

Answer **all** the questions.

1. List the following numbers in descending order, starting with the largest.

$1.8^2$

$\pi$

$\sqrt[3]{42}$

$3.14$

$\sqrt[3]{42}$ $1.8^2$ $\pi$ $3.14$	----- B1 for 2 correct positions -----B2 for all correct
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Answer ..... [2]  
(largest) (smallest)

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2. (a) Solve the inequality
- $4y > -38$
- .

$4y > -38$ $y > -9.5$	----- B1
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Answer ..... [1]

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- (b) Find the smallest integer satisfying
- $4y > -38$
- .

$-9$	----- B1
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Answer ..... [1]

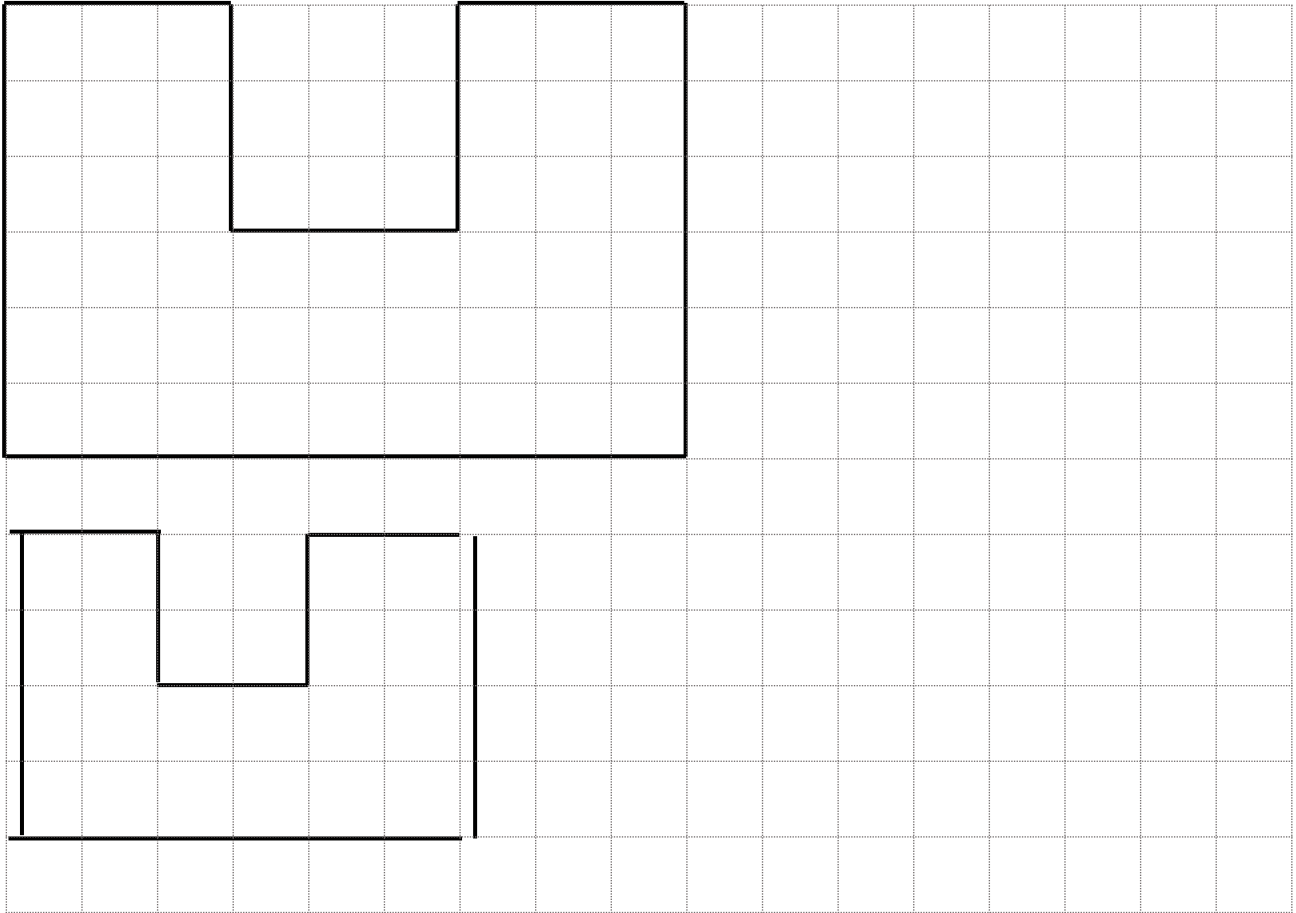
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3. Factorise
- $3xy - py + 6xq - 2pq$
- completely.

$3xy - py + 6xq - 2pq$ $= y(3x - p) + 2q(3x - p)$ $= (y + 2q)(3x - p)$	----- M1 (first line factorisation) ----- A1
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Answer ..... [2]

4. Draw a reduction of the figure using a scale factor of  $\frac{2}{3}$ .  
*Answer*



----- B2/1/0

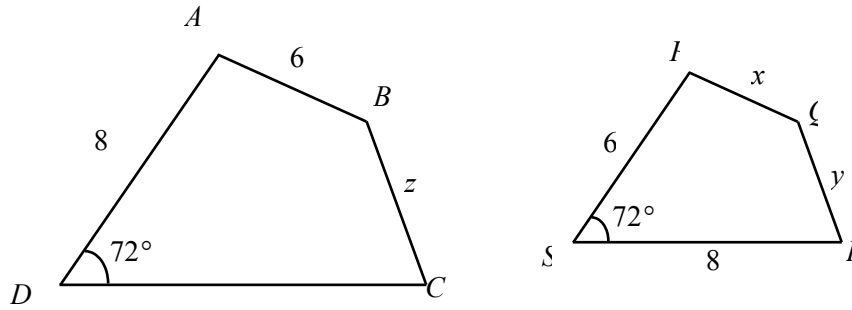
[2]

5. Solve  $3(1 - x) = 15$ .

$3(1 - x) = 15$ $3 - 3x = 15$ $-3x = 15 - 3$ $-3x = 12$ $x = -4$	<p>----- M1 (expand)</p> <p>----- A1 / B1</p>	$3(1 - x) = 15$ $1 - x = \frac{15}{3}$ $1 - x = 5$ $x = -4$	<p>----- M1 (<math>\div 3</math>)</p> <p>----- A1 / B1</p>
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*Answer*  $x = \dots\dots\dots$  [2]

6.



Quadrilaterals  $ABCD$  and  $PQRS$  are similar.

All the lengths are in centimetres.

(a) Calculate  $x$ .

Since figures are similar:

$$\frac{x}{6} = \frac{6}{8}$$

$$8x = 36$$

$$x = 4.5 \text{ cm}$$

----- M1 (O.E)

----- A1 / B2

Answer  $x = \dots\dots\dots$  [2]

(b) Find  $y$  in terms of  $z$ .

$$\frac{y}{z} = \frac{6}{8}$$

$$y = \frac{3z}{4}$$

----- B1

Answer  $y = \dots\dots\dots$  [1]

7.

2, 9, 16, 23, 30, ...

(a) Write down the next 2 terms in the sequence.

37 , 44

----- B1

Answer  $\dots\dots\dots$  ,  $\dots\dots\dots$  [1]

(b) Find an algebraic expression for the  $n$ th term in the sequence.

$7n - 5$

----- B2

Answer  $\dots\dots\dots$  [2]

(c) Find the 154<sup>th</sup> term of this sequence.

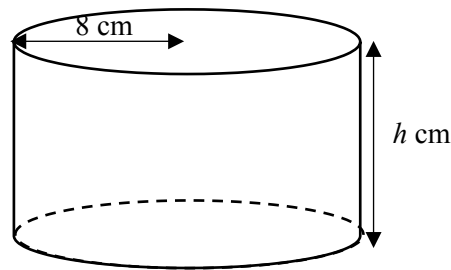
$7(154) - 5 = 1073$

----- B1

Answer  $\dots\dots\dots$  [1]



10. A solid cylinder has radius 8 cm and height  $h$  cm.



Given that the total surface area of the cylinder is  $650 \text{ cm}^2$ , calculate  $h$ .

<p>Total surface area of cylinder = <math>2\pi r^2 + 2\pi rh</math></p> <p><math>2\pi(8)^2 + 2\pi(8)h = 650</math></p> <p><math>128\pi + 16\pi h = 650</math></p> <p><math>16\pi h = 650 - 128\pi</math></p> <p><math>h = \frac{650 - 128\pi}{16\pi}</math></p> <p><math>h = \frac{650 - 128\pi}{16\pi}</math></p> <p><math>= 4.93133</math></p> <p><math>= 4.93 \text{ cm (3 sf)}</math></p>	<p>----- M1 (correct application of formula)</p> <p>----- M1 (isolating h correctly)</p> <p>----- A1</p>
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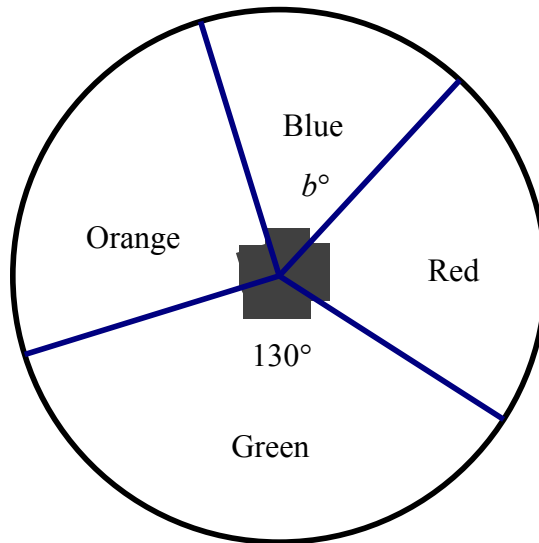
Answer  $h = \dots\dots\dots \text{ cm}$  [3]

11. Simplify  $\frac{3}{x-5} + \frac{x}{x^2-25}$ .

<p><math>\frac{3}{x-5} + \frac{x}{x^2-25} = \frac{3}{x-5} + \frac{x}{(x+5)(x-5)}</math></p> <p><math>= \frac{3(x+5)}{(x-5)(x+5)} + \frac{x}{(x+5)(x-5)}</math></p> <p><math>= \frac{3x+15+x}{(x+5)(x-5)}</math></p> <p><math>= \frac{4x+15}{(x+5)(x-5)}</math></p>	<p>----- M1 (factorization)</p> <p>----- M1 (making single fraction)</p> <p>----- A1</p>
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Answer  $\dots\dots\dots$  [3]

12.



The diagram (not drawn to scale) shows a circle divided into sectors of different colours.

Given that  $\frac{2}{9}$  of the circle is red, find  $b$ .

$\text{Red} = \frac{2}{9} \times 360^\circ$ $= 80^\circ$	-- M1	$\frac{130}{360} + \frac{90}{360} + \frac{2}{9} = \frac{5}{6}$	----- M1
$b = 360^\circ - 80^\circ - 130^\circ - 90^\circ$ $= 60^\circ$	-- M1	$1 - \frac{5}{6} = \frac{1}{6}$	----- M1
	-- A1	$\frac{1}{6} \times 360^\circ = 60^\circ$	----- A1

Answer  $b = \dots\dots\dots$  [3]

13. The equation of a straight line is  $3y = 12 - 2x$ .

Find the coordinates of the point where the line cuts the  $y$ -axis.

$3y = 12 - 2x$ $\text{Let } x = 0, \quad 3y = 12 - 0$ $y = 4$ $(0, 4)$	<p>----- M1 (accept rearranging to make <math>y</math> the subject to find <math>c</math>)</p> <p>----- A1 / B2</p>
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Answer (  $\dots\dots\dots$  ,  $\dots\dots\dots$  ) [2]

$x = \frac{0+4}{2}$ $x = 2$	----- B1
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Answer ..... [1]

16. (a) Rearrange this equation to make  $a$  the subject of the formula.

$$\frac{3a + c}{d} = 2$$

$\frac{3a + c}{d} = 2$	
$3a + c = 2d$	----- M1
$3a = 2d - c$	
$a = \frac{2d - c}{3}$	----- A1

Answer  $a =$  ..... [2]

(b) Hence or otherwise, find the value of  $a$  if  $c = -5$  and  $d = 8$ .

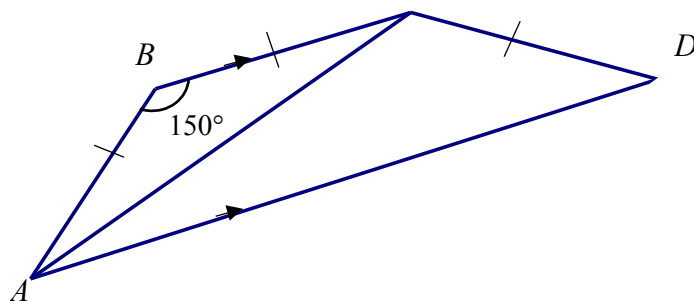
$a = \frac{2(8) - (-5)}{3}$	----- M1
$= 7$	----- A1

Answer  $a =$  ..... [2]

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17. The diagram below shows a trapezium, where  $AB = BC = CD$ ,  $BC$  is parallel to  $AD$  and angle  $ABC = 150^\circ$ .



- (a) Find angle  $ACD$ .

$\text{angle } BCA = \frac{180 - 150}{2} \quad (\text{base angle isosceles triangle})$ $= 15^\circ$	----- M1
$\text{angle } ACD = 150^\circ - 15^\circ$ $= 135^\circ$	----- A1

Answer ..... $^\circ$  [2]

- (b) Explain why  $AC$  bisects angle  $BAD$ . Show working and/or reasons clearly.

Answer

$\text{angle } CAD = 15^\circ \quad (\text{alternate angles})$ $= 15^\circ$	----- M1 (with reason)
$\text{angle } BAC = 15^\circ \quad (\text{base angle isosceles triangle})$	----- M1 (with reason) (give 1m for $15^\circ$ if both reasons not given)
$\text{Since angle } CAD = \text{angle } BAC, AC \text{ bisects angle } BAD,$	----- A1 (conclusion)

A geometric diagram showing a triangle with vertices  $R$ ,  $Q$ , and  $P$ . Vertex  $R$  is at the top left,  $Q$  is at the bottom left, and  $P$  is at the bottom right. The angle at vertex  $R$  is labeled  $77^\circ$ . A horizontal line passes through the triangle, intersecting side  $RQ$  and side  $RP$ . The line is labeled  $c(c)$  on the right side. A line segment labeled  $c(b)$  extends from vertex  $Q$  upwards and to the right, intersecting the horizontal line. Another line segment labeled  $s$  extends from vertex  $P$  upwards and to the left, intersecting the horizontal line. There are several faint, curved lines drawn across the diagram, possibly representing construction arcs or a background pattern.

19.  $(x+1)^2 - 11$  can be expressed in the form  $x^2 + bx + c$ .

(a) Find the value of  $b$  and  $c$ .

$(x+1)^2 - 11 = x^2 + 2x + 1 - 11$ $= x^2 + 2x - 10$	----- M1
$b = 2, c = -10$	----- A1 (or B2)

Answer  $b = \dots\dots\dots, c = \dots\dots\dots$  [2]

(b) Solve the equation  $(x+1)^2 - 11 = 0$ , leaving your answers correct to two decimal places.

$(x+1)^2 - 11 = 0$ $(x+1)^2 = 11$ $x+1 = \sqrt{11} \quad \text{or} \quad x+1 = -\sqrt{11}$ $x = \sqrt{11} - 1 \quad \text{or} \quad x = -\sqrt{11} - 1$ $x = 2.32 \quad \text{or} \quad x = -4.32$	----- M1
	----- A1 (both correct)

Answer  $x = \dots\dots\dots$  or  $x = \dots\dots\dots$  [2]

20. (a) Jae invested \$4500 at 2.5% compound interest per annum, compounded annually.

Calculate the compound interest Jae will receive at the end of 5 years?

Give your answer correct to the nearest cent.

$A = P \left( 1 + \frac{r}{100} \right)^n$ $A = \$4500 \left( 1 + \frac{2.5}{100} \right)^5$ $= \$5091.34$	----- M1
$\text{Interest} = \$5091.34 - \$4500$ $= \$591.34$	----- M1 (their A - P) ----- A1

Answer \$  $\dots\dots\dots$  [3]

(b) Gina invested some money in government bonds.

One year later her investment had gained 8.5% of its original value.

It was then worth \$8029.

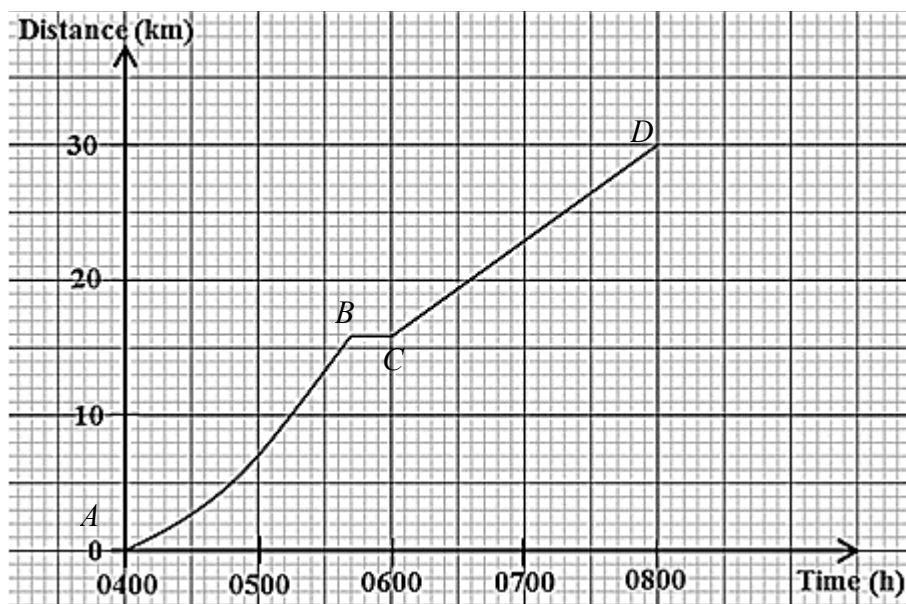
How much did Gina invest originally?

$\frac{\$8029}{108.5} \times 100$ $= \$7400$	----- M1
	----- A1

Answer \$  $\dots\dots\dots$  [2]

21. George participated in a 30 km marathon.

The distance-time graph below represents his run from the start to finish.



(a) What does the line  $BC$  represent?

**George is at rest / not moving ----- B1 (O.E)**

Answer ..... [1]

(b) How long did it take for George to reach point B?

**1 h 42 min ----- B1**

Answer ..... h ..... min [1]

(c) 'George's average running speed from  $A$  to  $B$  is faster than his average running speed from  $C$  to  $D$ .'

Is this statement correct? Explain your answer.

Answer

$$\text{AB Speed} = 16 \div 1\frac{7}{10} = 9.4117 \text{ km/h}$$

$$\text{CD speed} = 14 \div 2 = 7 \text{ km/h}$$

The statement is correct because speed AB is faster than speed CD.

Alternatively:

From A to B, George covers 16 km in less than 2 hours. Whereas from C to D, George covers 14 km in 2 hours, covering less distance in longer time.

Hence, the statement is correct,

----- M1 (either correct speed)

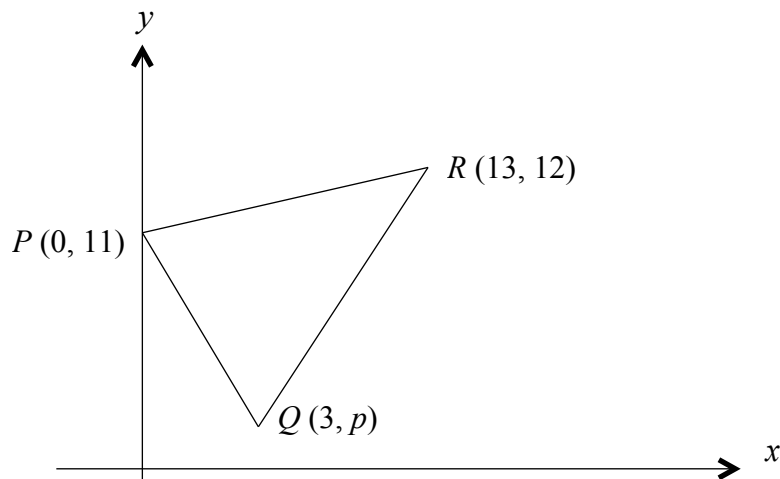
----- A1

M1 (compare distance with time covered)

A1

22. The diagram below, which is not drawn to scale, shows a triangle  $PQR$ .

The coordinates of  $P$ ,  $Q$  and  $R$  are  $(0, 11)$ ,  $(3, p)$  and  $(13, 12)$  respectively.



(a) Find the length of  $PR$ , leaving your answer correct to 2 decimal places.

$\begin{aligned}\text{Length } PR &= \sqrt{(12-11)^2 + (13-0)^2} \\ &= 13.0384 \\ &= 13.04 \text{ units}\end{aligned}$	<p>----- M1</p> <p>----- A1</p>
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Answer ..... [2]

(b) Given that the gradient of  $RQ$  is 1, find the value of  $p$ .

$\begin{aligned}\frac{12-p}{13-3} &= 1 \\ 12-p &= 10 \\ p &= 2\end{aligned}$	<p>----- M1</p> <p>----- A1 / B2</p>
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Answer ..... [2]

(c) Find the equation of  $RQ$ .

$\begin{aligned}y &= mx + c \\ \text{Equation } RQ, \text{ using } (3, 2): \\ 2 &= 3 + c \\ c &= -1 \\ \text{Answer : } y &= x - 1\end{aligned}$	<p>----- M1</p> <p>----- A1</p>
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Answer ..... [2]