 1.57	
	(a) Find p , q and r .	
	Answer $p=\frac{5}{8}$	
	$q = \left(-\frac{2}{3}\right)^0$	
m additional for con-	$r=rac{\pi}{2}$	[1]
	(b) Write down the irrational number(s).	
	Answer $\frac{\pi}{2}$ and $\sqrt{5}$	Ξ
2	A Shinkansen train 273 m long passes through a tunnel 2 km long. The average speed of the train is 240 km/h. Calculate the time taken for the train to pass through the tunnel completely.	
	Give your answer in seconds.	
	Time Taken = $\frac{2+\frac{273}{1000}}{240}$.	***************************************
	$= \frac{2 + \frac{273}{1000}}{240} \times 60 \times 60$ $= 34.095 \text{ s}$	
	Answer 34.095 seconds	[2]

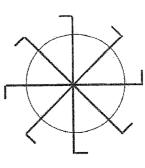
			ربن
$Ancwor = \frac{4q - cw}{w + 3}$	$w = \frac{4a - 3b}{b + c}$ $w(b + c) = 4a - 3b$ $b(w + c) = 4a - cw$ $b = \frac{4a - cw}{w + 3}$	Express b in terms of w , a and c .	It is given that $w = \frac{4a - 3b}{b + c}$.
[2]			

The diagram shows a simplified view of a waterwheel.

(Jn

The chart shows the total number of passengers at Changi Airport in the years 2016

to February 2020.



3 State the order of rotational symmetry.

Answer8..... Ξ

Ξ

3 Shade one more square on the diagram, such that the diagram has two lines of

> of passengers Total number 2016 2017 2018 Year 2019 2020

State one feature of the chart that may be misleading and explain why.

- Features & reason

 1. No values or scale on the vertical axis (if it starts from 0 or not) opened to misinterpretation as to total number of passengers. OR Exaggerates the
- differences between the years.

 2017 has a different width it is not clear whether the width or the height of the bar should be read as the total number of passenger movement.

 2020 bar implies the entire year while information given states up to February 2020 distortion or misrepresentation of information.

[2]

(a) $a^2b\times a^{-2}b^5$,

Ξ

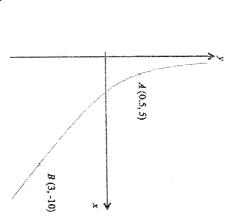
€

 $\left(\frac{27}{x^{18}}\right)^{\frac{-1}{3}}.$

Answer
$$\left(\frac{3}{x^6}\right)^{-1} or \frac{x^6}{3}$$

$$ar \frac{x^6}{3}$$
 [2]

The sketch below shows the graph of $y = \frac{p}{x} + qx + 1$. Find the values of p and q. The points A(0.5, 5) and B(3, -10) lie on the graph.



$$5 = \frac{p}{0.5} + 0.5q + 1$$

$$5 = 2p + 0.5q + 1$$

$$10 = 4p + q + 2$$

$$4p + q = 8 - (1)$$

$$-10 = \frac{p}{3} + 3q + 1$$

$$-30 = p + 9q + 3$$

$$p + 9q = -33$$

$$p = -33 - 9q - (2)$$
Sub (2) into (1)
$$4(-33 - 9q) + q = 8$$

$$-132 - 36q + q = 8$$

$$-132 - 35q = 8$$

$$-132 - 35q = 8$$

$$-132 - 35q = 8$$

$$35q = -140$$

$$q = -4$$
Sub $q = -4$ into (2)
$$p = -33 - 9(-4)$$

$$p = -33 - 9(-4)$$

$$p = 3$$



Turn over

 $\xi = \{\text{integers } x : 1 \le x \le 20\}$

30

- $P = \{\text{prime numbers}\}\$ $Q = \{\text{multiples of 3}\}\$
- **(2)** List the element(s) in $P \cap Q$.
- $P = \{2,3,5,7,11,13,17,19\}$ $Q = \{3,6,9,12,15,18\}$

 $P\cap Q=\{3\}$

Answer 3 or $\{3\}$

Ξ

ਭ

 $P \subset Q$

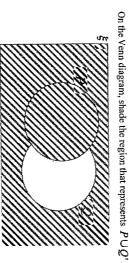
 $O \cap P' \neq \phi$.

 $(\mathcal{Q} \cup P)' = \{1\}$

Ξ

Circle the correct statement from the list below.

Ĉ



Turn over

Turn over

Ŷ Jen wants to buy a vacuum cleaner costing \$480. Covey Norm departmental store has a payment plan for customers to pay a deposit

of \$100 and then 24 monthly payments, each of 4% of the original cost of the vacuum cleaner.

How much more than the original cost will Jen pay if she uses the payment plan?

Total cost from offer

$$$100 + $480 \times \frac{4}{100} \times 24 = $560.80$$

Difference
$$$560.80 - $480 = $80.80$$

0

[3]

The owner of the land decides to use part of the land to build a nursery based on the following requirements: $\frac{1}{2} \int_{\mathbb{R}^{n}} \frac{1}{2} \int_{\mathbb{R}^{n}} \frac$

The nursery is closer to the line AB than AD. The nursery is closer to the point D than C.

By constructing an angle bisector and a perpendicular bisector, shade the area of the land where the nursery will be built.

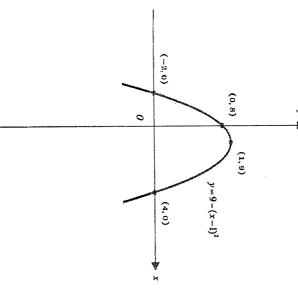
Answer E b

! Sketch the graph of $y = 9 - (x - 1)^2$ on the axes below. Indicate clearly the coordinates of the points where the graph crosses the axes and the maintum point on the curve.

Answer

=

12



[23

12 angle BDE =angle BCA. In the diagram, D and E are points on AB and BC respectively such that BD - 16 cm, DA = 8 cm and BE = 12 cm. 8 cm Ö

16 cm

12 cm

(a) Show that triangle BDE and triangle BCA are similar.

Answer (a) In triangle BDE and triangle BCA

Angle DBE = Angle CBA (is a common angle)

Angle BDE = Angle BCA (given)

Angle BED = Angle BAC (angles sum of triangle)

Therefore, Triangle BDE is similar to triangle, BCA (AA test)

[2]

9 Hence, find EC.

 $\frac{BC}{BD} = \frac{BA}{BE}$ $\frac{12 + EC}{16} = \frac{24}{12}$ EC = 20

Turn over

Answer EC =20.....cm

[2]

<u>.</u>

(B) Ξ Express 84 as the product of its prime factors.

13

Answer \dots , $2^2 \times 3 \times 7$...

Ξ

 \equiv The number $\frac{84h}{g}$ is a perfect square. h and g are prime numbers such that h < g.

Find the value of h and the value of g.

g=.....7....

$$360 = 2^{3} \times 3^{2} \times 5$$
$$24 = 2^{3} \times 3$$

€

Find two numbers, except 360 and 24, that have a lowest common multiple of

360 and a highest common factor of 24.

$$23 \times 32 \times 50 = 72$$
$$23 \times 3 \times 5 = 120$$

Answer72...., [2]

> 4 Factorise completely

 $2ax-x-a+2x^2.$

Method 1 $2ax - x - a + 2x^2$ $=2ax-a-x+2x^2$

= a(2x-1)+x(-1+2x)= (2x-1)(a+x)

Method 2 $2ax - x - a + 2x^2$

 $= 2\alpha x + 2x^2 - x - a$ = 2x(a+x) - (x+a)= (2x-1)(a+x)

Answer (2x-1)(a+x)

 $\overline{2}$

9 $4y^{3} - 16yx^{2}.$ $4y^{3} - 16yx^{2}$ $= 4y(y^{2} - 4x^{2})$ $= 4y(y^{2} - 2x)(y + 2x)$

Answer ... 4y(y-2x)(y+2x)

[2]

Turn over

- 5 A polygon has n sides. Two of its exterior angles are 21° and 54°. The remaining exterior angles are 15° each. Find (a) the value of n,

Sum of exterior angles = 360°

$$21^{\circ} + 54^{\circ} + (n-2)15 = 360^{\circ}$$

 $n = 21$

Answer
$$n = \dots 21 \dots 21$$

2

Ξ

the sum of interior angles of the polygon.

sum of interior angles
$$= (21-2)180^{\circ}$$

$$= 3420^{\circ}$$

16 (a) 4 skilled workers can complete a job in 5 days. 5 semi-skilled workers can I semi-skilled worker to complete the same job if they work together? complete the same job in 6 days. How long does it take 1 skilled worker and

$$\left(\frac{1}{20} + \frac{1}{30}\right)^{-1} = 12$$

1/30 inverse relation

9 It is given that y is directly proportional to the square of x and y = p for a particular value of x. Express y in terms of p when this value of x is halved.

Answer12.....days

[2]

 $y = \hbar x^2$

$$p = kx^{2}.$$

$$p = k\left(\frac{x}{2}\right)^{2}$$

$$p = \frac{k(\frac{x}{2})^{2}}{4}$$

$$p = \frac{kx^{2}}{4}$$

Answer
$$y = \frac{1}{4}p$$
 [2]

The ratio of the base areas of two geometrically similar cylinders is 9:25.

17

(a) If the surface area of the smaller cylinder is 480 cm², what is the surface area of the larger cylinder?

 A_s surface area of smaller cylinder A_L surface area of larger cylinder

$$\frac{480}{x} = \frac{9}{25}$$

$$= 1330 \text{ cm}^2 (3)$$

$$x = 1333\frac{1}{3}$$

= 1330 cm² (3 s.f)

Answer1330...... cm²

2

h_s height of smaller cylinderh_L height of larger cylinder

$$\frac{h_{\perp}}{h_{\perp}} = \sqrt{\frac{A_{\perp}}{A_{\perp}}} = \sqrt{\frac{9}{25}} = \frac{3}{5}$$
or

$$\frac{h_L}{h_s} = \sqrt{\frac{A_L}{A_s}} = \sqrt{\frac{25}{9}} = \frac{5}{3}$$

c Both cylinders are filled with silica. The mass of the silica in the larger cylinder is 36 kg. Find the mass of silica in the smaller cylinder.

$$\frac{m_{S}}{m_{L}} = \left(\frac{3}{5}\right)^{3}$$

$$m_{\rm g} = \left(\frac{3}{5}\right)^3 \times 36$$
$$= 7.776 \text{ kg}$$

$$=7.776 \text{ kg}$$

Answer7.776.....kg [2]

Turn over

- Ç A is the point (3, 2) and B is the point (9, -1).
- (a) Find the length of the line AB.

Length AB =
$$\sqrt{(9-3)^2 + (-1-2)^2}$$

= $\sqrt{45}$
= 6.7082 = 6.71 units (3 s.f)

(b) Find the equation of the straight line that is parallel to AB, and passes through point C(-4,0).

Answer6.71.....units

2

Gradient_{AB} =
$$\frac{-1-2}{9-3}$$

= $\frac{-3}{6}$ = $-\frac{1}{2}$

$$y = -\frac{1}{2}x + c$$
Sub $C(-4, 0)$

$$y = -\frac{1}{2}x + c$$

$$Sub C(-4, 0)$$

$$0 = -\frac{1}{2}(-4) + c$$

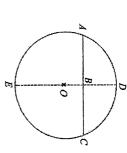
$$c = -2$$

$$y=-\frac{1}{2}x-2$$

Answer ...
$$y = -\frac{1}{2}x - 2$$

19

5



- B Calculate angle AOC in radian.
- $AOC = 2\cos^{-1}\frac{9}{16}$ = 1.94678 = 1.95 (3 s.f) $\cos B OC = \frac{9}{16}$ $\overset{\wedge}{BOC} = \cos^{-1} \frac{9}{16}$
- Answer1.95..... [2]

Hence, find the area of the segment ABCE.

3

Reflex angle
$$AOC = 2\pi - 2\cos^{-1}\frac{9}{16}$$

= 4.336405

Area of segment ABCE

$$=\frac{1}{2}\Big(16^2\Big)\Big(4.336405-\sin 4.336405\Big)$$

$$= 674.1186$$

= $674 \text{ cm}^2 (3 \text{ s.f})$

 Ξ

Turn over

20

20 The time taken to complete a task by two groups of students, Group 1 and Group 2, were

The results are shown in the dot diagram

Time (in hours) taken to complete a task

		0				
		0		•	•	
	•	() N		•		
		⊕ ω		*	•	
0	0	4 (6)	and the second	•	•	•
		(J)		•	•	
	0	⊕ 6				
•	0	0 7				
		œ				
		9		•		
		10				
		10 @Group 2	Group 1			

- 3 Write down the median time taken by Group 1.
- Answer4..... hours Ξ
- € Write down the range of the time taken by Group 2.
- Answer6...... hours Ξ
- <u></u> Alice claims that Group 2 took a shorter time to complete the task as the range of your answer. the time taken by Group 2 is shorter than that of Group I. Do you agree? Justify
- because Group 1 has an extreme value which will affect the range of Group 1. Hence, it is not fair/ accurate to claim that Group 2 took a shorter time based on the range.... [2]
- 3 Which group's timing was more consistent? Justify your answer.

Answer (d) Group1..'s timing was more consistent because the interquartile range of Group 1. 3 hours, is less than that of Group 2. 4 hours.

Alternative solution:

Group 2's timing was more consistent because the standard deviation of Group 2 is 2.06 hours (3 s.f) which is less than that of Group 1's 2.14 hours.

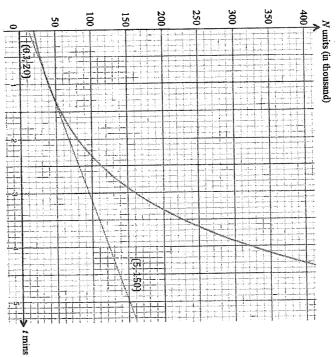
Turn over

Ξ

21

21 The number of bacteria, N units (in thousand), in a food item after t minutes, are connected by the equation $N = 40(2^{t-1})$.

The graph $N = 40(2^{t-1})$ is drawn on the grid below.



(a) Use the graph to estimate the range of values of i such that 80 < N < 320.

Answer
$$2 < t < 4$$
 [1]

(b) (i) By drawing a tangent, find the gradient of the curve at (1, 40).

Gradient =
$$\frac{150-20}{5-0.3}$$

= 27.7 (±0.5 i.e 27.2 \(\sigma\) gradient \(\sigma\) 28.2)

23

(ii) Hence, state what the tangent at (1, 40) represents.

Answer The tangent represents the rate of change/ growth/ increase of the number of bacteria in the food after 1 mins or after/ at r = 1 min...

Ξ

(iii) The food item is not safe to be consumed when the number of bacteria is at least 800% from its original amount.

be consumed. At t = 0, N = 20 (can be read from graph)

Using the graph, determine after how long the food item is no longer safe to

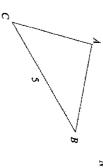
$$800\% \times 20 = \frac{800}{100} \times 20 = 160$$

time = 3 min

Solving of t-values using algebraic method is not acceptable.

22 In the diagram, ABC represents a horizontal triangular garden.

Angle $ACB = 64^{\circ}$ and the bearing of A from B is 280°



a Calculate the bearing of B from A, Bearing = $280^{\circ} - 180^{\circ} = 100^{\circ}$ OR

Bearing = $180^{\circ} - (360^{\circ} - 280^{\circ}) = 100^{\circ}$

Answer100...... Ξ

(b)

A vertical tree, BT, has its base at B.

The angle of depression of the point C when viewed from the top of the tree is 24°.
(i) Find the height of the tree.
Height of cliff = 5 tan 24°.

= 2.23 m=2.22614Answer2.23...... [2]

(ii) David measured the largest angle of elevation of the top of the tree as seen from the path AC.

Calculate this angle of elevation.

 $\sin 64^\circ = \frac{\text{shortest distance}}{5}$

shortest distance = 5sin 64° = 4.49397

Let the largest angle of elevation be θ .

 $\tan\theta = \frac{5\tan 24}{5\sin 64}$

 $\theta = 26.35208$

 $=26.4^{\circ} (1 d.p)$

End of Paper

Answer26.4

[3]



MATHEMATICS PAPER 2 SECONDARY 4 2020 PRELIMINARY EXAMINATION

4048/2

2	Sej	ptember	2020	(Wednes	day)
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2 hours 30 minutes

CANDIDATE NAME			
CLASS INDEX NUMBER			
READ THESE INSTRUCTIONS FIRST	For Ex	aminer	's Use
Do not turn over the page until you are told to do so.	Q1	10	5 0 5 0
Write your name, class and index number in the spaces above. Write in dark blue or black pen in the space provided for each question.	Q1	10	
	Q2	4	
You may use a pencil for any diagrams or graphs. Do not use paper clips, highlighters, glue or correction fluid.	Q3	5	
	Q4	6	
INFORMATION FOR CANDIDATES Answer all the questions.	Q5	9	
If working is needed for any question it must be shown with the answer.	Q6	8	
Omission of essential working will result in loss of marks.	Q7	10	
The use of an approved scientific calculator is expected, where	Q7 Q8	 8	
appropriate.	Q ₀		-
If the degree of accuracy is not specified in the question, and if the answer is not exact, give the answer to three significant figures.	Q9	9	
Give answers in degrees to one decimal place.	Q10	10	
For π , use either your calculator value or 3.142, unless the question	Q11	11	
requires the answer in terms of π .	Q12	10	
The number of marks is given in brackets [] at the end of each question or part question.	Total		/100
The total number of marks for this paper is 100.			

Mathematical Formulae

Compound Interest

Total amount =
$$P\left(1 + \frac{r}{100}\right)^n$$

Mensuration

Curved surface area of a cone = πrl

Surface area of a sphere = $4\pi r^2$

Volume of a cone =
$$\frac{1}{3} \pi r^2 h$$

Volume of a sphere =
$$\frac{4}{3} \pi r^3$$

Area of triangle
$$ABC = \frac{1}{2}ab \sin C$$

Arc length = $r\theta$, where θ is in radians

Sector area =
$$\frac{1}{2}r^2\theta$$
, where θ is in radians

Trigonometry

$$\frac{a}{\sin A} = \frac{b}{\sin B} = \frac{c}{\sin C}$$

$$a^2 = b^2 + c^2 - 2bc \cos A$$

Statistics

$$Mean = \frac{\sum fx}{\sum f}$$

Standard deviation =
$$\sqrt{\frac{\sum fx^2}{\sum f} - \left(\frac{\sum fx}{\sum f}\right)^2}$$

Answer all questions.

1 (a) Solve the equation $\frac{a^2}{7} = \frac{a}{3}$.

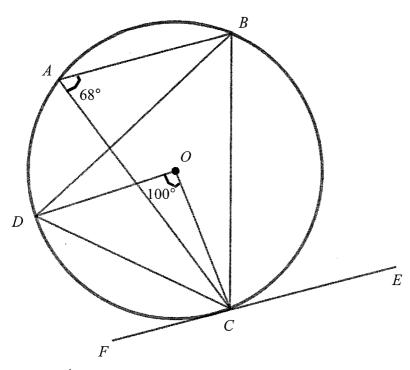
(b) Solve the inequalities $-2 < \frac{7x+3}{2} \le 3-x$.

(c) Express $\frac{6}{18d^2 - 30d + 8} + \frac{3}{16 - 9d^2}$ as a single fraction in its simplest form.

Answer [4]

2 In the diagram below, A, B, C and D are points on the circumference of a circle of centre O. FCE is a tangent to the circle at C.

Angle $BAC = 68^{\circ}$ and angle $DOC = 100^{\circ}$



Find, giving reasons for each answer,

(:)	1	~ D	DC
(1)	angl	e D	DC

Answer	 [1]

(ii) angle DCF

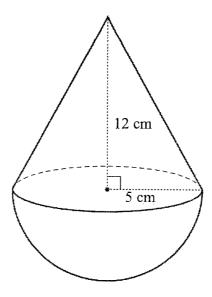
Answer [1]

(iii) angle BDO.

Answer [2]

The diagram shows a solid made up of a cone and a hemisphere. The hemisphere has a radius of 5 cm.

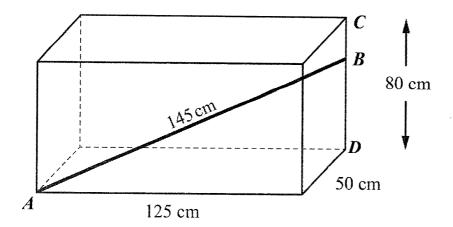
The cone has a base radius of 5 cm and a height of 12 cm.



(a) Calculate the surface area of the solid.

(b) Calculate the volume of the solid.

Answer cm³ [2]



A piece of steel rod AB is placed in a box as shown above. AB is 145 cm. One end of the steel rod, A, is in the bottom corner of the box and the other end of the steel rod, B, is below the top corner of the box.

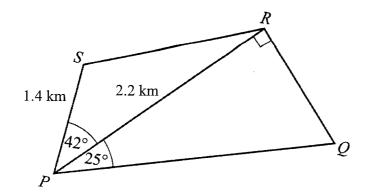
It is given that the box has a height of 80 cm, length of 125 cm and width of 50 cm.

(a) Find the length of BD.

(b) Find the angle ABC.

Answer° [3]

5 The diagram shows a plot of land that is in the shape of a quadrilateral PQRS where PR = 2.2 km and PS = 1.4 km. Angle $PRQ = 90^{\circ}$, angle $RPQ = 25^{\circ}$ and angle $SPR = 42^{\circ}$.



(a) Calculate the length of QR.

Answer	km	[2]
--------	----	-----

(b) Calculate the area of the plot of land.

)	Determine whether it is possible to build a circular fence such that points P , Q , R and S lie on the circumference of a circle. Justify your decision and show your calculations clearly.				
	Answer				
	11160 TO 11111111111111111111111111111111111				
	······································				
	[4				

in the same of the	6	Ben has just relocated	back to	Singapore	from	United	Kingdom.
--	---	------------------------	---------	-----------	------	--------	----------

(a) Ben converted his savings of £50 000 to Singapore dollars when the exchange rate between pounds (£) and Singapore dollars (S\$) was £1 = S\$1.78. Calculate the amount of money in Singapore dollars Ben received after the conversion.

Answer S\$.....[1]

(b) Ben is intending to invest this sum of money in a fixed deposit called the "Multiply Plan" for a period of one year. The interest earned from the "Multiply Plan" is compounded monthly based on the interest rates listed below.

Multip	oly Plan
Interest rate for first six-month period	2% per annum
Interest rate for next six-month period	2.5% per annum (based on total amount at the end of the first six months)

Calculate the total amount of money in Singapore dollars that Ben would have at the end of one year, correct to the nearest cent.

Answer S\$..... [3]

(c) Prior to returning to Singapore, Ben worked out a projected monthly expenditure for living in Singapore.

Rental of a HDB flat	S\$2200
Food	S\$400
Transport	S\$100
Leisure	S\$500

However, he realised that his actual monthly expenditure was different from his projected amount. He has to pay 25% more for rental of a flat, 40% more for food and 30% more for transport than what he had projected.

In order to reduce his monthly expenditure, he decided to cut back his monthly expenses for leisure by 50%.

(i)	Calculate	Ben'	S	actual	monthly	expenditure.
-----	-----------	------	---	--------	---------	--------------

Answer S\$	[2]
------------	-----

(ii) Calculate the percentage increase in Ben's actual expenditure compared to his projected monthly expenses, correcting your answer to 3 significant figures.

1 20 53 41 674	 0/	[2]
Answer	 . /0	[4]

7 A local restaurant has 3 outlets in Bishan, Clementi and Orchard Road.

Each outlet offers 4 different set meals at the following prices.

Set A	Set B	Set C	Set D
\$10	\$12	\$14	\$20

The table below shows the number of set meals sold at the different outlets for the month of January.

Set / Outlet	Bishan	Clementi	Orchard Road
Set A	250	100	300
Set B	100	80	150
Set C	50	30	120
Set D	80	20	100

(a)	Represent the information given in two matrices, a 1×4 matrix, P , and
	a 4×3 matrix, Q .

Answer	P =		[1]	
--------	------------	--	-----	--

$$Q =$$
 [1]

(b) Evaluate PQ.

Answer
$$PQ = \dots [2]$$

(c) Explain what each element in **PQ** represents.

Answei	r	 	 	 			 	
		 	 	 ••••••	•••	•••••	 ••••	
		 	 	 			 	 [1]

In view of the Circuit Breaker which took place in the month of April, the restaurant st	arted a
delivery service in place of dine-in and offered the different set meals at the same price	:_

In the month of April, there was a 20% increase for each type of set meal sold at the outlet in Bishan and a decrease of 40% for each type of set meal sold at the outlet in Orchard Road. The number for each type of set meal sold at the Clementi outlet remained the same in the

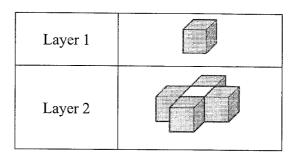
moni	n of April.
	matrix \mathbf{R} , a 3 × 1 matrix, is such PQR gives the total amount of money collected by the outlets in the month of April.
(d)	Write down matrix R .
	Answer $\mathbf{R} = \dots $ [1]
(e)	Evaluate PQR .
(0)	L'valuate I QIV.
	Answer $PQR = \dots [2]$
(f)	Calculate the difference in the total amount of money collected by the restaurant in April compared to January.
	Was there an increase or decrease in the total amount of money collected by the restaurant in April compared to January?
	Answer
	[2]

8 A tower is made of grey and white cubes.

The first layer of the tower is made with one grey cube.



A tower with two layers is made with five grey cubes and one white cube as shown below.



A tower with three layers is made with nine grey cubes and six white cubes as shown below.

Layer 1	
Layer 2	
Layer 3	

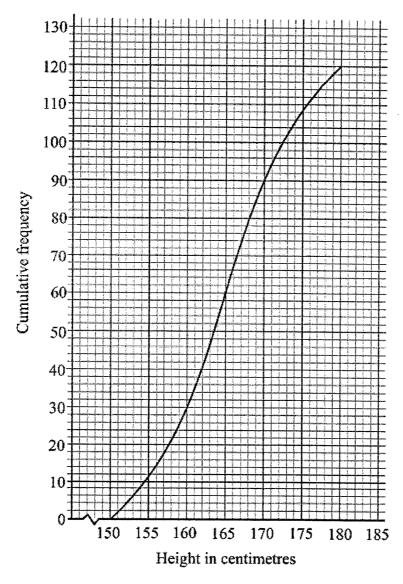
(a) Complete the table below.

Number of layers 1 2 3 4 5 Total number of white cubes 0 1 6 5 Total number of grey cubes 1 9 Total number of cubes 1 6 15

[3]

(b)	Find, in terms of n , the total number of grey cubes in a tower with n layers.	
(c)	Answer Find, in terms of n , the total number of cubes in a tower with n layers.	[1]
	Answer	[1]
(d)	Sarah used 97 grey cubes to build a tower. Calculate the number of white cubes she used.	
	Answer cubes	[3]

9 The graph below shows the heights of 120 Secondary Four students in a school.



(a)	Using the graph,
	(i) write down the median

(ii) find the interquartile range

Answer cm [1]

(b) Given that 40% of the students are taller than x cm, find the value of x.

 $Answer x = \dots [1]$

(c)	The minimum height requirement to join the school's basketball team is 175 cm. If two students are randomly selected, calculate the probability that they meet the height requirement for the school's basketball team.					
			Answer		[2]	
(d)	(i) Complete the frequen	ncy table below.			[2]	
		Height (cm)	Frequency			
		$150 < x \le 155$				
		$155 < x \le 160$				
		$160 < x \le 165$				
		$165 < x \le 170$				
		$170 < x \le 175$:			
		$175 < x \le 180$				
	(ii) Estimate the mean l	neight of the studer	nts.			
			Answer	cm	[1]	
	(iii) Estimate the standa	ard deviation of the	height of students.			
			Answer	cm	[1]	

10 The diagram shows a rectangle PQRS, where PQ = 15 cm and PS = 10 cm.

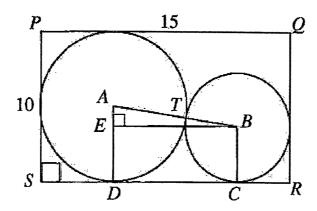
The large circle has a centre A and touches three sides of the rectangle.

The small circle has a centre B and touches two sides of the rectangle.

The small circle touches the large circle at point T.

The large and small circles touch the side \hat{SR} at D and C respectively.

The point E is the foot of the perpendicular from B to AD.



It is given that the radius of the large circle is 5 cm and the radius of the small circle is x cm.

(a)	Write down, in terms of x , an expression for the lengths of
	(i) AB,

	Answer	 [1]
(ii) AE and		
(iii) DC.	Answer	 [1]

Answer [1]

	21	
(b)	Form an equation in x and show that it simplifies to $x^2 - 40x + 100 = 0$.	[3]
(c)	Solve $x^2 - 40x + 100 = 0$, giving your answer correct to 2 decimal places.	
	Answer $x = \dots$ or $x = \dots$	[3]
(d)	Hence, find the radius of the small circle, correct to two decimal places.	

11 The variables x and y are connected by the equation $y = 2x + \frac{4}{x^2} - 5$.

Some corresponding values of x and y, correct to 2 decimal places, are given in the table below.

х	0.75	1	1.5	2	3	4	5	6
у	3.61	1	p	0	1.44	3.25	5.16	7.11

(a) Find the value of p, giving your answer to 2 decimal places.

Answer $p = \dots$ [1]

(b) Using a scale of 2 cm to represent 1 unit, draw a horizontal x-axis for $0 \le x \le 7$. Using a scale of 2 cm to represent 1 unit, draw a vertical y-axis for $-1 \le y \le 8$. On your axes, plot the points given in the table and join them with a smooth curve.

[3]

(c)	Use your graph to find,		
	(i) the least value of y ,		
		<i>Answer y</i> =	[1]
	(ii) the range of values of x for which y is less than	2,	
		Answer	[2]
	(iii) the solutions of the equation $3x^3 = 14x^2 - 8$ by	drawing a suitable straight line.	

12 The most popular ride at the Outer Space amusement park is the Ferris wheel. The diagram below shows a model of the Ferris wheel at the park.



Each day, the Ferris wheel rides run from 10:30 a.m. to 8:30 p.m. with an hour break for maintenance work at 3 p.m.

The Ferris wheel has 16 passenger cabins. There are seats for 3 passengers in each cabin. Due to recent rules on social distancing, it is mandatory to have an empty seat in between two passengers in each cabin.

Before each ride, passengers take about 5 minutes to be seated and undergo safety checks. At the end of each ride, passengers take about 2 minutes to disembark.

The table below shows the ticket prices for one ride on the Ferris wheel for weekdays and weekends. Tickets must be used on the same day of purchase.

Weekday Ticket	\$18
Weekend Ticket	\$23

(a)	Given that the Ferris wheel makes 1 revolution every two minutes and makes
` '	4 revolutions per ride, calculate the total number of rides each cabin on the Ferris
	wheel makes in one day.

Answer rides [2]

(b) Calculate the maximum number of passengers that the Ferris wheel can take in one day.

Answer passengers [1]

(c) If all the seats are taken up for every ride, calculate the total amount of money that the park can collect from the sale of tickets for Ferris wheel rides on a <u>weekday</u>.

Answer \$..... [1]

(d) To commemorate its tenth birthday, the amusement park is planning to give out free tickets for its Ferris wheel rides.

Propose a sensible number of tickets to be given free such that the amount collected from the sale of tickets sales for the day covers its operating cost of \$10 000. It is also estimated that 40% to 60% of the total possible seats will be taken for each ride.

Explain your proposal clearly and state any assumptions made.

(d)

Answer	 	
	 	 [6]

End of Paper

4		



Solutions

	NAME
	CANDIDATE
2 hours 30 minutes	2 September 2020 (Wednesday)
	2020 PRELIMINARY EXAMINATION
	SECONDARY 4
	PAPER 2
4048/2	MATHEMATICS

CLASS

INDEX NUMBER

For Examiner's Use

QI

10

4

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READ THESE INSTRUCTIONS FIRST

Do not turn over the page until you are told to do so. Write your name, class and index number in the spaces above.
Write in dark blue or black pen in the space provided for each question.

You may use a pencil for any diagrams or graphs.

Do not use paper clips, highlighters, glue or correction fluid.

INFORMATION FOR CANDIDATES

Q4 $^{\circ}$ Q2

Answer all the questions.

If working is needed for any question it must be shown with the answer.

Omission of essential working will result in loss of marks.

The use of an approved scientific calculator is expected, where

Q7

10

8 Q_5

00 9

8

If the degree of accuracy is not specified in the question, and if the answer is not exact, give the answer to three significant figures. Give answers in degrees to one decimal place.

For π , use either your calculator value or 3.142, unless the question requires the answer in terms of π .

Q11

=

QIO Q9

10 9

Statistics

The number of marks is given in brackets [each question or part question.] at the end of

The total number of marks for this paper is 100.

Total Q12 5 /100

This document consists of 27 printed pages including the Cover Sheet.

Mathematical Formulae

Compound Interest

Total amount =
$$P\left(1 + \frac{r}{100}\right)^n$$

Mensuration

Curved surface area of a cone = $\pi r l$

Surface area of a sphere = $4m^2$

Volume of a cone =
$$\frac{1}{3} m^2 h$$

Volume of a sphere =
$$\frac{4}{3}m^3$$

Area of triangle
$$ABC = \frac{1}{2}ab \sin C$$

Arc length = $r\theta$, where θ is in radians

Sector area = $\frac{1}{2}r^2\theta$, where θ is in radians

Trigonometry

$$\frac{a}{\sin A} = \frac{b}{\sin B} = \frac{c}{\sin C}$$

$$a^2 = b^2 + c^2 - 2bc \cos A$$

 $Mean = \frac{\sum fx}{\sum f}$

Standard deviation =
$$\sqrt{\frac{\sum f^2}{\sum f}} - \left(\frac{\sum f}{\sum f}\right)^2$$

1 (a) Solve the equation $\frac{a^2}{7} = \frac{a}{3}$. Answer all questions.

$$\frac{a^2}{7} = \frac{a}{3}$$

$$\frac{a^2}{7} = 7a$$

$$3a^2 = 7a = 0$$

$$a(3a - 7) = 0$$

$$a = 0 \quad or \quad a = 2\frac{1}{3}$$

(b) Solve the inequalities $-2 < \frac{7x+3}{2} \le 3-x$.

$$-2 < \frac{7x + 3}{2} \le 3 - x$$

$$-2 < \frac{7x + 3}{2} \quad and \quad \frac{7x + 3}{2} \le 3 - x$$

$$-4 < 7x + 3 \quad and \quad 7x + 3 \le 2(3 - x)$$

$$-4 < 7x + 3 \quad and \quad 7x + 3 \le 6 - 2x$$

$$-7x < 7 \quad and \quad 9x + 3 \le 6$$

$$-x < 1 \quad and \quad 9x \le 3$$

$$x > -1 \quad and \quad x \le \frac{1}{3}$$

$$Ans: \quad -1 < x \le \frac{1}{3}$$

$$-2 < \frac{7x+3}{2} \le 3-x$$

$$-2 < \frac{7x+3}{2} \quad and \quad \frac{7x+3}{2} \le 3-x$$

[2]

(3d-1)(3d-4)(4+3d)

 $= \frac{3}{(3d-1)(3d-4)} = \frac{3}{(3d-4)(4+3d)}$ $= \frac{3(4+3d)-3(3d-1)}{(3d-1)(3d-4)(4+3d)}$ $= \frac{12+9d-9d+3}{(3d-1)(3d-4)(4+3d)}$

 $=\frac{-15}{(4-3d)(3d-1)(4+3d)}$

Alternative solution
$$\frac{6}{18d^2 - 30d + 8} + \frac{3}{16 - 9d^2}$$

$$= \frac{6(16 - 9d^2) + 3(18d^2 - 30d + 8)}{(16 - 9d^2)(18d^2 - 30d + 8)}$$

$$= \frac{6(4 - 3d)(4 + 3d) + 6(3d - 1)(3d - 4)}{2(4 - 3d)(4 + 3d)(3d - 1)(3d - 4)}$$

$$3d)(4+3d)+6(3d-1)(3d-4)$$

$$2(4-3d)(4+3d)(3d-1)(3d-4)$$

$$6(4-3d)[(4+3d)-(3d-1)]$$

6(4-3d)(4+3d)-6(3d-1)(4-3d)

$$\frac{6(4-3d)[(4+3d)-(3d-1)]}{2(4-3d)(4+3d)(3d-1)(3d-4)}$$

$$\frac{15}{[A1]}$$

(3d-1)(3d-4)(4+3d) [A1]

Ĉ Express as a single fraction in its simplest form

$$\frac{6}{18d^2 - 30d + 8} + \frac{3}{16 - 9d^2}$$

[3]

$$\frac{6}{18d^2 - 30d + 8} + \frac{3}{16 - 9d^2}$$

$$\frac{6}{8d^2 - 30d + 8} + \frac{3}{16 - 9d^2}$$

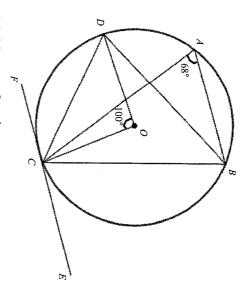
$$\frac{6}{x^2-30d+8} + \frac{3}{16-9d^2}$$

 $\frac{6}{18d^2 - 30d + 8} + \frac{3}{16 - 9d^2}$ $= \frac{6}{2(3d - 1)(3d - 4)} + \frac{3}{(4 - 3d)(4 + 3d)}$

(3d-1)(3d-4) + (4-3d)(4+3d)

4

- In the diagram below, A, B, C and D are points on the circumference of a circle of centre O. FCE is a tangent to the circle at C. Angle $BAC=68^\circ$ and angle $DOC=100^\circ$



Find, giving reasons for each answer, (i) angle DBC,

Angle DBC

 $=\frac{1}{2}$ (angle *DOC*)

= 50° [Angle at the centre is twice the angle at the circumference]

(ii) angle DCF

angle DCF = angle DBC = 50° (angles in alternate segment are equal)

(iii) angle BDO,

Angle ODC

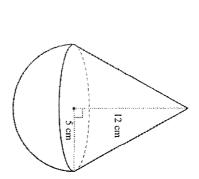
= 180°-100°

= 40° 2

Angle BDC = Angle BAC = 68° (angles in the same segment are equal

Angle BDO
= Angle DBC - Angle PDC
= 68° - 40°
= 28°

3 The diagram shows a solid made up of a cone and a hemisphere. The hemisphere has a radius of 5 cm.
The cone has a base radius of 5 cm and a height of 12 cm.



(a) Calculate the surface area of the solid.

[3]

 $=\sqrt{12^2+5^2}$ Slant height

= 13 cm

Surface area of solid
$$= \left[\pi(5)(13)\right] + \left[\frac{1}{2} \times 4\pi(5)^{2}\right]$$

 $=65\pi + 50\pi$

 $=115\pi \text{ cm}^2$

 $=361 cm^2 (3sf)$

(b) Calculate the volume of the solid.

Volume of the solid
$$= \left[\frac{1}{3} \pi (5)^{2} (12) \right] + \left[\left(\frac{1}{2} \right) \left(\frac{4}{3} \right) \pi (5)^{3} \right]$$

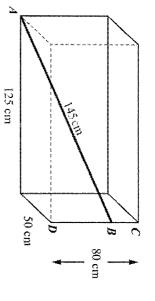
$$= 100 \pi + 83 \frac{1}{3} \pi$$

$$= 183 \frac{1}{3} \pi \quad or \quad \frac{550}{3} \pi \ cm^{3}$$

$$= 576 \ cm^{3} (35)$$

[2]

∞



One end of the steel rod, A, is in the bottom corner of the box and the other end of the steel rod, B, is below the top corner of the box. It is given that the box has a height of 80 cm, length of 125 cm and width of 50 cm. A piece of steel rod AB is placed in a box as shown above. AB is 145 cm.

[3]

(a) Find the length of BD.

By Pythagoras' theorem,

$$(AD)^2 = (DX)^2 + (AX)^2$$

 $(AD)^2 = 50^2 + 125^2$

$$(AD) = 50^{\circ} + 125^{\circ}$$
$$AD = \sqrt{2500 + 15625}$$
$$AD = \sqrt{18125} cm$$

$$(BD)^2 = (AB)^2 - (AD)^2$$

 $(BD)^2 = 145^2 - (\sqrt{18125})^2$

$$BD = \sqrt{21025 - 18125}$$

$$BD = 53.8516$$

$$BD = 53.9 cm (3sf)$$

$$BD = 53.9 cm (3sf)$$

(b) Find the angle ABC.

$$\cos\angle ABD = \frac{BD}{AB}$$

$$\cos\angle ABD = \frac{\sqrt{2900}}{145}$$

$$\angle ABD = \cos^{-1}\left(\frac{\sqrt{2900}}{145}\right)$$

$$\angle ABD = 68.199^{\circ}(3dp) [M1]$$

or
$$\sin \angle ABD = \frac{\sqrt{18125}}{145}$$

 $\angle ABD = 68.199^{\circ} (3dp)$

or
$$\tan \angle ABD = \frac{\sqrt{18125}}{\sqrt{2900}}$$

 $\angle ABD = 68.199^{\circ} (3dp)$

$$\angle ABC = 180^{\circ} - \angle ABD$$

 $\angle ABC = 180^{\circ} - 68.199^{\circ}$
 $\angle ABC = 111.8^{\circ} (1dp)$

Alternative solution

By Pythagoras' theorem,

$$(AC)^{2} = (CD)^{2} + (AD)^{2}$$

$$(AC)^{2} = 80^{2} + (\sqrt{18125})^{2}$$

$$AC = \sqrt{24525} \ cm$$

Using cosine rule,
$$(AC)^{2} = (AB)^{2} + (BC)^{2} - 2(AB)(BC)\cos \angle ABC$$

$$(\sqrt{24525})^{2} = (145)^{2} + (80 - \sqrt{2900})^{2} - 2(145)(80 - \sqrt{2900})\cos \angle ABC$$

$$\cos \angle ABC = \frac{(145)^{2} + (80 - \sqrt{2900})^{2} - (\sqrt{24525})^{2}}{2(145)(80 - \sqrt{2900})}$$

$$\cos \angle ABC = -0.37139$$

$$ABC = 111.8^{\circ} (1db)$$

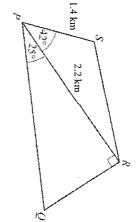
$$\cos \angle ABC = -0.37139$$

\(\angle ABC = 111.8\circ (1dp)\)

[3]

5 The diagram shows a plot of land that is in the shape of a quadrilateral PQRS where PR = 2.2 km and PS = 1.4 km. Angle $PRQ = 90^{\circ}$, angle $RPQ = 25^{\circ}$ and angle SPR = 42° .

10



(a) Calculate the length of QR.

[2]

$$\tan 25^\circ = \frac{QR}{2.2}$$

$$QR = 2.2 \tan 25^\circ$$

$$QR = 1.03 \text{ km } (3s.f.)$$

- *Alternative method: Using Sine Rule
- (b) Calculate the area of the plot of land.

[3]

Area of the plot of land $= \left[\frac{1}{2} (2.2) (2.2 \tan 25^{\circ}) \right] + \left[\frac{1}{2} (1.4) (2.2 \sin 42^{\circ}) \right]$ [M1,M1-subtitution of values into formula for area]

$$=1.12846+1.03046$$

- 3 Determine whether it is possible to build a circular fence such that points P, Q, Rand S lie on the circumference of a circle.

$$\left(PS\right)^{2} = \left(PS\right)^{2} + \left(PR\right)^{2} - 2\left(PS\right)\left(PR\right)\cos \angle SP$$

$$(SR)^{c} = 2.2222 (5sf)$$

$$SR = 1.4907 \, km \, (5sf)$$

$$\frac{\sin \angle PSR}{PR} = \frac{\sin \angle SPR}{SR}$$

$$\angle PSR = 80.936^{\circ}(3dp)$$

$$\angle RQP = 180^{\circ} - 2$$

$$\angle RQP = 65^{\circ}$$

$$\angle PSR + \angle RQP = 80.936^{\circ} + 65^{\circ}$$

- Since $\angle PSR + \angle RQP \neq 180^{\circ}$, points P, Q, R and S do not lie on the circumference
- supplementary or opposite angles in a cyclic quadrilateral add up to 180°).

- <u>∓</u>
- Justify your decision and show your calculations clearly.

$$= (PS)^{2} + (PR)^{2} - 2(PS)(PR)\cos \angle SPP$$

Using cosine rule,

$$(SR)^2 = (PS)^2 + (PR)^2 - 2(PS)(PR)\cos \angle SPR$$

 $(SR)^2 = (1.4)^2 + (2.2)^2 - 2(1.4)(2.2)\cos 42^\circ$

$$\left(\frac{\partial \mathbf{n}}{\partial \mathbf{n}}\right) = 2.2222 \left(\frac{\partial \mathbf{n}}{\partial \mathbf{n}}\right)$$

Using sine rule,

$$\frac{\sin \angle PSR}{PR} = \frac{\sin \angle SPR}{SR}$$

$$\frac{\sin \angle PSR}{2} = \frac{\sin 42^{\circ}}{1.4907}$$

$$\sin \angle PSR = \frac{\sin 42^{\circ}}{1.4907} \times 2.2$$

$$\sin \angle PSR = \frac{\sin 42^{\circ}}{1.4907} \times 2.2$$

$$\angle PSR = 80.936^{\circ} (3dp)$$

$$\angle RQP = 180^{\circ} - \angle PRQ - \angle RPQ$$

$$\angle RQP = 180^{\circ} - 90^{\circ} - 25^{\circ}$$
$$\angle RQP = 65^{\circ}$$

$$\angle PSR + \angle RQP = 145.936^{\circ}$$

- (By the converse of the property that angles in opposite segments are

- Ben has just relocated back to Singapore from United Kingdom.
- \mathfrak{S} conversion. Ben converted his savings of £50 000 to Singapore dollars when the exchange rate between pounds (£) and Singapore dollars (S\$) was £1 = S\$1.78. Calculate the amount of money in Singapore dollars Ben received after the

Ben had S\$89 000 after conversion.

3 Plan" for a period of one year. The interest earned from the "Multiply Plan" is compounded monthly based on the interest rates listed below. Ben is intending to invest this sum of money in a fixed deposit called the "Multiply [3]

2.5% per annum (based on total amount at the end of the first six months)	interest rate for next six-month period
2% per annum	Interest rate for first six-month period
op i mn	1111111

Amount of money Ben has after the first 6 months

the end of one year, correct to the nearest cent.

Calculate the total amount of money in Singapore dollars that Ben would have at

$$= (89000) \left(1 + \frac{\left(\frac{2}{12}\right)}{100} \right)$$
$$= (89000) \left(1 + \frac{1}{600} \right)^{6}$$
$$= (8989893.7166 (4dp))$$

Amount of money Ben has after the next 6 months

$$= (89893.7166) \left(1 + \frac{2.5}{12}\right)^{6}$$

$$= (89893.7166) \left(1 + \frac{1}{100}\right)^{6}$$

$$= (89893.7166) \left(1 + \frac{1}{480}\right)^{6}$$

$$= \$91023.2568 (4dp)$$

$$= \$91023.2568 (2dp)$$

 Leisure	Transport	Food	Rental of a HDB flat
S\$500	S\$100	S\$400	S\$2200

However, he realised that his actual monthly expenditure was different from his projected amount. He has to pay 25% more for rental of a flat, 40% more for food and 30% more for transport than what he had projected.

In order to reduce his monthly expenditure, he decided to cut back his monthly expenses for leisure by 50%.

[2]

(i) Calculate Ben's actual monthly expenditure.

Ben's actual monthly expenditure $= \left[\frac{125}{100} \times 2200 \right] + \left[\frac{140}{100} \times 400 \right] + \left[\frac{130}{100} \times 100 \right] + \left[\frac{50}{100} \times 500 \right]$ = 2750 + 560 + 130 + 250

(ii) Calculate the percentage increase in Ben's actual expenditure compared to his projected monthly expenses, correcting your answer to 3 significant figures. [2]

Total projected expenditure = \$\$2200 + \$\$400 + \$\$100 + \$\$500 =\$\$3200

Percentage increase in his actual expenditure compared to his projected monthly expenses

$$= \frac{3690 - 3200}{3200} \times 100$$
$$= 15.3\% \quad (3s.f.)$$

Turn over

14

7 A local restaurant has 3 outlets in Bishan, Clementi and Orchard Road

Each outlet offers 4 different set meals at the following prices.

\$10	Set A
 \$12	Set B
\$14	Set C
\$20	Set D

The table below shows the number of set meals sold at the different outlets for the month of January.

Set D	Set C	Set B	Set A	Set / Outlet
80	50	100	250	Bishan
20	30	80	100	Clementi
100	120	150	300	Orchard Road

(a) Represent the information given in two matrices, a 1×4 matrix, **P**, and a 4×3 matrix, **Q**.

2

$$P = \begin{bmatrix} 10 & 12 & 14 & 20 \\ 250 & 100 & 300 \\ 100 & 80 & 150 \\ 50 & 30 & 120 \\ 80 & 20 & 100 \end{bmatrix}$$

(b) Evaluate PQ.

[2]

(c) Explain what each element in PQ represents.

Ξ

6000 represents the total amount of money (in dollars) collected from the sales of set meals by the Bishan outlet of the restaurant in the month of January.

2780 represents the total amount of money (in dollars) collected from the sales of set meals by the Clementi outlet of the restaurant in the month of January.

8480 represents the total amount of money (in dollars) collected from the sales of set meals by the Orchard Road outlet of the restaurant in the month of January.

In view of the Circuit Breaker which took place in the month of April, the restaurant started a delivery service in place of dine-in and offered the different set meals at the same price.

number for each type of set meal sold at the Clementi outlet remained the same in the month of Bishan and a decrease of 40% for each type of set meal sold at the outlet in Orchard Road. The In the month of April, there was a 20% increase for each type of set meal sold at the outlet in

The matrix \mathbf{R} , a 3 × 1 matrix, is such PQR gives the total amount of money collected by the three outlets in the month of April.

Ē Write down matrix R.

Ξ

$$R = \begin{bmatrix} 1.2 \\ 1 \\ 0.6 \end{bmatrix}$$

e Evaluate PQR.

[2]

$$PQR = \begin{bmatrix} 6000 & 2780 & 8480 \\ 0.6 \end{bmatrix} \begin{bmatrix} 1.2 \\ 1 \\ 0.6 \end{bmatrix}$$

$$PQR = \begin{bmatrix} 7200 + 2780 + 5088 \end{bmatrix}$$

$$PQR = \begin{bmatrix} 15068 \end{bmatrix}$$

3 Calculate the difference in the total amount of money collected by the restaurant in April compared to January.

restaurant in April compared to January? Was there an increase or decrease in the total amount of money collected by the

[2]

Total amount collected in January = \$6000 + \$2780 + \$8480 = \$17 260

Total amount collected in April = \$15068

= \$17 260 - \$15068 = \$2 192 Difference

There was a decrease in the total amount collected by the restaurant in April.

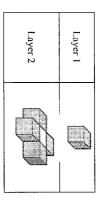
[Turn over

A tower is made of layers of grey and white cubes.

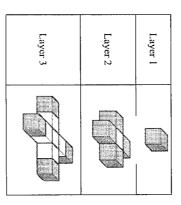
The first layer of the tower is made with one grey cube.



A tower with two layers is made with five grey cubes and one white cube as shown



A tower with three layers is made with nine grey cubes and six white cubes as shown



(E) Complete the table below.

[3]

Total number of cubes	Total number of grey cubes	Total number of white cubes	Number of layers
_	-	0	_
9	5	1	2
6 15 28 45	9	6	3
28	9 13 17	6 15 28	4
45	17	28	5
2n² - n	411 3	(n -1)(2n-3)	n

The graph below shows the heights of 120 Secondary Four students in a school.

(Find, in terms of n, the total number of grey cubes in a tower with n layers.

Ξ

For n = 5, no. of grey cubes = 17 = 1 + 4 + 4 + 4 + 4 + 4 + 4For n = 3, no. of grey cubes = 9 = 1 + 4 + 4For n = 4, no. of grey cubes = 13 = 1 + 4 + 4 + 4For n = 2, no. of grey cubes = 5 = 1 + 4For n = 1, no. of grey cubes = 1

$$= 1 + 4n - 4$$

or
 $= 4n - 3$

= 1 + 4n - 4

Ĉ

â

$$4n = 100$$
 $n = 25$

$$= 1225 - 97$$

= 1128

For n = 2, total no. cubes =
$$6 = 2 \times 3$$

For n = 3, total no. cubes = $15 = 3 \times 5$
For n = 4, total no. cubes = $28 = 4 \times 7$
For n = 5, total no. cubes = $45 = 5 \times 9$
Total no of grey cubes in a tower with n layers = 15×10^{-1} m =

Sarah used 97 grey cubes to build a tower. Calculate the number of white cubes she used.

No. of white cubes used
$$= 1225 - 97$$



Total no of grey cubes in a tower with n layers = 1 + (n-1)(4)

Find, in terms of n, the total number of cubes in a tower with n layers. Ξ





[3]



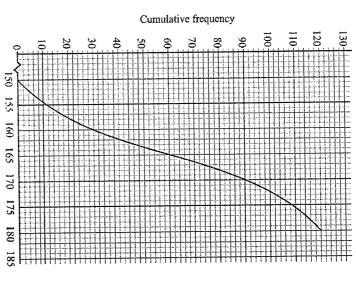
$$= 25 (50 - 1)$$

=1225

$$= 25 (50 - 1)$$

$$= 1225 - 97$$

 $= 1128$



Height in centimetres

(a) Using the graph,

(i) write down the median,

Ξ

Ξ

(ii) find the interquartile range

 $=10 \, \mathrm{cm}$

Given that 40% of the students are taller than x cm, find the value of x.

Ξ

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x = 167

The minimum height requirement to join the school's basketball team is 175 cm. If two students are randomly selected, calculate the probability that they meet the

[2]

height requirement for the school's basketball team.

<u>c</u>

0 The diagram shows a rectangle PQRS, where PQ = 15 cm and PS = 10 cm.

20

The small circle has a centre B and touches two sides of the rectangle. The large circle has a centre Λ and touches three sides of the rectangle. The point E is the foot of the perpendicular from B to AD. The large and small circles touch the side SR at D and C respectively. The small circle touches the large circle at point T.

10 7 2

It is given that the radius of the large circle is 5 cm and the radius of the small circle is x cm.

٥

 $= \frac{12}{120} \times \frac{11}{119}$ $= \frac{11}{1190}$

 $= \frac{11}{120} \times \frac{10}{119}$ $= \frac{11}{1428}$

(i) Complete the frequency table below

Height (cm)

Frequency

(Alternative | (Alternative

Solution)

Solution)

(Alternative Solution) Frequency

Frequency

Frequency

[2]

(a) Write down, in terms of x, an expression for the lengths of

(iii)

EB = DC

EB = SR - SD - CR

EB = 15 - 5 - x

EB = 10 - x

DC = 10 - x

 $175 < x \le 180$

=

12

Ξ

12

(e) Mean (f) SD

7.10 cm (3 sf) 165 cm (3 sf)

7.16 cm (3sf)

7.04 cm

7.10 cm 165 cm (3 sf)

(3sf)

(3sf)

165 cm (3 sf)

165 cm (3 sf)

 $170 < x \le 175$

19

8

19

8

 $165 < x \le 170$

30

30

30

30

(ii) AE = AD - ED AE = 5 - x

(i) AB = 5 + x

 $160 < x \le 165$

30

30

30

30

 $155 < x \le 160$

19

19

18

8

 $150 < x \le 155$

 \equiv

=

12

12

(ii) Estimate the mean height of the students.

Mean height = 165 cm (3 s.f.)

(iii) Estimate the standard deviation of the height of students.

 Ξ

Ξ

Standard deviation = 7.04 cm or 7.10 cm

[Turn over

[3]

(b) Form an equation in x and show that it simplifies to $x^2 - 40x + 100 = 0$.

[3]

$$(AB)^{2} = (AE)^{2} + (EB)^{2}$$

$$(5+x)^{2} = (5-x)^{2} + (10-x)^{2}$$

$$25+x^{2}+10x=25+x^{2}-10x+100+x^{2}-20x$$

$$25+x^{2}-10x+100+x^{2}-20x-25-x^{2}-10x=0$$

$$x^{2}-40x+100=0 (shown)$$

(c) Solve
$$x^2 - 40x + 100 = 0$$
, giving your answer correct to 2 decimal places.

[3]

$$x^{2} - 40x + 100 = 0$$

$$x = \frac{-(-40) \pm \sqrt{(-40)^{2} - 4(1)(100)}}{2(1)} \quad [M1]$$

$$x = 37.3205 \quad or \quad x = 2.67949$$

$$x = 37.32 (2dp) \quad or \quad x = 2.68 (2dp) \quad [A1, A1]$$

(d) Hence, find the radius of the small circle, correct to two decimal places. Radius of the small circle = 2.68 cm (Reject x = 37.32 as as x < 5)

Ξ

11 The variables x and y are connected by the equation $y = 2x + \frac{4}{x^2} - 5$.

Some corresponding values of x and y, correct to 2 decimal places, are given in the table below.

Ų	x
3.61	0.75
pared.	-
p	1.5
0	2
1.44	· ω
3.25	4
5.16	5
7.11	6

(a) Find the value of p, giving your answer to 2 decimal places.

Ξ

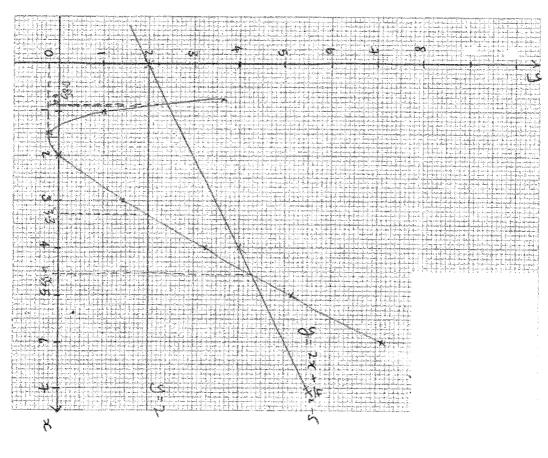
sub x = 1.5,

$$p = 2(1.5) + \frac{4}{(1.5)^2} - 5$$

$$p = -0.22 (2dp)$$

[Turn over

Using a scale of 2 cm to represent 1 unit, draw a horizontal x-axis for $0 \le x \le 7$. Using a scale of 2 cm to represent 1 unit, draw a vertical y-axis for $-1 \le y \le 8$. On your axes, plot the points given in the table and join them with a smooth curve. [3]



Turn over

24

Ĉ Use your graph to find

(i) the least value of y,

Ξ

Least value of $y = -0.24 (\pm 0.1)$

(ii) the range of values of x for which y is less than 2,

[2]

Graph of y = 2 drawn

 $0.9 (\pm 0.1) < x < 3.3 (\pm 0.1)$

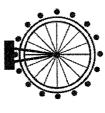
(iii) the solutions of the equation $3x^3 = 14x^2 - 8$ by drawing a suitable straight line.

[4]

 $3x = 14 - \frac{8}{x^2}$ $\frac{3x}{2} = 7 - \frac{4}{x^2}$ $3x^3 = 14x^2 - 8$

Line of $y = \frac{1}{2}x + 2 drawn$

 $x = 0.85 (\pm 0.1)$ or $x = 4.55 (\pm 0.1)$



Each day, the Ferris wheel rides run from 10:30 a.m. to 8:30 p.m. with an hour break for maintenance work at 3 p.m.

Due to recent rules on social distancing, it is mandatory to have an empty seat in between two passengers in each cabin. The Ferris wheel has 16 passenger cabins. There are seats for 3 passengers in each cabin.

checks. At the end of each ride, passengers take about 2 minutes to disembark. Before each ride, passengers take about 5 minutes to be seated and undergo safety

and weekends. Tickets must be used on the same day of purchase The table below shows the ticket prices for one ride on the Ferris wheel for weekdays

Weekend Ticket	Weekday Ticket
\$23	\$18

(a) on the Ferris wheel makes in one day. makes 4 revolutions per ride, calculate the total number of rides each cabin Given that the Ferris wheel makes I revolution every two minutes and [2]

Time taken for 1 ride

= 4 revolutions x 2 minutes

= 8 minutes

 $=\frac{60}{8+2+5} \times 9$ No. of rides per day

Calculate the maximum number of passengers that the Ferris wheel can take Ξ

Ξ

Maximum number of passengers that the Ferris wheel can take a day

= 2 passengers \times 16 cabins \times 36 rides

Turn over

26

rides on a weekday. money that the park can collect from the sale of tickets for Ferris wheel If all the seats are taken up for every ride, calculate the total amount of

[1]

on the Ferris wheel on a weekday. Total amount of money the park can collect from the sale of tickets for rides

 $= 1152 \times 18

<u>a</u> To commemorate its tenth birthday, the amusement park is planning to give out free tickets for its Ferris wheel rides.

[6]

estimated that 40% to 60% of the total possible seats will be taken for each ride. from the sale of tickets sales for the day covers its operating cost of \$10 000. It is also Propose a sensible number of tickets to be given free such that the amount collected

Explain your proposal clearly and state any assumptions made.

Marking Scheme

greater possible free tickets due to higher ticket prices for paid tickets | Stating reasons for decision to give out weekend or weekday tickets.

Eg. Identifying that maximum possible free tickets would be on a weekend due to

Eg. 60% occupancy rate for weekend is a high possibility Eg. 50% occupancy rate as it is the mean between 40% and 60% Stating assumptions related to range of occupancy between 40% to 60%

of \$10 000. Value should be rounded up. Showing calculation for number of paid tickets required to cover operating cost

occupancy rate (subtraction made for the right values) Showing calculation for number of free tickets based on assumption made on

Overall clear explanation and conclusion

	٠
3	٠

nearest whole no.)		nearest whole no.)
(691.2 is rounded down to		(460.8 is rounded up to
=135		[Not possible]
=691-556	=20	=-96
=691.2-556	=576-556	= 460 - 556
$=\left(\frac{60}{100}\times1152\right)-556$	$=\left(\frac{50}{100}\times1152\right)-556$	$=\left(\frac{40}{100}\times1152\right)-556$
No. of free tickets	No. of free tickets	No. of free tickets
60% occupancy	50% occupancy	40% occupancy
Assumption:	Assumption:	Assumption:
	ole no.)	(rounded up to nearest whole no.)
		= 556
		= 555.6
		18
		\$10000
	over operating cost	Max no of paid tickets to cover operating cost
	Weekday Lickets	

	Weekend Lickets	
Max no of paid tickets to cover operating cost	ver operating cost	
\$10000		
23		
= 434.8		-
= 435		
(rounded up to nearest whole no.)	le no.)	
Assumption:	Assumption:	Assumption:
40% occupancy	50% occupancy	60% occupancy
No. of free tickets	No. of free tickets	No. of free tickets
$=\left(\frac{40}{100}\times1152\right)-435$	$=\left(\frac{50}{100}\times1152\right)-435$	$=\left(\frac{60}{100}\times1152\right)-435$
= 460.8 - 435	=576-435	=691.2-435
= 461 - 435	=141	=691-435
= 26		= 256
(460.8 is rounded up to		(691.2 is rounded down to
nearest whole no.)		nearest whose no.)