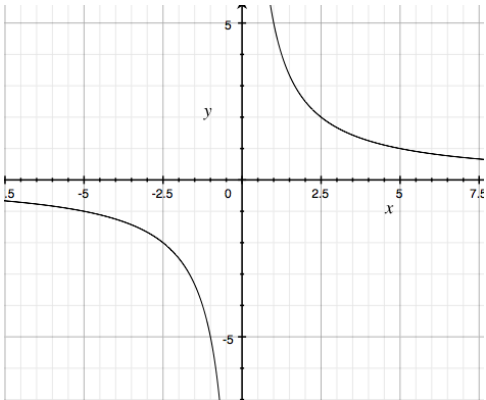
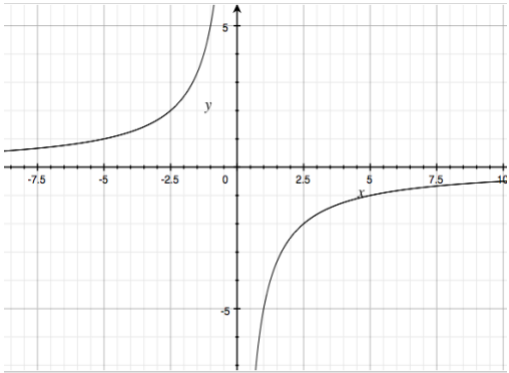
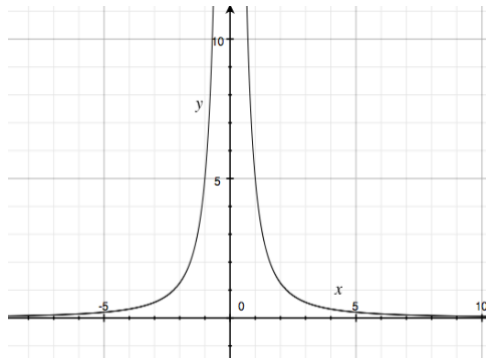
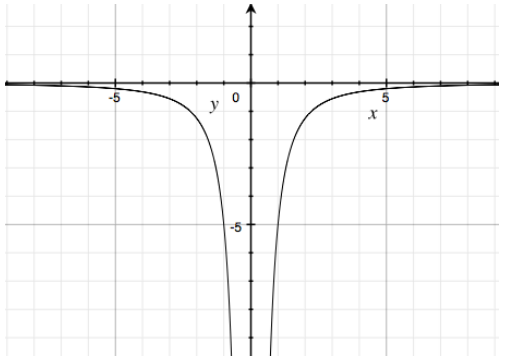
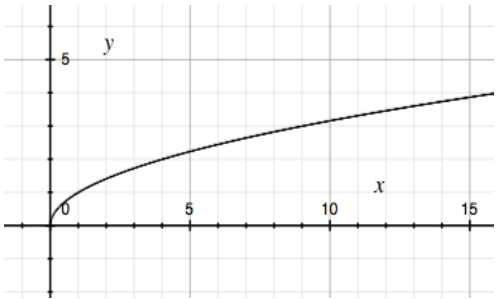
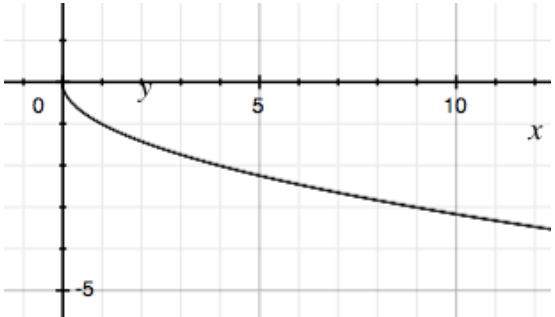
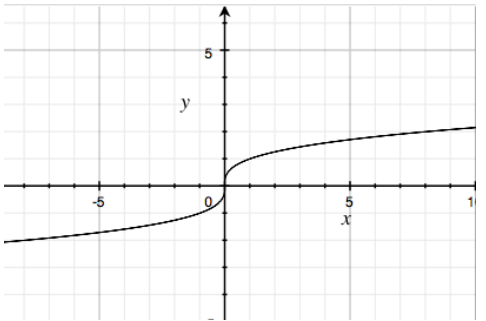
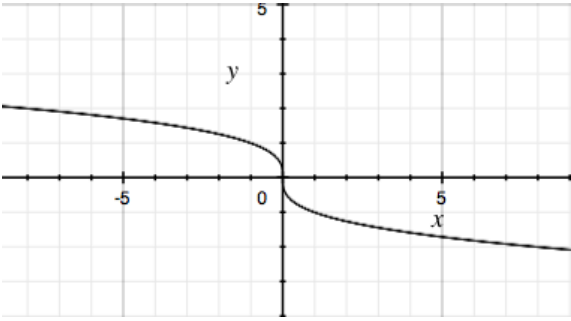
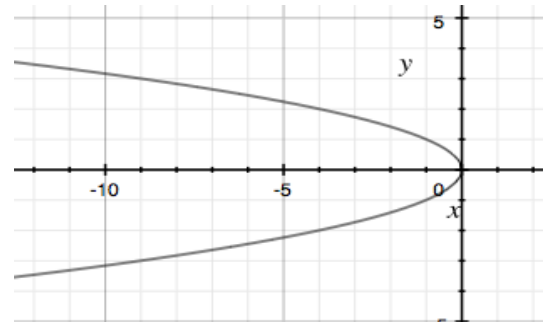
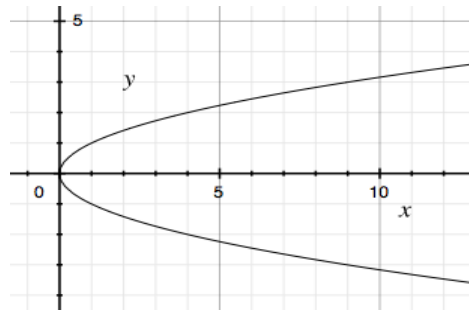


| Equation | If $a > 0$ | If $a < 0$ |
|---|---|--|
| $y = \frac{a}{x}$ <p>Asymptote: $x = 0$ $y = 0$</p> |  |  |
| $y = \frac{a}{x^2}$ <p>Asymptote: $x = 0$ $y = 0$</p> |  |  |
| $y = ax^{\frac{1}{2}}$ |  |  |
| $y = ax^{\frac{1}{3}}$ |  |  |
| | | |

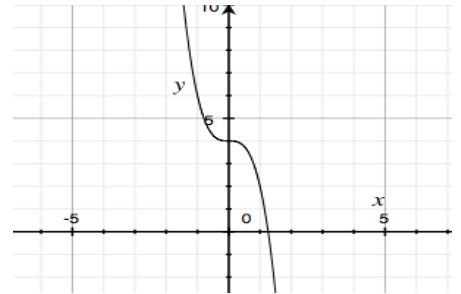
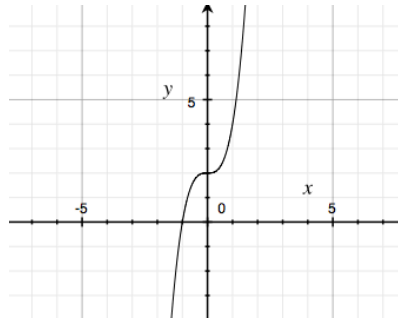
$$y^2 = ax$$



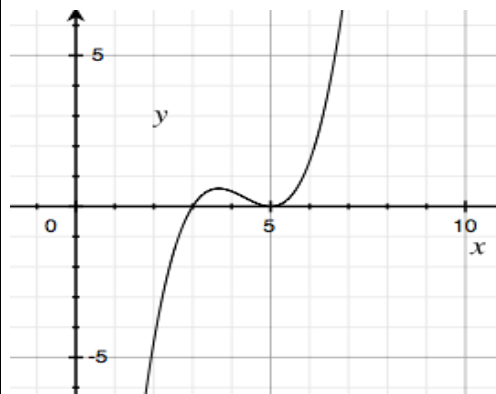
$$y = ax^3 + d$$

y intercept = (0, d)

x intercept = $(\sqrt[3]{\frac{d}{a}}, 0)$

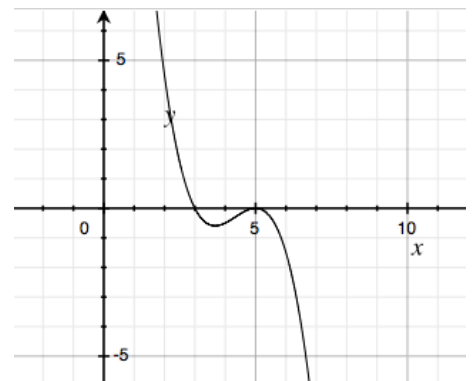


$$y = a(x - p)(x - q)^2$$



Touches x axis at $x = q$
Crosses x axis at $x = p$

Roots: (p, 0) and (q, 0) where $p < q$
(p, 0) then (q, 0)

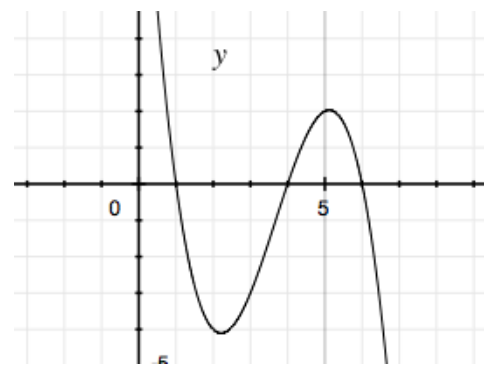
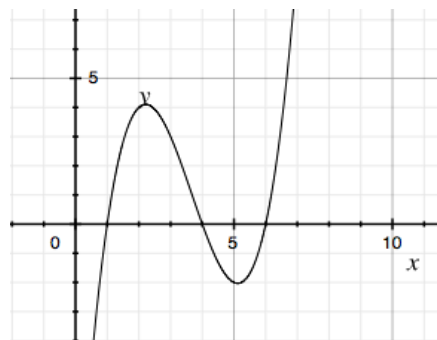


Touches x axis at $x = q$
Crosses x axis at $x = p$

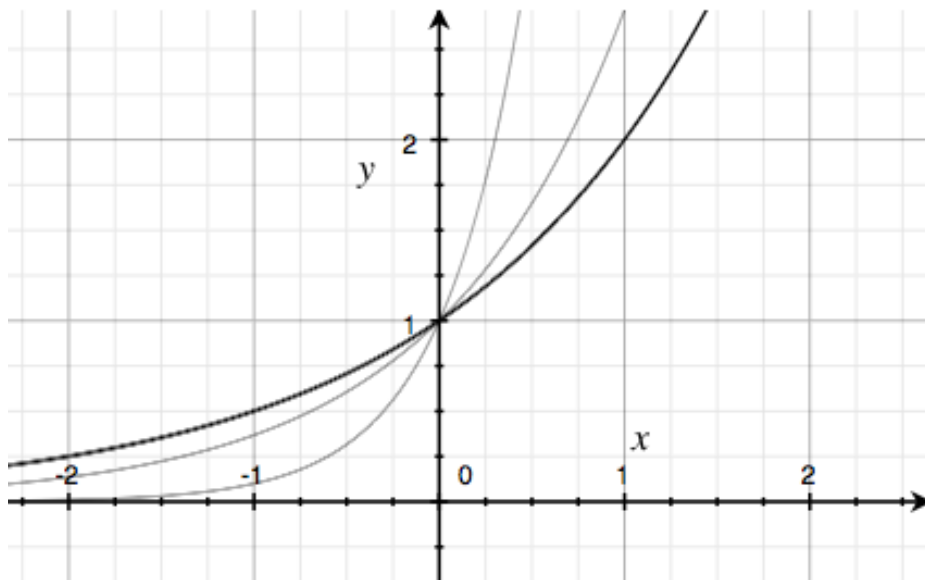
Roots: (p, 0) and (q, 0) where $q < p$
(q, 0) then (p, 0)

$$y = a(x - p)(x - q)(x - r)$$

3 real and distinct roots

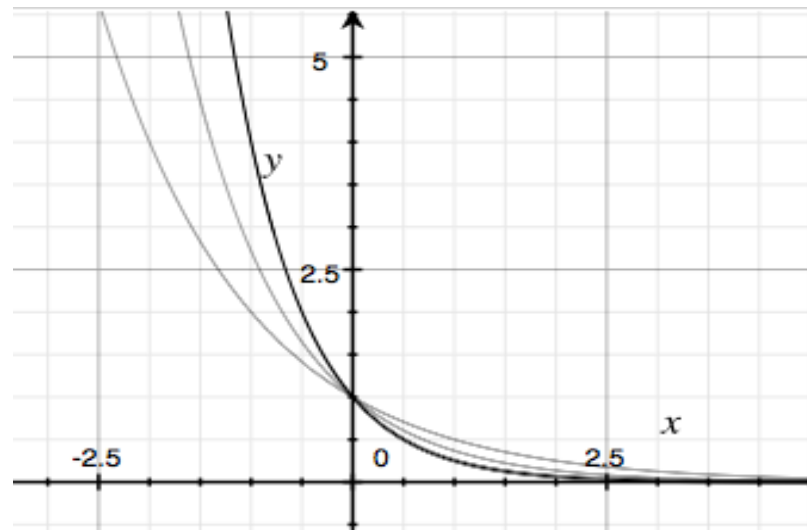


Logarithm Graphs



Graph of $y = a^x$, where $a > 1$.

- Domain: $(-\infty, \infty)$
- Range: $(0, \infty)$
- As value of x increases, value of y increases.
- y intercept: NIL (Graph does not touch x axis, asymptote: $y = 0$)
- x intercept: $(0, 1)$



Graph $y = a^x$, where $a < 1$.

- Domain: $(-\infty, \infty)$
- Range: $(0, \infty)$
- As value of x increases, value of y decreases.
- y intercept: NIL
- x intercept $(0, 1)$

Graphical Transformation

| Equation | Transformation | Values |
|----------------|---|--|
| $y = f(x) + a$ | Graph translates parallel to y axis by a units. | $(x, y \pm a) \rightarrow y$ values change |
| $y = f(x + a)$ | Graph translates parallel to x axis by $-a$ units. | $(x + a, y) \rightarrow x$ values change |
| $y = f(ax)$ | Graph is stretched parallel to the x axis by scale factor $1/a$. | $(x/a, ay) \rightarrow x$ values change |
| $y = af(x)$ | Graph is stretched parallel to the y axis by scale factor a. | $(x, ay) \rightarrow y$ values change |
| $y = -f(x)$ | Graph is reflected in the x axis. | $x, -y \rightarrow y$ values change |
| $y = f(-x)$ | Graph is reflected in the y axis. | $-x, y \rightarrow x$ values change |

For transformations that affect y values, $f(x)$ remains intact.

For transformations that affect x values, change is within bracket.