

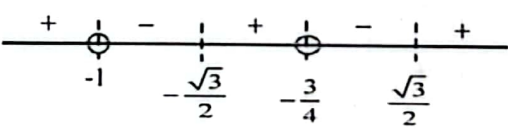
ANNEX B

IJC H2 Preliminary Examination (Paper 2)

Qn/No	Topic Set	Answers
1	Inequalities	$x < -1$ or $-\frac{\sqrt{3}}{2} \leq x < -\frac{3}{4}$ or $x \geq \frac{\sqrt{3}}{2}$; $x < \ln\left(\frac{\sqrt{3}}{2}\right)$
2	AP and GP	(i) 9 (iii) $x \geq 8755$ (last part) Software Y is unable to remove all the comments because eventually it is only able to remove 150 000 comments.
3	Differential Equations	(i) $x = \frac{5e^{\frac{1}{2}t}}{4 + e^{\frac{1}{2}t}}$ (ii) $2\ln\left(\frac{8}{3}\right)$ years (iii) The population of wild boars will increase and stabilise at 500 eventually.
4	Vectors (Lines and Planes)	(i) $\theta = 67.8^\circ$ (ii) $(-1, 1, -3)$ (iii) $\begin{pmatrix} -2 \\ 0 \\ -4 \end{pmatrix}$ (iv) $\mathbf{r} = \begin{pmatrix} -1 \\ 1 \\ -3 \end{pmatrix} + \alpha \begin{pmatrix} 4 \\ 1 \\ -2 \end{pmatrix}, \alpha \in \mathbb{R}$
5	Sampling Methods	(i) Systematic sampling (ii) (slower, more difficult to collect) Systematic sampling is a more tedious process to select the employees, whereas quota sampling is quick and easy.
6	Sampling distribution (Central Limit Theorem)	143
7	Probability	(i) 0.902 (ii) 0.199
8	Hypothesis Testing	(i) 44.1; 3.52 (ii) The battery life of a PI-99 calculator is assumed to be normally distributed.

		$H_0: \mu = k$ (iii) $H_1: \mu \neq k$ (iv) $\{k \in \mathbb{R}: 42.97 < k < 45.24\}$
9	Poisson Distribution	(i) The average number of faults detected by each system (for the track and the train) is constant from one day to another. (ii) 0.629 (iii) 8 (iv) 0.237
10	Binomial Distribution	(i) Ben's performance (i.e. whether he loses or wins) in a game is independent of any other games that he plays with Alex. (ii) 0.850 (iii) 14 (iv) 0.910
11	Correlation & Regression	(ii)(a) -0.8454 (ii)(b) -0.9961 (iii) m and $\ln t$ is the better model; $m = 179 - 31.2 \ln t$ (iv) 22.61 micrograms per litre ; The estimate obtained is reliable, because the given value of $t = 150$ lies within the given sample data range for t and the product moment correlation coefficient between m and $\ln t$ is very close to -1 , hence indicating a strong negative linear correlation between the variables m and $\ln t$.
12	Normal Distribution	(i) 0.809 (ii) 0.375 (last part) 0.916

Innova Junior College
H2 Mathematics
JC2 Preliminary Examinations Paper 2
Solutions

1	Solution
	$\frac{3}{4x+3} \leq \frac{x}{x+1}$ $\frac{3}{4x+3} - \frac{x}{x+1} \leq 0$ $\frac{3x+3-4x^2-3x}{(4x+3)(x+1)} \leq 0$ $\frac{-4x^2+3}{(4x+3)(x+1)} \leq 0 \quad \text{--- (*)}$ $\frac{4x^2-3}{(4x+3)(x+1)} \geq 0$ $\frac{(2x-\sqrt{3})(2x+\sqrt{3})}{(4x+3)(x+1)} \geq 0$ <div style="text-align: center;">  </div> <p>Hence $x < -1$ or $-\frac{\sqrt{3}}{2} \leq x < -\frac{3}{4}$ or $x \geq \frac{\sqrt{3}}{2}$</p>
	<p>For $\frac{3}{4e^x+3} > \frac{e^x}{e^x+1}$, making use of the result in above part,</p> $-1 < e^x < -\frac{\sqrt{3}}{2} \quad \text{or} \quad -\frac{3}{4} < e^x < \frac{\sqrt{3}}{2}$ <p>(no solns since e^x is always positive)</p> <p>Hence, $e^x < \frac{\sqrt{3}}{2} \Rightarrow x < \ln\left(\frac{\sqrt{3}}{2}\right)$</p>

2 Solution

(i)

Hour	Start of hour	End of hour
1	1	$1 + 3 = 4$
2	4	$4 + 12 = 16$
3	16	$16 + 48 = 64$
4

$$4(4)^{n-1} > 200\,000$$

$$(4)^{n-1} > 50\,000$$

$$n-1 > 7.80482$$

$$n > 8.80842$$

Number of complete hours = 9

Alternative Solution

$$4(4)^{n-1} > 200\,000$$

n	Total
8	$65536 < 200\,000$
9	$262144 > 200\,000$
10	$11048576 > 200\,000$

Number of complete hours = 9

(ii)

Day	Start of day	End of day
1	$200000 - x$	$1.02(200000 - x)$
2	$1.02(200000 - x) - x$	$1.02[1.02(200000 - x) - x]$ $= 1.02^2(200000) - 1.02x - 1.02^2x$
3

At the end of day n , the number comments

$$= 1.02^n(200000) - (1.02x + 1.02^2x + \dots + 1.02^n x) \dots (*)$$

	$= 1.02^n (200000) - x \left(\frac{1.02(1.02^n - 1)}{0.02} \right)$ $= 1.02^n (200000) - 51x(1.02^n - 1)$
(iii)	$1.02^{30} (200\ 000) - 51x(1.02^{30} - 1) < 0$ $x > \frac{1.02^{30} (200\ 000)}{51(1.02^{30} - 1)}$ $x \geq 8755 \text{ (to nearest integer)}$
	<p>Day 1: no. of comments removed = 15000</p> <p>Day 2: no. of comments removed = $15000(0.9)$</p> <p>Day 3: no. of comments removed = $15000(0.9)^2$</p> <p>As $n \rightarrow \infty$, no. of comments removed</p> $= \frac{15000}{1-0.9} = 150\ 000$ <p>Software Y is unable to remove all the comments because eventually it is only able to remove 150 000 comments.</p>

3	Solution
(i)	<p><u>Method 1:</u></p> $\int \frac{1}{x(5-x)} dx = \int \frac{1}{10} dt \text{ ----} (*)$ <p>Doing partial fractions</p> $\frac{1}{x(5-x)} = \frac{A}{x} + \frac{B}{5-x}$ $= \frac{A(5-x) + B(x)}{x(5-x)}$ $A = \frac{1}{5}$ $B = \frac{1}{5}$ $\int \frac{1}{5x} + \frac{1}{5(5-x)} dP = \int \frac{1}{10} dt$ $\frac{1}{5} [\ln x - \ln 5-x] = \frac{1}{10} t + c$ $\ln \left \frac{x}{5-x} \right = \frac{1}{2} t + c$ $\frac{x}{5-x} = Ae^{\frac{1}{2}t}, \text{ where } A = \pm e^c$ <p>Given $x=1$ when $t=0$, $\frac{1}{5-1} = Ae^0 \Rightarrow A = \frac{1}{4}$</p> $x = \frac{5}{4} e^{\frac{1}{2}t} - \frac{1}{4} x e^{\frac{1}{2}t}$ $x(4 + e^{\frac{1}{2}t}) = 5e^{\frac{1}{2}t}$ $x = \frac{5e^{\frac{1}{2}t}}{4 + e^{\frac{1}{2}t}}$

(i)	<p><u>Method 2:</u></p> $\int \frac{1}{x(5-x)} dx = \int \frac{1}{10} dt \quad \text{--- (*)}$ $\int \frac{1}{\frac{25}{4} - (x - \frac{5}{2})^2} dx = \int \frac{1}{10} dt$ $\frac{1}{2(\frac{5}{2})} \ln \left \frac{\frac{5}{2} + (x - \frac{5}{2})}{\frac{5}{2} - (x - \frac{5}{2})} \right = \frac{1}{10} t + c$ $\ln \left \frac{x}{5-x} \right = \frac{1}{2} t + c$ $\frac{x}{5-x} = Ae^{\frac{1}{2}t}, \text{ where } A = e^{\pm c}$ <p>Given $x = 1$ when $t = 0$, $\frac{1}{5-1} = Ae^0 \Rightarrow A = \frac{1}{4}$</p> $x = \frac{5}{4} e^{\frac{1}{2}t} - \frac{1}{4} x e^{\frac{1}{2}t}$ $x(4 + e^{\frac{1}{2}t}) = 5e^{\frac{1}{2}t}$ $x = \frac{5e^{\frac{1}{2}t}}{4 + e^{\frac{1}{2}t}} \quad \text{or} \quad x = \frac{5}{4e^{-\frac{1}{2}t} + 1}$
(ii)	<p>When $x = 2$, $\frac{5e^{\frac{1}{2}t}}{4 + e^{\frac{1}{2}t}} = 2$</p> $8 + 2e^{\frac{1}{2}t} = 5e^{\frac{1}{2}t}$ $3e^{\frac{1}{2}t} = 8$ $e^{\frac{1}{2}t} = \frac{8}{3}$ $t = 2 \ln \left(\frac{8}{3} \right)$ <p>It takes $t = 2 \ln \left(\frac{8}{3} \right)$ years.</p>
(iii)	<p>As $t \rightarrow \infty$, $x \rightarrow 5$. \therefore The population of wild boars will increase and stabilise at 500 eventually.</p>

4	Solution
(i)	<p> $l: \mathbf{r} = \begin{pmatrix} 1 \\ 0 \\ -7 \end{pmatrix} + \lambda \begin{pmatrix} -2 \\ 1 \\ 4 \end{pmatrix}$, where λ is a real parameter. </p> <p> $p: \mathbf{r} \cdot \begin{pmatrix} 1 \\ 0 \\ -1 \end{pmatrix} = 2$ </p> <p> $\sin \theta = \frac{\left \begin{pmatrix} -2 \\ 1 \\ 4 \end{pmatrix} \cdot \begin{pmatrix} 1 \\ 0 \\ -1 \end{pmatrix} \right }{\left \begin{pmatrix} -2 \\ 1 \\ 4 \end{pmatrix} \right \left \begin{pmatrix} 1 \\ 0 \\ -1 \end{pmatrix} \right } = \frac{6}{\sqrt{21}\sqrt{2}}$ </p> <p> $\therefore \theta = 67.8^\circ$ (1 dec pl) </p>
(ii)	<p>For the point of intersection between l and p,</p> <p> $\begin{pmatrix} 1-2\lambda \\ \lambda \\ -7+4\lambda \end{pmatrix} \cdot \begin{pmatrix} 1 \\ 0 \\ -1 \end{pmatrix} = 2$ </p> <p> $1-2\lambda+7-4\lambda=2$ $\lambda=1$ </p> <p> The position vector of point of intersection is $\begin{pmatrix} 1 \\ 0 \\ -7 \end{pmatrix} + \begin{pmatrix} -2 \\ 1 \\ 4 \end{pmatrix} = \begin{pmatrix} -1 \\ 1 \\ -3 \end{pmatrix}$. </p> <p>Coordinates of point of intersection are $(-1, 1, -3)$.</p>
(iii)	<p>The line perpendicular to p passing through $(1, 0, -7)$ is</p> <p> $\mathbf{r} = \begin{pmatrix} 1 \\ 0 \\ -7 \end{pmatrix} + \mu \begin{pmatrix} 1 \\ 0 \\ -1 \end{pmatrix}, \mu \in \mathbb{R}$ </p> <p> $\begin{pmatrix} 1+\mu \\ 0 \\ -7-\mu \end{pmatrix} \cdot \begin{pmatrix} 1 \\ 0 \\ -1 \end{pmatrix} = 2$ </p> <p> $1+\mu+7+\mu=2$ </p>

	$2\mu = -6$ $\mu = -3$ $\vec{ON} = \begin{pmatrix} 1-3 \\ 0 \\ -7+3 \end{pmatrix} = \begin{pmatrix} -2 \\ 0 \\ -4 \end{pmatrix}$
(iv)	<p><u>Method 1:</u></p> <p>Let the coordinates of A be $(1, 0, -7)$. Let A' be the reflected point of A in p.</p> <p>Using ratio theorem, $\vec{ON} = \frac{\vec{OA} + \vec{OA'}}{2}$</p> $\Rightarrow \vec{OA'} = 2\vec{ON} - \vec{OA} = 2 \begin{pmatrix} -2 \\ 0 \\ -4 \end{pmatrix} - \begin{pmatrix} 1 \\ 0 \\ -7 \end{pmatrix} = \begin{pmatrix} -5 \\ 0 \\ -1 \end{pmatrix}$ <p>The reflected line contains the point A' and point of intersection between l and p.</p> <p>The direction vector of the reflected line is $\begin{pmatrix} -1 \\ 1 \\ -3 \end{pmatrix} - \begin{pmatrix} -5 \\ 0 \\ -1 \end{pmatrix} = \begin{pmatrix} 4 \\ 1 \\ -2 \end{pmatrix}$</p> $\therefore \mathbf{r} = \begin{pmatrix} -1 \\ 1 \\ -3 \end{pmatrix} + \alpha \begin{pmatrix} 4 \\ 1 \\ -2 \end{pmatrix}, \alpha \in \mathbb{R}$
(iv)	<p><u>Method 2:</u></p> <p>Let the coordinates of A be $(1, 0, -7)$. Let A' be the reflected point of A in p. Let the coordinates of B be $(-1, 1, -3)$.</p> $\vec{BN} = \frac{\vec{BA} + \vec{BA'}}{2}$ $\vec{BA'} = 2\vec{BN} - \vec{BA}$ $= 2 \begin{pmatrix} -2 \\ 0 \\ -4 \end{pmatrix} - 2 \begin{pmatrix} -1 \\ 1 \\ -3 \end{pmatrix} - \begin{pmatrix} 1 \\ 0 \\ -7 \end{pmatrix} + \begin{pmatrix} -1 \\ 1 \\ -3 \end{pmatrix} = \begin{pmatrix} -4 \\ -1 \\ 2 \end{pmatrix}$ $\therefore \mathbf{r} = \begin{pmatrix} -1 \\ 1 \\ -3 \end{pmatrix} + \alpha \begin{pmatrix} -4 \\ -1 \\ 2 \end{pmatrix}, \alpha \in \mathbb{R}$

5	Solution						
(i)	Systematic sampling						
(ii)	<p>(slower, more difficult to collect) Systematic sampling is a more tedious process to select the employees, whereas quota sampling is quick and easy.</p> <p>Another possible reason: might miss out a certain group of people due to different reporting times.</p>						
(iii)	<p>The interviewer could consider transport mode of the employees as the stratum. A possible quota for each stratum is as follows:</p> <table><tr><td>By private transport</td><td>By public transport</td><td>By walking</td></tr><tr><td>10</td><td>10</td><td>10</td></tr></table> <p>The interviewer can then stand at the entrance of the building and select the sample until the above quota is met.</p>	By private transport	By public transport	By walking	10	10	10
By private transport	By public transport	By walking					
10	10	10					

6	Solution
	<p>$E(X) = 1.93$ $\text{Var}(X) = 1.4$</p> <p>Since n is large, by Central Limit Theorem,</p> <p>$\bar{X} \sim N\left(1.93, \frac{1.4}{n}\right)$ approximately.</p> <p>Given that $P(\bar{X} > 2) < 0.24 \dots (*)$</p>
	<p><u>Method 1: Using GC to set up table</u></p> <p>when $n = 142$, $P(\bar{X} > 2) = 0.24041$ (> 0.24)</p> <p>when $n = 143$, $P(\bar{X} > 2) = 0.23964$ (< 0.24)</p> <p>when $n = 144$, $P(\bar{X} > 2) = 0.23887$ (< 0.24)</p> <p>\therefore least n is 143.</p>
	<p><u>Method 2: Using algebraic method via standardization</u></p> <p>$P(\bar{X} \leq 2) > 0.76$</p> $P\left(Z \leq \frac{2 - 1.93}{\sqrt{1.4/n}}\right) > 0.76$

From GC,

$$\frac{2-1.93}{\sqrt{1.4/n}} > 0.70630 \quad \text{---}(**)$$

$$\sqrt{n} > \frac{0.70630}{0.07} \sqrt{1.4}$$

$$\sqrt{n} > 11.939$$

$$n > 142.53$$

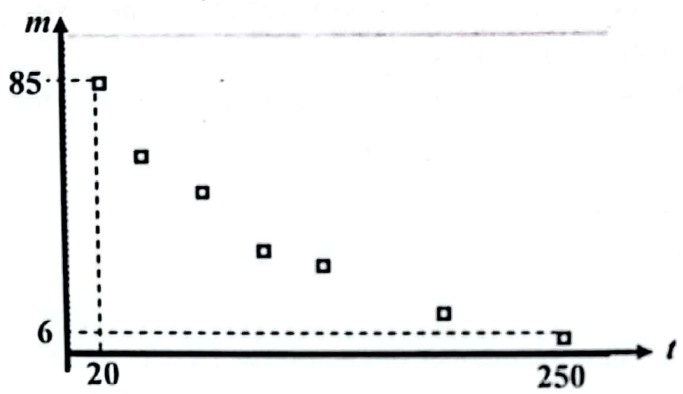
\therefore least n is 143.

7	Solution
(i)	<p><u>Method 1:</u> Required probability $= 1 - \frac{{}^{13}C_4}{{}^{24}C_4} - \frac{{}^{11}C_4}{{}^{24}C_4} = 0.902 \text{ (3 sig fig)}$</p> <p><u>Method 2:</u> Required probability $= 1 - \frac{13 \times 12 \times 11 \times 10}{24 \times 23 \times 22 \times 21} - \frac{11 \times 10 \times 9 \times 8}{24 \times 23 \times 22 \times 21} = 0.902 \text{ (3 sig fig)}$</p> <p><u>Method 3:</u> Required probability $= \frac{{}^{11}C_1 \times {}^{13}C_3 + {}^{11}C_2 \times {}^{13}C_2 + {}^{11}C_3 \times {}^{13}C_1}{{}^{24}C_4}$ $= 0.902 \text{ (3 sig fig)}$</p>
(ii)	<p><u>Method 1:</u> Required probability $= \frac{{}^{11}C_2 \times 2! \times {}^{22}C_2 \times 2!}{{}^{24}C_4 \times 4!} = 0.199 \text{ (3 sig fig)}$</p> <p><u>Method 2:</u> Required probability $= \frac{11 \times 10 \times 22 \times 21}{24 \times 23 \times 22 \times 21} = 0.199 \text{ (3 sig fig)}$</p>

8	Solution
(i)	<p>Unbiased estimate of the population mean</p> $\bar{x} = \frac{573.39}{13} = 44.10692308 = 44.1 \text{ (3 s.f.)}$ <p>Unbiased estimate of the population variance</p> $s^2 = \frac{42.22}{12} = 3.518333333 = 3.52 \text{ (3 s.f.)}$
(ii)	The battery life of a PI-99 calculator is assumed to be normally distributed.
(iii)	<p>Let X be the r.v. denoting the battery life of a randomly chosen PI-99 calculator. Let μ be the population mean battery life of the PI-99 calculators.</p> <p>$H_0: \mu = k$ $H_1: \mu \neq k$</p> <p>where H_0 is the null hypothesis and H_1 is the alternative hypothesis.</p>
(iv)	<p>To test at 5% level of significance.</p> <p>Under H_0, the test statistic is $T = \frac{\bar{X} - k}{\frac{S}{\sqrt{13}}} \sim t_{(12)}$.</p> <p>Since the null hypothesis is not rejected, t-value falls outside critical region. $\therefore -2.178812 < t\text{-value} < 2.178812$</p> $-2.178812 < \frac{\bar{x} - k}{\frac{s}{\sqrt{13}}} < 2.178812 \text{ --- (*)}$ $\bar{x} - 2.178812 \left(\frac{s}{\sqrt{13}} \right) < k < \bar{x} + 2.178812 \left(\frac{s}{\sqrt{13}} \right)$ <p>where $\bar{x} = 44.10692$ and $s = \sqrt{3.51833}$</p> <p>$\therefore 42.97 < k < 45.24$</p> <p>The required set is $\{k \in \mathbb{R} : 42.97 < k < 45.24\}$</p>

9	Solution
(i)	The average number of faults detected by each system (for the track and the train) is constant from one day to another.
(ii)	<p>Let X be the r.v. denoting the total number of faults detected by the two systems in a periods of 10 days.</p> <p>$X \sim \text{Po}((0.25 + 0.15) \times 10)$, i.e. $X \sim \text{Po}(4)$</p> <p>$\therefore P(X \leq 4) = 0.6288369 = 0.629$ (3 sig fig)</p>
(iii)	<p>Let Y be the r.v. denoting the total number of faults detected by the two systems in a period of n days.</p> <p>$Y \sim \text{Po}(0.4n)$</p> <p>Given $P(Y = 0) < 0.05$,</p> <p><i>Method 1: Algebraic method</i></p> $e^{-0.4n} < 0.05 \quad (\text{o.e. } (e^{-0.25n})(e^{-0.15n}) < 0.05)$ $n > 7.489$ <p>\therefore the smallest number of days required is 8.</p> <p><i>Method 2: GC table</i></p> <p>When $n = 7$, $P(Y = 0) = 0.06081$ (> 0.05)</p> <p>When $n = 8$, $P(Y = 0) = 0.04076$ (< 0.05)</p> <p>When $n = 9$, $P(Y = 0) = 0.02732$ (< 0.05)</p> <p>\therefore the smallest number of days required is 8.</p>
(iv)	<p>Let W and V be the r.v. denoting the number of faults detected on the track and on the track in a period of 10 days respectively.</p> <p>$W \sim \text{Po}(2.5)$ and $V \sim \text{Po}(1.5)$</p> <p>Required probability</p> $= P(W \geq 3 V + W \leq 4)$ $= \frac{P(W \geq 3 \cap V + W \leq 4)}{P(V + W \leq 4)}$ $= \frac{P(W = 3)P(V = 0) + P(W = 3)P(V = 1) + P(W = 4)P(V = 0)}{P(V + W \leq 4)}$ $= \frac{P(W = 3)P(V \leq 1) + P(W = 4)P(V = 0)}{P(V + W \leq 4)}$ <p>$= 0.237$ (3 sig fig)</p>

10	Solution
(i)	Ben's performance (i.e. whether he loses or wins) in a game is independent of any other games that he plays with Alex.
(ii)	<p>Let X be the r.v. denoting the number of games that Ben loses out of 10 games.</p> $X \sim B(10, 0.7)$ $P(X > 5) = 1 - P(X \leq 5)$ $= 0.84973$ $\approx 0.850 \text{ (3 sig fig)}$
(iii)	<p>Let Y be the r.v. denoting the number of games that Ben loses out of n games.</p> $Y \sim B(n, 0.3)$ $P(Y > 8) \leq 0.01$ $1 - P(Y \leq 8) \leq 0.01$ <p>Using GC,</p> <p>When $n = 13$, $P(Y > 8) = 0.00403$ (< 0.01)</p> <p>When $n = 14$, $P(Y > 8) = 0.00829$ (< 0.01)</p> <p>When $n = 15$, $P(Y > 8) = 0.01524$ (> 0.01)</p> <p>\therefore the greatest value of n is 14.</p>
(iv)	<p>Let W be the r.v. denoting the number of games that Ben loses out of 50 games.</p> $W \sim B(50, 0.3)$ <p>As $n = 50$ is large, $np = 15$ (> 5) and $nq = 35$ (> 5),</p> <p>$\therefore W \sim N(15, 10.5)$ approximately</p> $P(10 \leq W \leq 20) = P(9.5 \leq W \leq 20.5) \text{ --- (*)}$ $= 0.910 \text{ (3 sig fig)}$

11	Solution
(i)	 <p>From the scatter diagram, a curvilinear correlation is observed between m and t (i.e. as t increases, m decreases at a decreasing rate), and hence a linear model with equation of the form $m = a + bt$ cannot be used to model the relationship between m and t.</p>
(ii)	Product moment correlation coefficient between m and $t^2 = -0.8454$.
(a)	
(b)	Product moment correlation coefficient between m and $\ln t = -0.9961$.
(iii)	<p>Since the absolute value of the correlation coefficient between m and $\ln t$ (i.e. case (b)) is <u>closer</u> to 1, this indicates that the linear correlation between the variables m and $\ln t$ is <u>stronger</u> as compared to that between the variables for case (a).</p> <p>\therefore case (b) is the better model for the relationship between m and t.</p> $m = 179.026 - 31.2175 \ln t$ $\Rightarrow m = 179 - 31.2 \ln t \text{ (3 sig fig)}$
(iv)	<p>When $t = 150$,</p> $m = 179.026 - 31.2175 \ln 150 = 22.61 \text{ (2 dec pl)}$ <p>The estimate obtained is reliable, because the given value of $t = 150$ lies within the given sample data range for t and the product moment correlation coefficient between m and $\ln t$ is very close to -1, hence indicating a strong negative linear correlation between the variables m and $\ln t$.</p>

12	Solution
(i)	$X + Y \sim N(50, 32.65)$ $P(X + Y > 45) = 0.809224 = 0.809 \text{ (3 sig fig)}$
(ii)	$E(X + Y - S) = 12$ $\text{Var}(X + Y - S) = 39.41$ $\therefore X + Y - S \sim N(12, 39.41)$ $P(\text{method A is faster than method B by more than 5 mins})$ $= P(S + 15 - (X + Y) > 5)$ $= P(X + Y - S < 10)$ $= 0.375020 = 0.375 \text{ (3 sig fig)}$
(iii)	<p>Let $A = X + Y$ and $B = S + 15$.</p> <p>$A \sim N(50, 32.65)$ and $B \sim N(53, 2.6^2)$</p> <p>Let $W = \frac{A_1 + A_2 + A_3 + A_4 + B_1 + \dots + B_6}{10}$</p> <p>$\therefore E(W) = \frac{50 \times 4 + 53 \times 6}{10} = 51.8$</p> <p>& $\text{Var}(W) = \frac{32.65 \times 4 + 2.6^2 \times 6}{10^2} = 1.7116$</p> <p>$\therefore W \sim N(51.8, 1.7116)$</p> <p>Required probability</p> <p>$= P(W > 50)$</p> <p>$= 0.915566 = 0.916 \text{ (3 sig fig)}$</p>